

UPDATED

whitson

BHP in whitson+

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Course held Virtually

24 April 2024



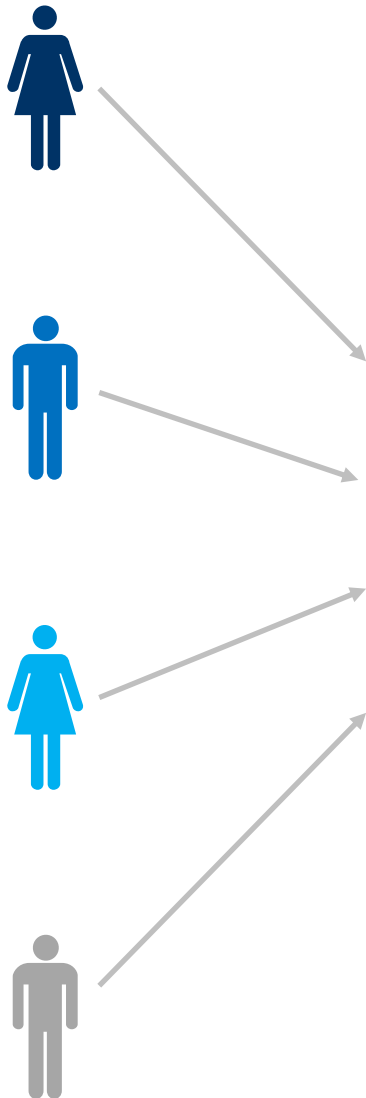
General Information

General Information

- ½ day course
- Interactive class
- Ask questions – drive the course emphasis
 - In chat or unmute to speak (mute when not talking 😊)
- Will send out all digital material after class
- Some content in this slide deck is meant for presentation purposes, while some parts are meant for reference.

Software

Access to whitson+



DO NOT USE COMPANY DOMAIN!
Not same as your company domain

<https://courses.whitson.com/>

Username: your e-mail

Password: WhitsonBHP2024

*Send an e-mail to support@whitson.com if you need help to login.
Need to use Google Chrome, Firefox or Microsoft Edge.
Internet Explorer won't work.

Agenda

Course Agenda

BHP Calculation Fundamentals

- Why calculate BHP
- Input to the BHP calculation
- BHP Correlations
- Flowpaths and artificial lift methods
- BHP Smoothing & Tuning
- Estimate initial reservoir pressure with IPR

Exercises in **whitson⁺**

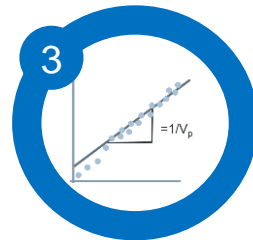


Unconventional Reservoir Workflow

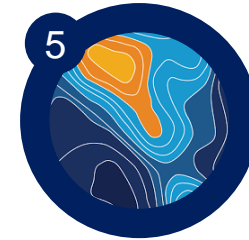
PVT & Fluids



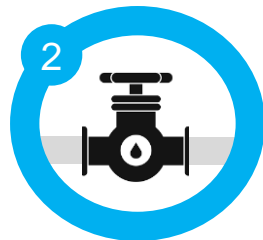
Multiphase FMB



Simulation + Forecast



Bottomhole Pressure
Calculations



Analytical &
Numerical RTA

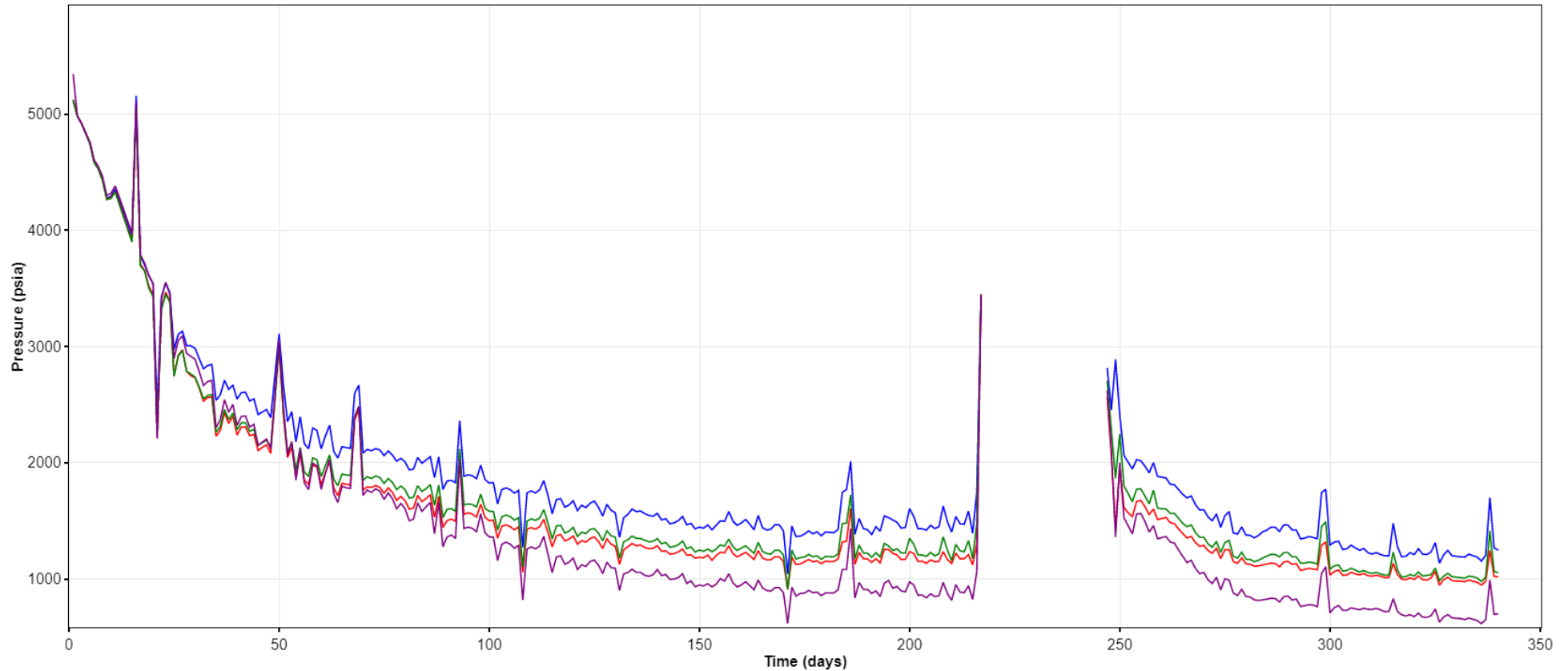


Flowing Bottomhole Pressures (p_{wf})

Bottomhole Pressure ☐ Smoothed results ☐ Dates

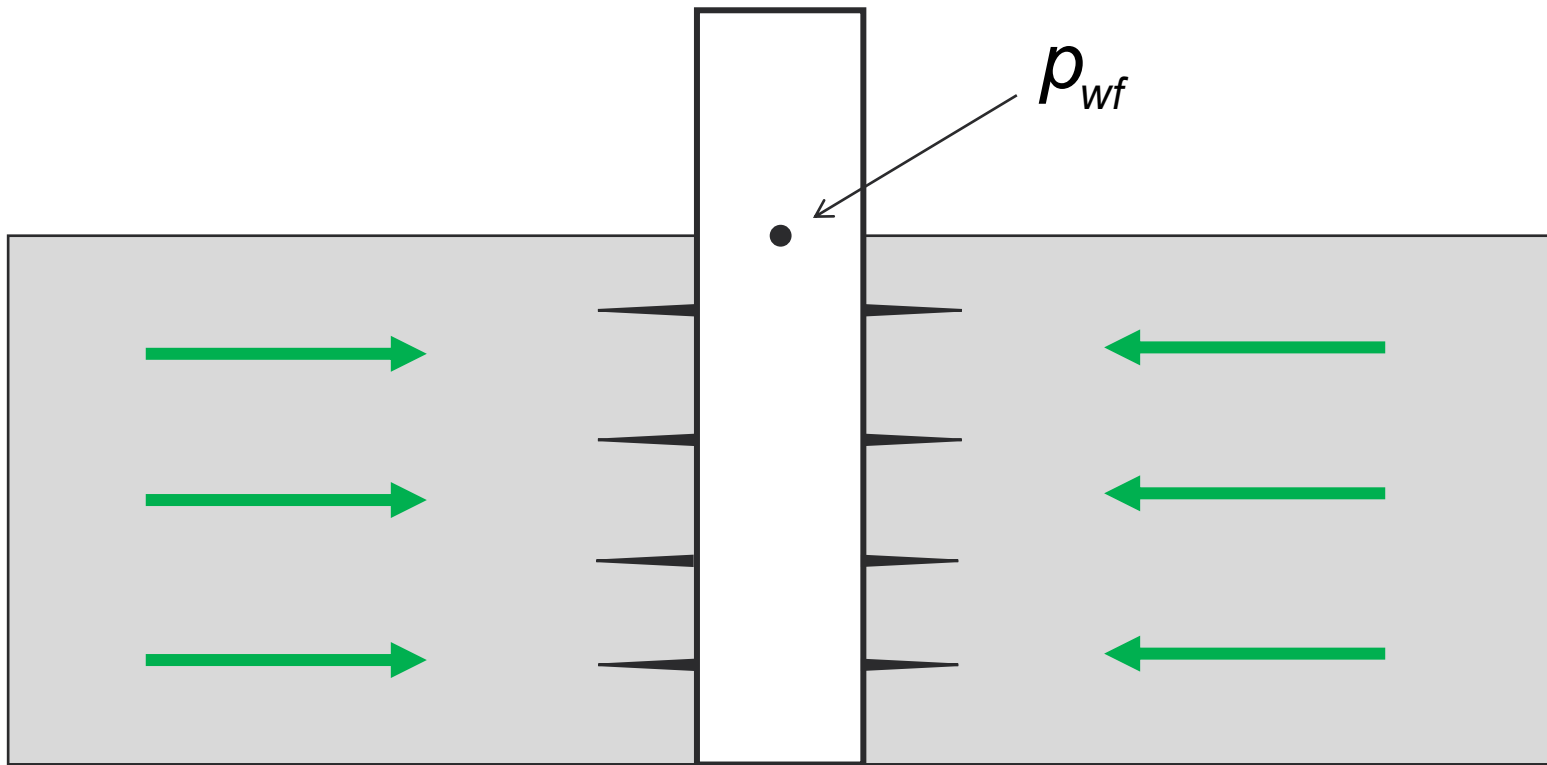


$p_{wf, gauge}$ Beggs & Brill Hagedorn & Brown Woldesemayat & Ghajar Gray



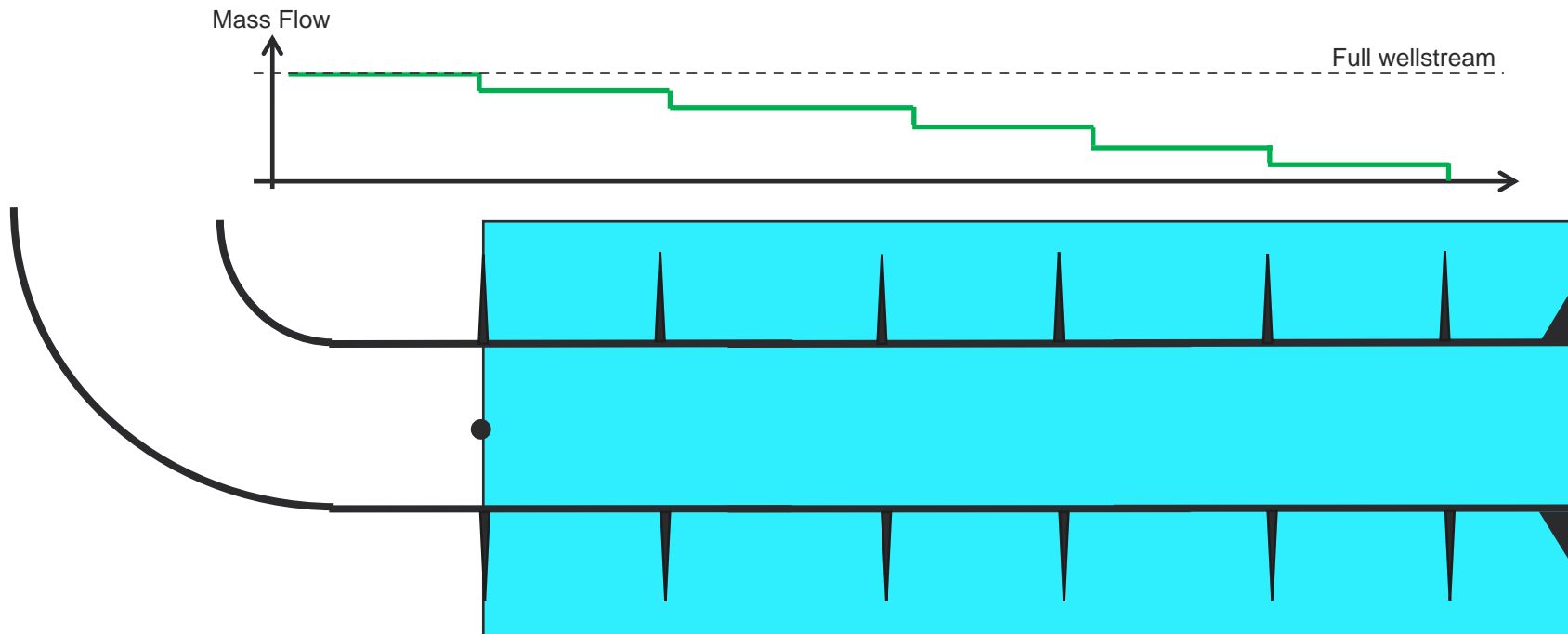
Bottomhole Pressure—What?

- The bottomhole pressure (BHP | p_{wf}) is defined in **whitson**⁺ as the well pressure at the top of the perforated interval (top perforation).



Bottomhole Pressure—What?

- The reference point for BHP is set at the *deepest point* in the well where the *full mass flow* of the well stream can be found.
- Moving the point for BHP to any other point in the perforated interval (lateral part in tight unconventionals) will require the use of an IPR to model the change in mass flow as you move from heel to toe.



Bottomhole Pressure—What?

- The reference point can be set by the user to anywhere along the well if it is set shallower than the deepest MD in the deviation survey
 - If “Top Perforation MD” is set at well heel, then the full well stream is modeled along the lateral.

Depth at which
BHP is calculated

Deepest point
in the well

Well Data

1 Well Deviation Survey 2 Well Data

Perforated Interval

Top Perforation MD 7958 ft Bottom Perforation MD 15439 ft

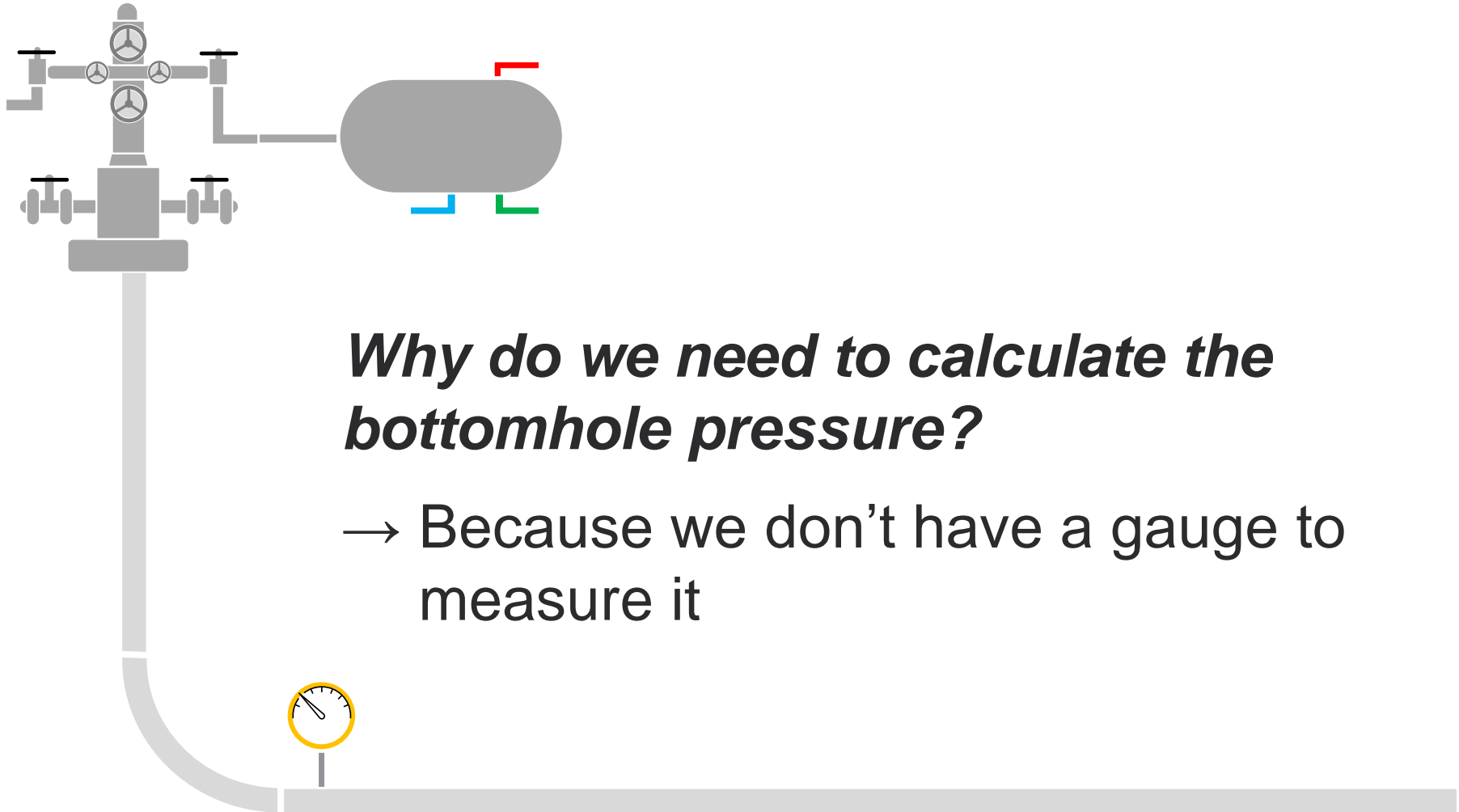
Deviation Survey
(Input entire survey, table expands with input)

Measured Depth (MD) (ft)	True Vertical Depth (TVD) (ft)
14743	7857.61
14833	7859.52
14923	7862.76
15012	7866.57
15101	7869.92
15191	7873.86
15281	7878.36
15370	7883.62
15431	7887.34
15493	7890.81

SAVE

Why Calculate BHP?

BHP Calculations—Why?



Why do we need to calculate the bottomhole pressure?

→ Because we don't have a gauge to measure it

BHP Calculations—Why?

- The BHP is a required input in many production data analyses.
 - DCA (p_{wf} should be constant)
 - Flowing Material Balance (FMB)
 - Analytical Rate-Transient Analysis (ARTA)
 - Numerical Rate-Transient Analysis (NRTA)
 - Numerical Model
 - Nodal Analysis
 - Production Data Diagnostics

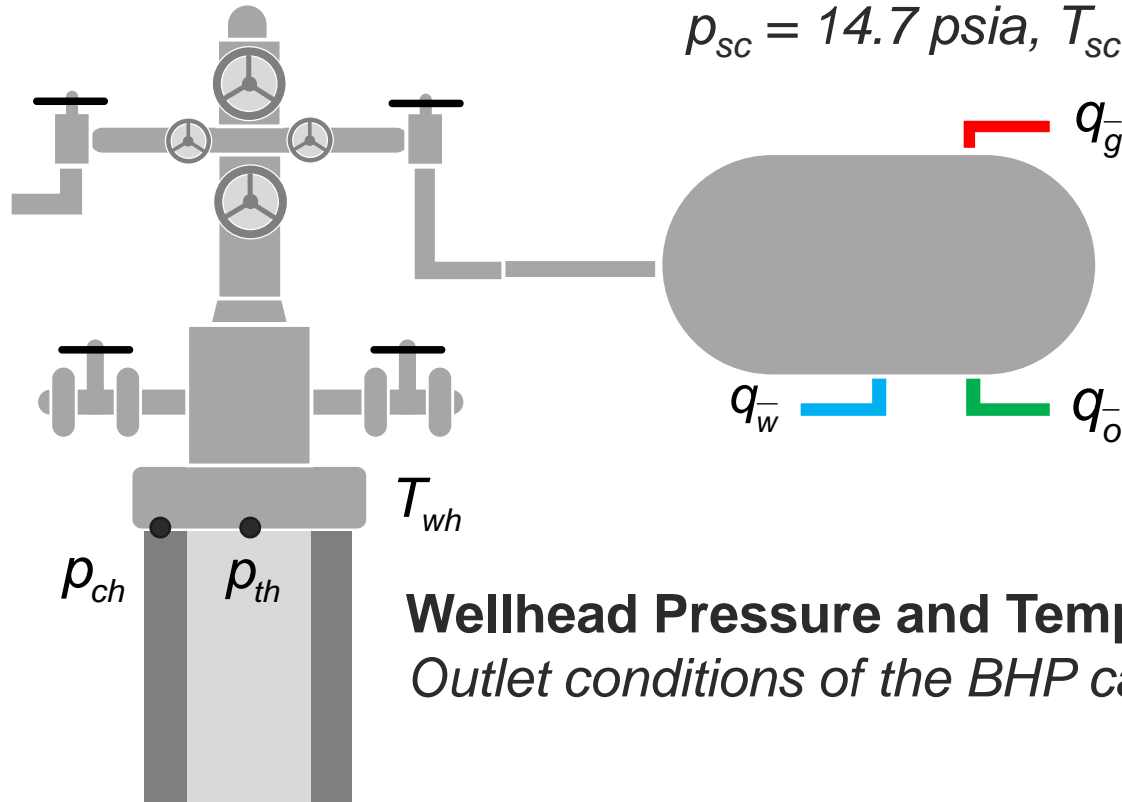
Input to BHP Calculation

Required Input—Production Data

Surface Rates

Produced volumes that are processed and measured at standard conditions

$$p_{sc} = 14.7 \text{ psia}, T_{sc} = 60^\circ\text{F}$$



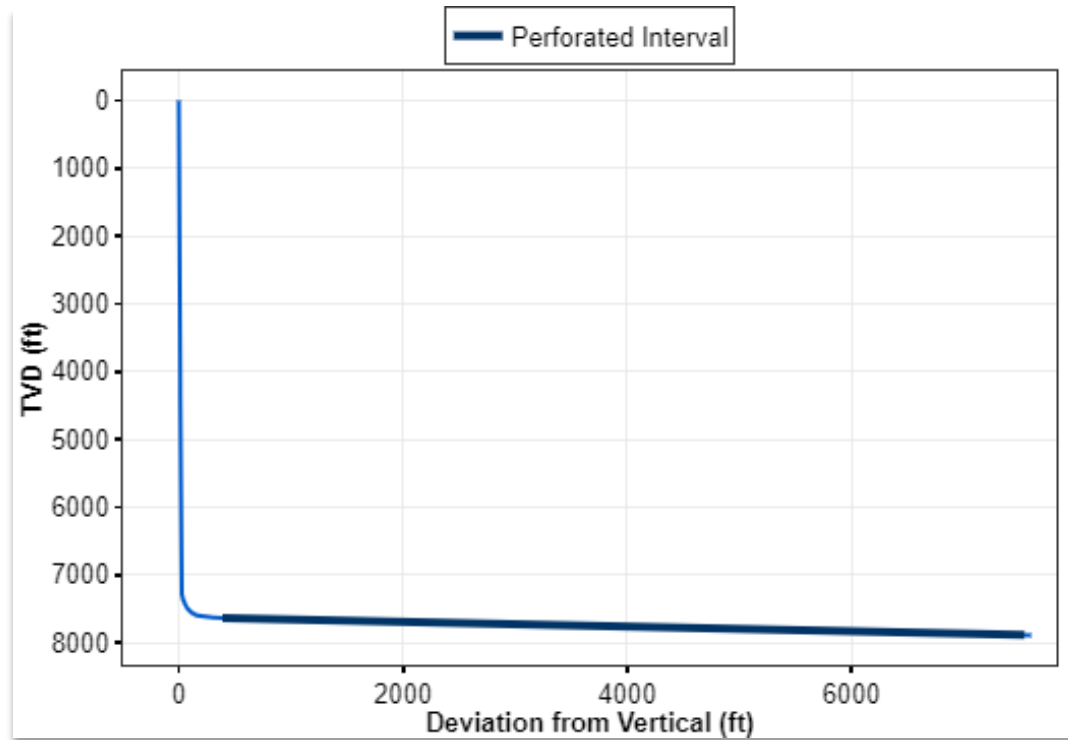
Wellhead Pressure and Temperature

Outlet conditions of the BHP calculations

Required Input—Well Data

Wellbore trajectory—Deviation Survey

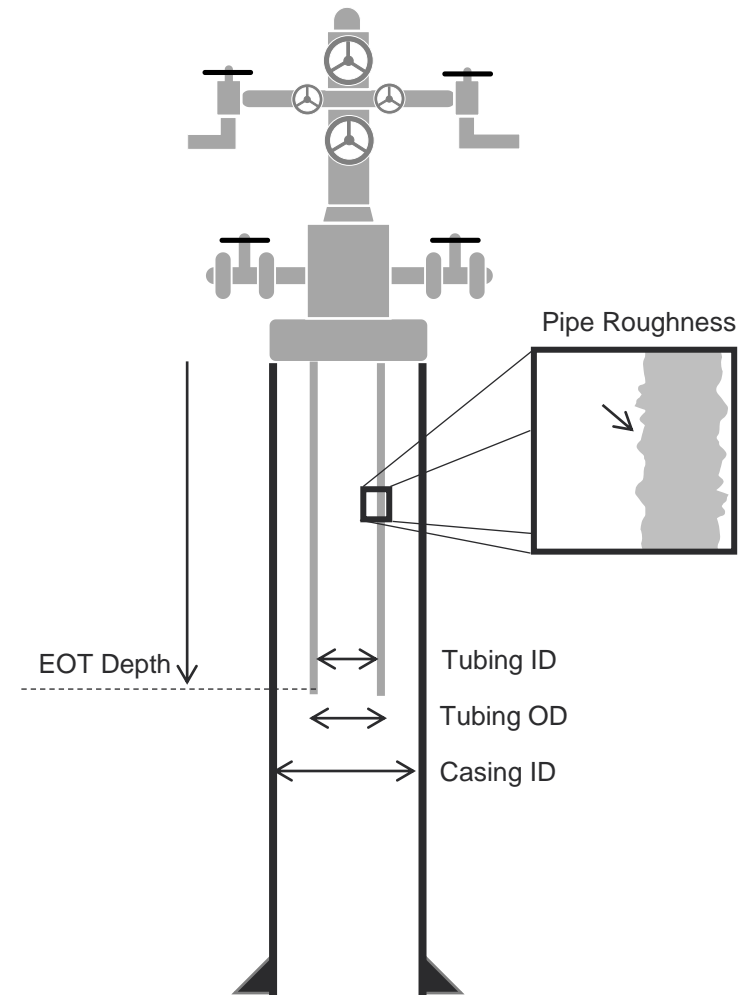
- MD vs TVD
- Top and Bottom Perforation Depth (Perforated Interval)



Required Input—Well Data

Well completion—Casing and Tubing Data

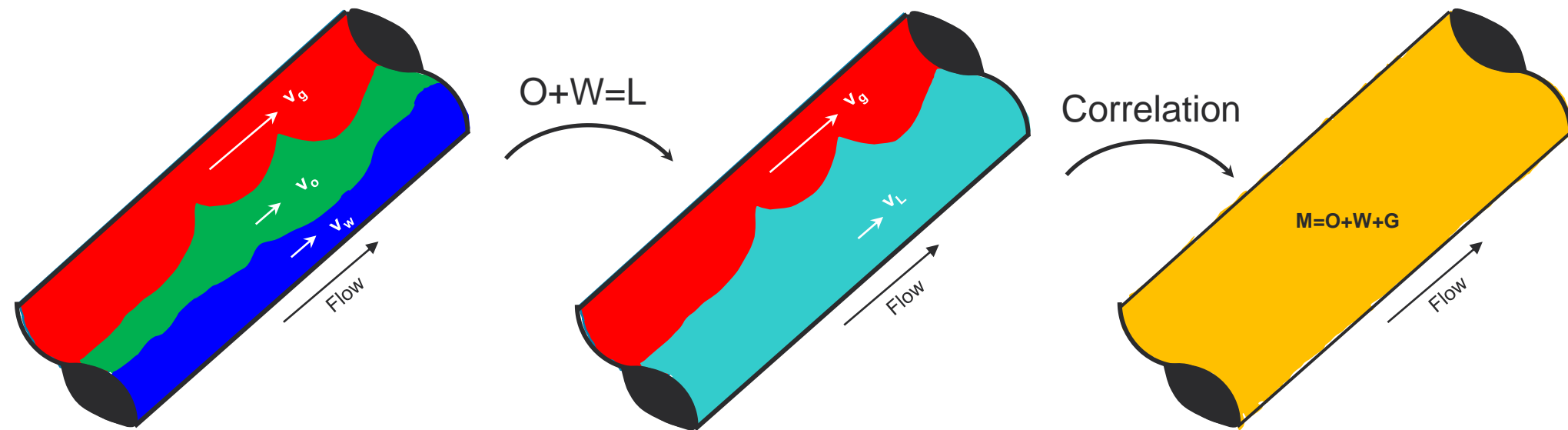
- Inner Diameter (ID)
- Outer Diameter (OD)
- Pipe roughness
- EOT depth



BHP Correlations

BHP Calculations

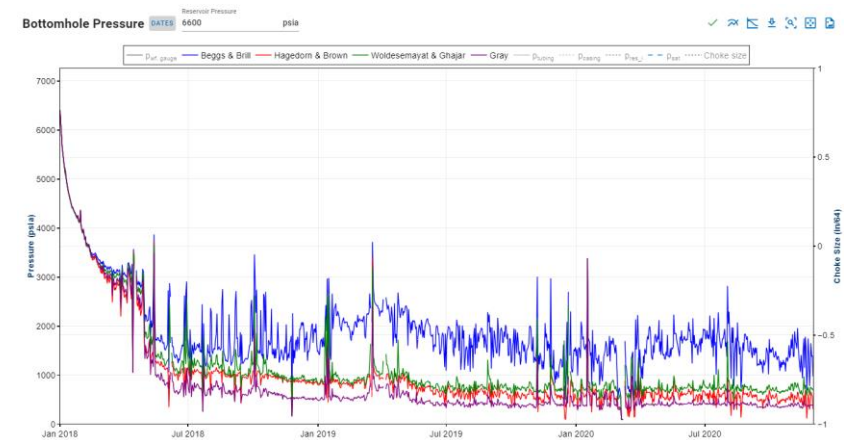
- BHP calculations rely on using single-phase flow equations to model multiphase flow.
- Oil and water are lumped together into a liquid phase.
- Liquid and gas are averaged into a single-phase mixture.
 - *Averaging is correlation dependent*



BHP Correlations

whitson+ supported correlations^[1] are

- Hagedorn and Brown (1965)
- Beggs and Brill (1973)
- Gray (1978)
- Woldesemayat and Ghajar (2006)



^[1] These are so-called drift-flux models, which is preferred due to their simplicity. The alternative is to solve the momentum- and energy equations for each phase separately, which is commonly referred to as mechanistic models. More in URTeC: 4045619.

BHP Calculations—Pressure Gradient

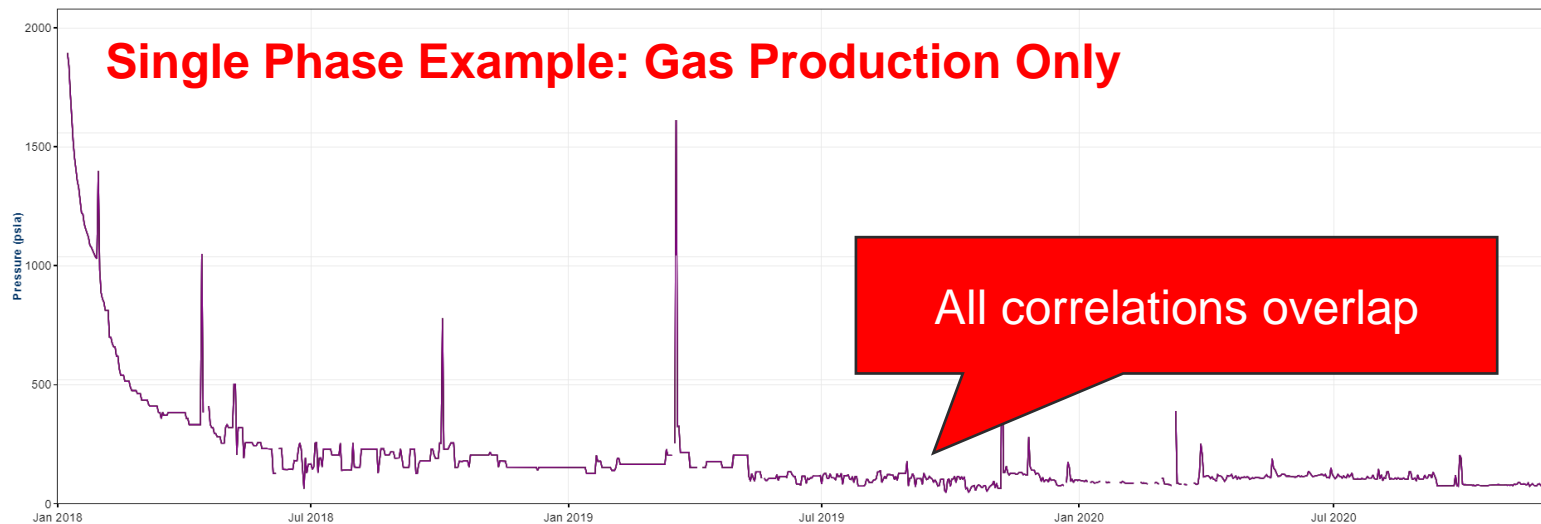
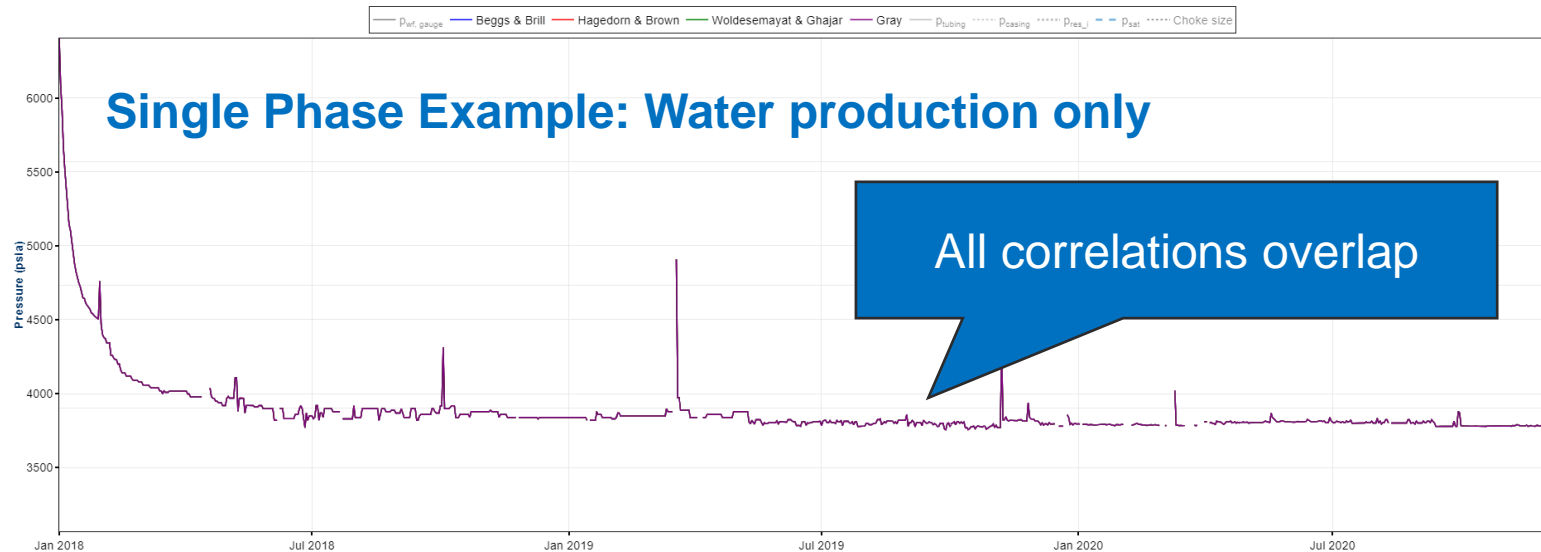
$$-\frac{dp}{ds} = \overbrace{\rho \frac{g}{g_c} \cos(\theta)}^{\text{Gravity}} + \underbrace{\frac{f_D \rho v^2}{2d_h g_c}}_{\text{Friction}} + \overbrace{\frac{\rho v}{g_c} \frac{dv}{ds}}^{\text{Acceleration}}$$

Gravity: Caused by the weight of the fluids. Acts in the direction of gravity.

Friction: Caused by the pipe wall.

Acceleration: Caused by a rapid expansion of the fluids. Only relevant for gaseous wells near the wellhead for low p_{wh} .

Differences between the Correlations



Note to instructor: BHP study URTeC Field

Correlations—The Common Equation

- The pressure-gradient equation is common to all the correlations.
- The difference between the correlations lies in how the correlations calculate the liquid hold-up
 - Affects some of the properties in the pressure gradient

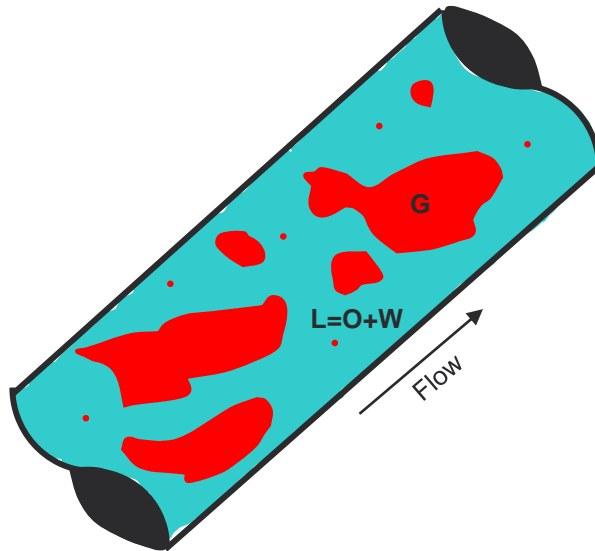
$$-\frac{dp}{ds} = \frac{\rho_g \frac{g}{g_c} \cos(\theta) + \frac{f_{Ds} \rho_f v_m^2}{2d_h g_c}}{1 - \frac{\rho_a v_m v_{sg}}{g_c p}}$$

Diagram illustrating the components of the pressure gradient equation:

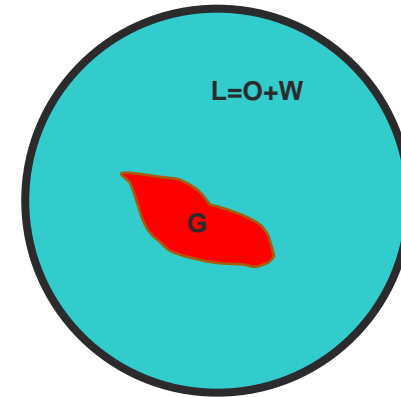
- Gravity Density:** ρ_g
- Multiphase Friction Factor:** f_{Ds}
- Friction Density:** ρ_f
- Acceleration Density:** ρ_a

Multiphase Flow—Liquid Hold-Up

- The liquid hold-up, H_L , represents the part of the pipe cross-sectional area occupied by liquid.



$$H_L = \frac{A_L}{A_g + A_L}$$



**Which BHP Correlation
is the most Accurate?**

Comprehensive BHP Study

Objective: Measured gauge pressure vs correlations

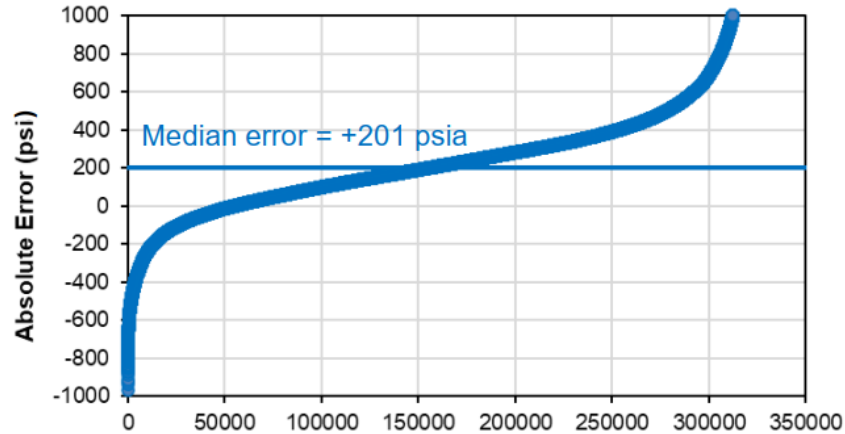
Wells: 420 wells

Datapoints: >300,000

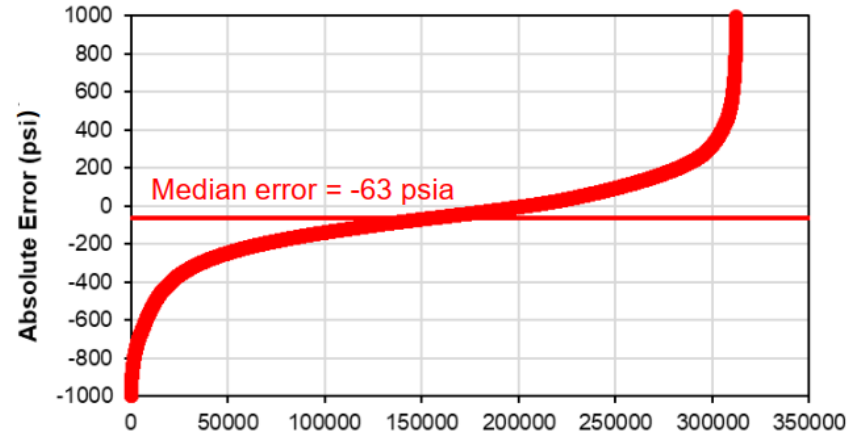
Basins: Delaware, Midland, DJ, Powder River, Anadarko and Utica

Absolute Error Distribution

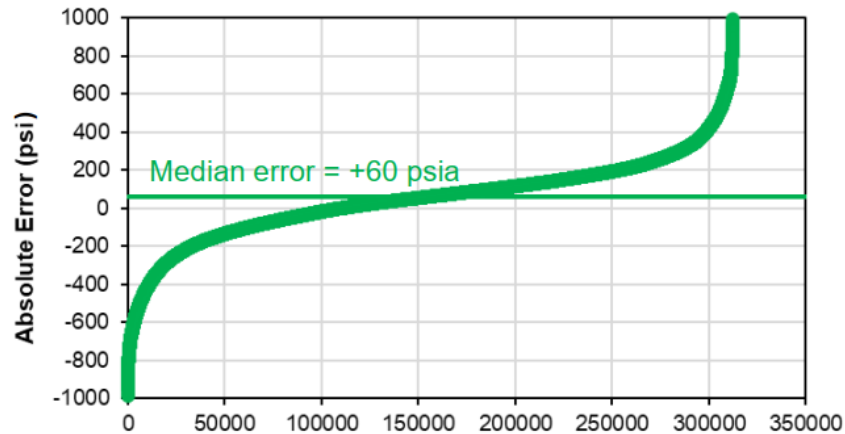
Beggs & Brill



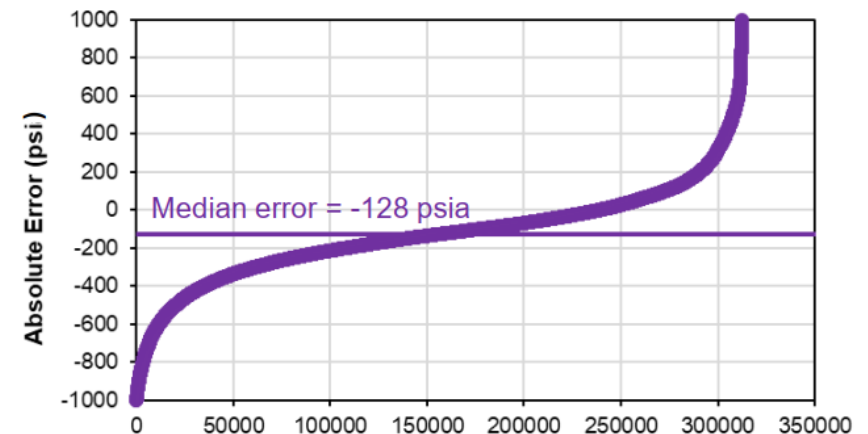
Hagedorn & Brown



Woldesemayat & Ghajar



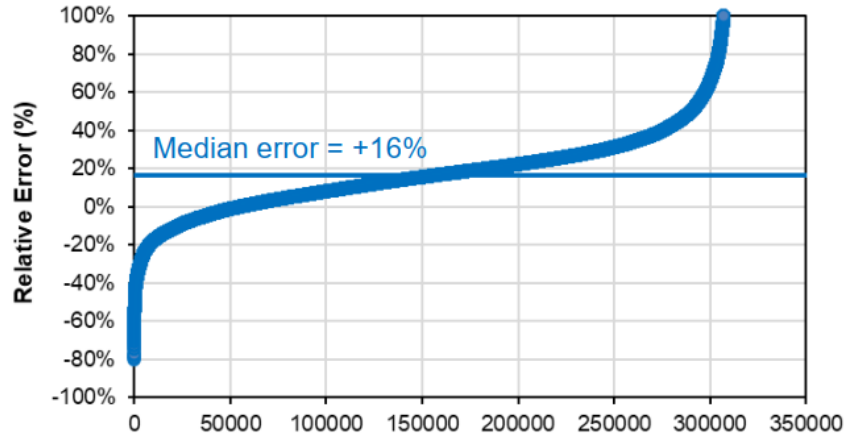
Gray



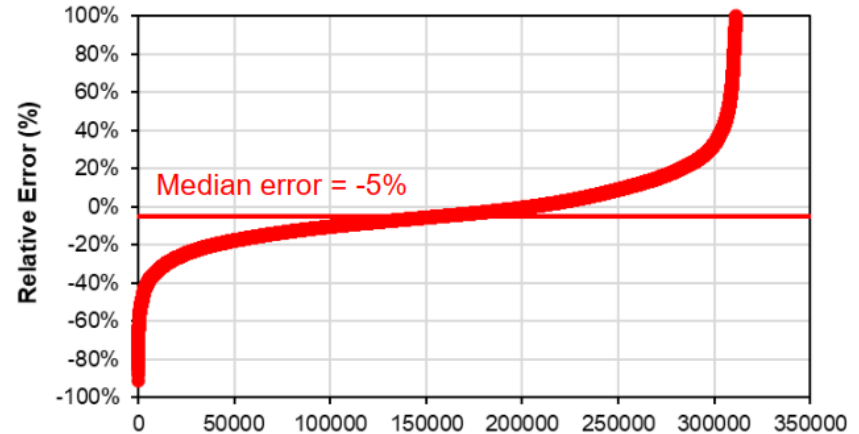
Source: URTeC 4045619

Relative Error Distribution

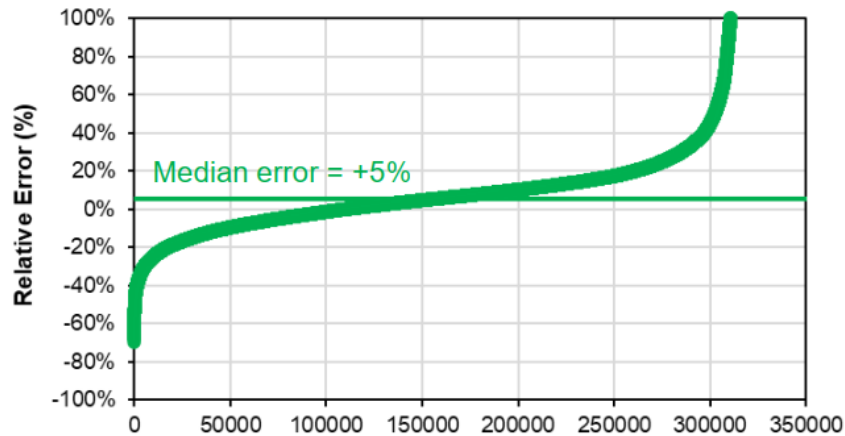
Beggs & Brill



Hagedorn & Brown



Woldesemayat & Ghajar

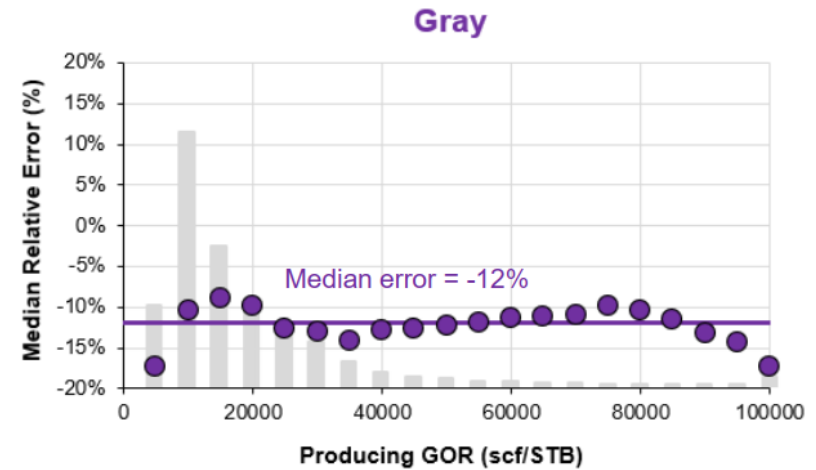
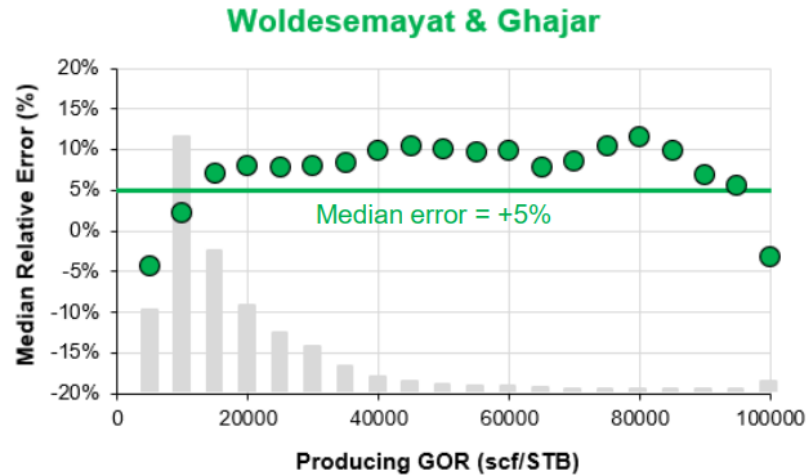
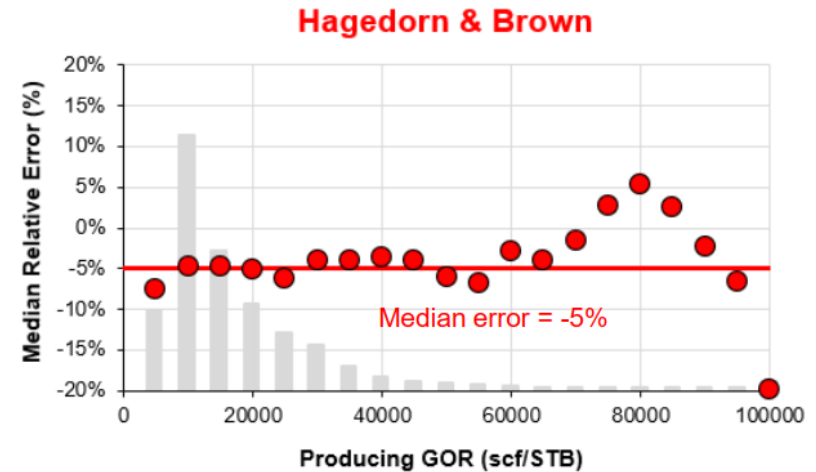
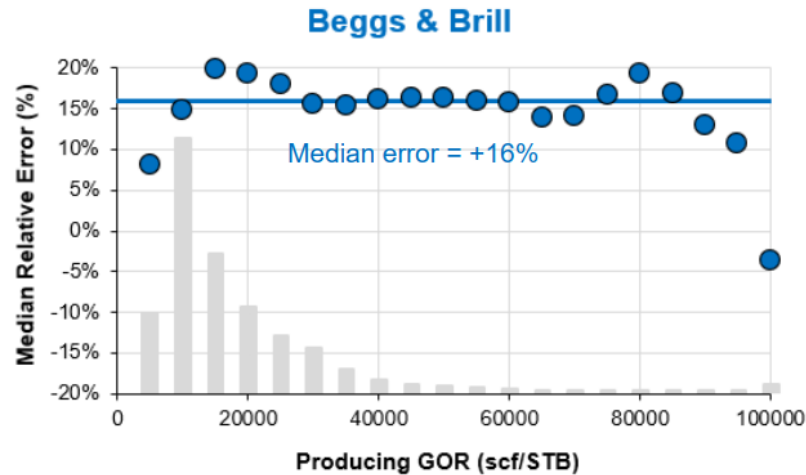


Gray



Source: URTeC 4045619

Producing GOR vs Relative Error



Source: URTeC 4045619

Summary

Recommendation 1: Compare BHP calcs to gauge data when available. Use most accurate correlation for wells in the same basin.

Recommendation 2: if no gauge data is available, use Woldesemayat & Ghajar.

Further work: Goal is to expand on this study over the next year (include more wells).

Flow Paths

Flow Paths—Overview

- Several flow paths may be selected in **whitson+**
 - Casing
 - Tubing
 - Annulus
 - Tubing and Annulus
 - Measured BHP
 - Unknown

The screenshot displays the 'Well Data' interface in Whitson+. It features a sidebar with 'Configuration 1' and a main panel for 'Wellbore Configuration 1 (Initial)'. The main panel contains two tables: 'Casing Data' and 'Tubing Data'. Below these tables are dropdown menus for 'Flowpath' and 'Artificial Lift Method'. The 'Flowpath' dropdown is currently set to 'Tubing' and is open, showing options: Casing, Tubing, Annulus, Tubing and Annulus, Measured Gauge Pressures, and Unknown. The 'Artificial Lift Method' is set to 'None'. There is also a toggle for 'Calculate from gauge to sandface using measured pressures' and a 'SAVE' button.

Well Data

1 Well Deviation Survey 2 Well Data

Configuration 1
Flowpath: Tubing
Artificial Lift: None

1 Wellbore Configuration 1 (Initial)

Casing Data

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)
1	0	15493	4.778	0.0006

Tubing Data

Pipe No. (#)	Bottom MD (ft)	ID (in)	OD (in)	Roughness (in)
1	7000	2.441	2.875	0.0006

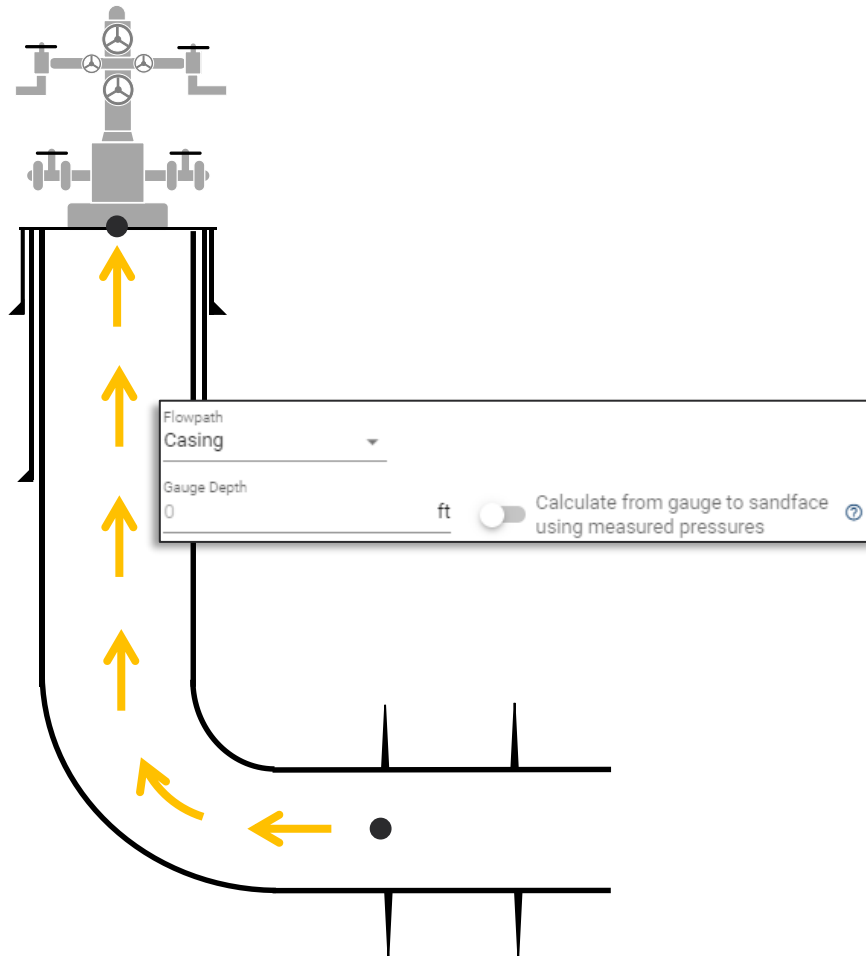
Flowpath: Tubing Artificial Lift Method: None

Calculate from gauge to sandface using measured pressures

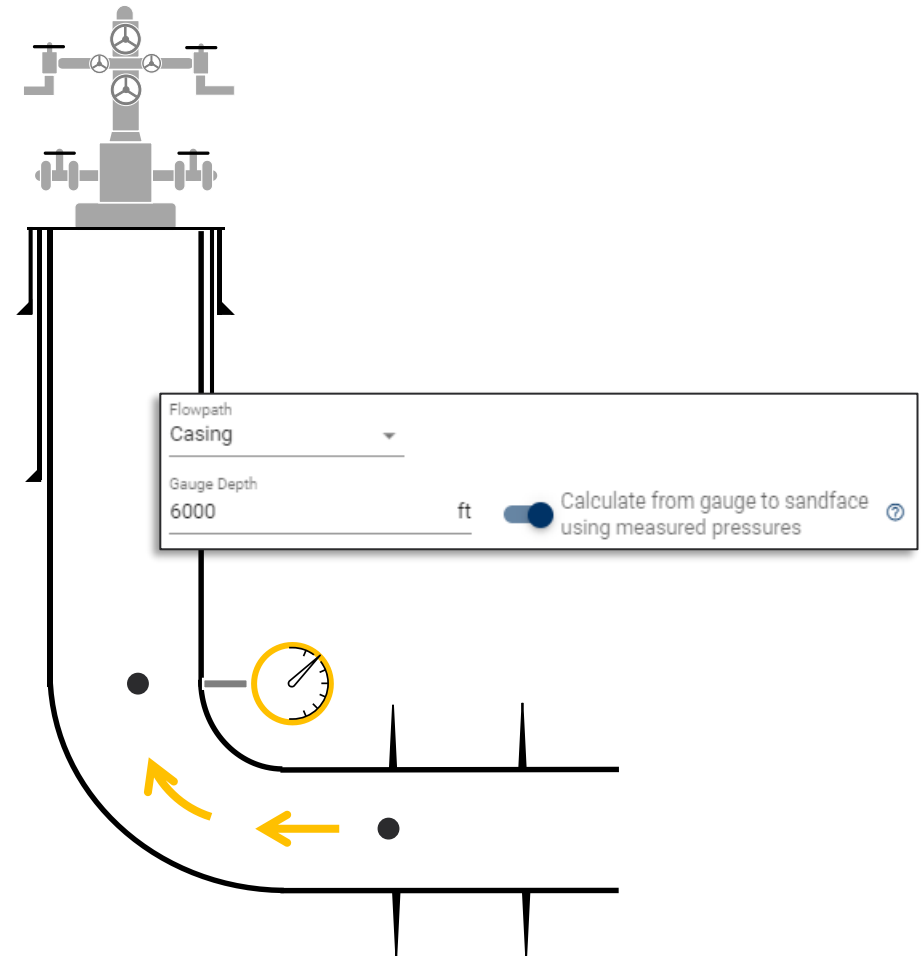
SAVE

Flow Paths—Casing

From wellhead to top perf.

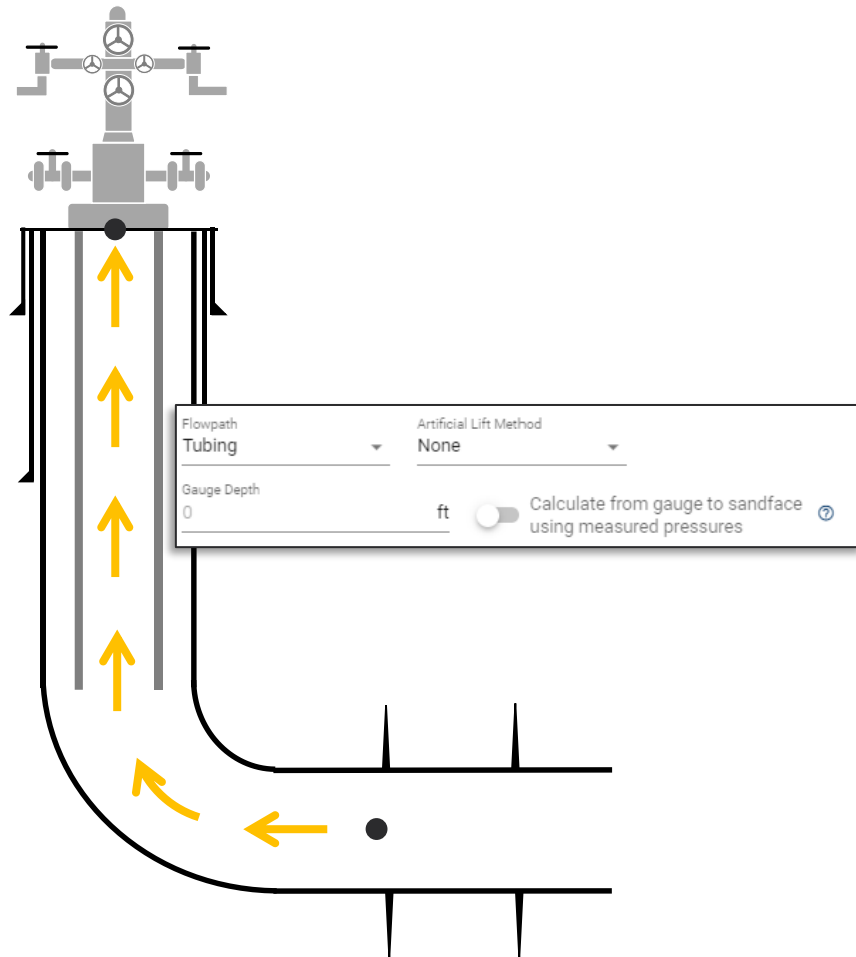


From gauge to top perf.

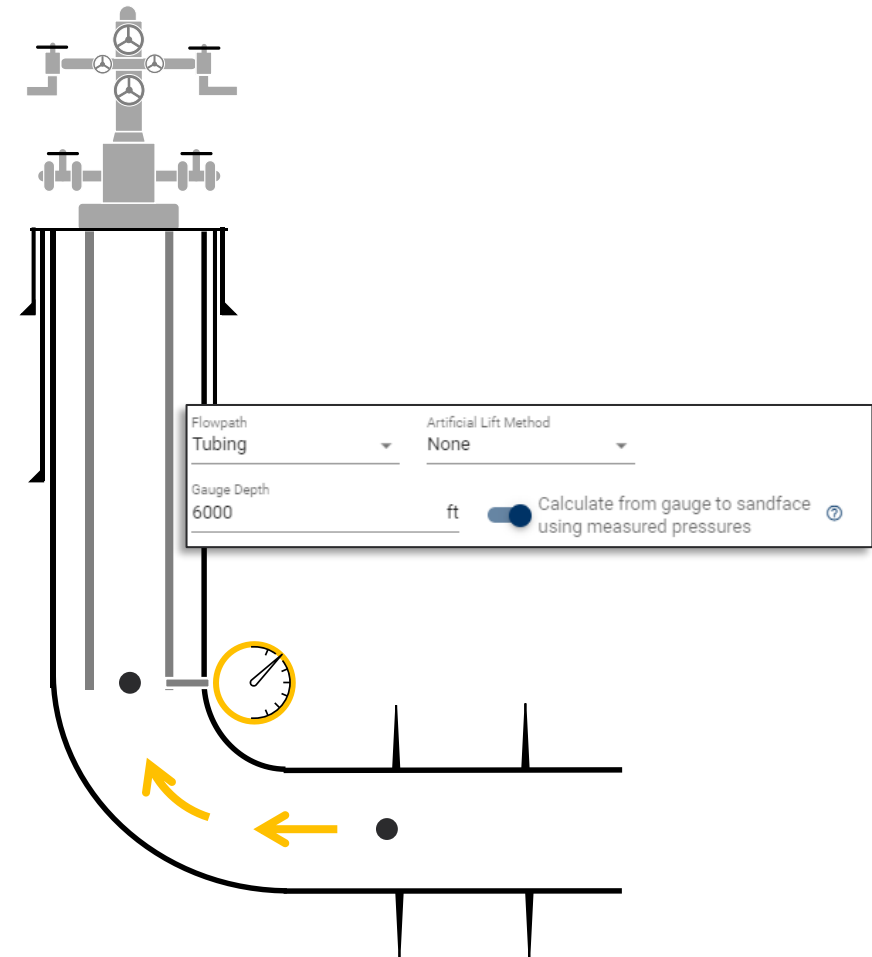


Flow Paths—Tubing

From wellhead to top perf.

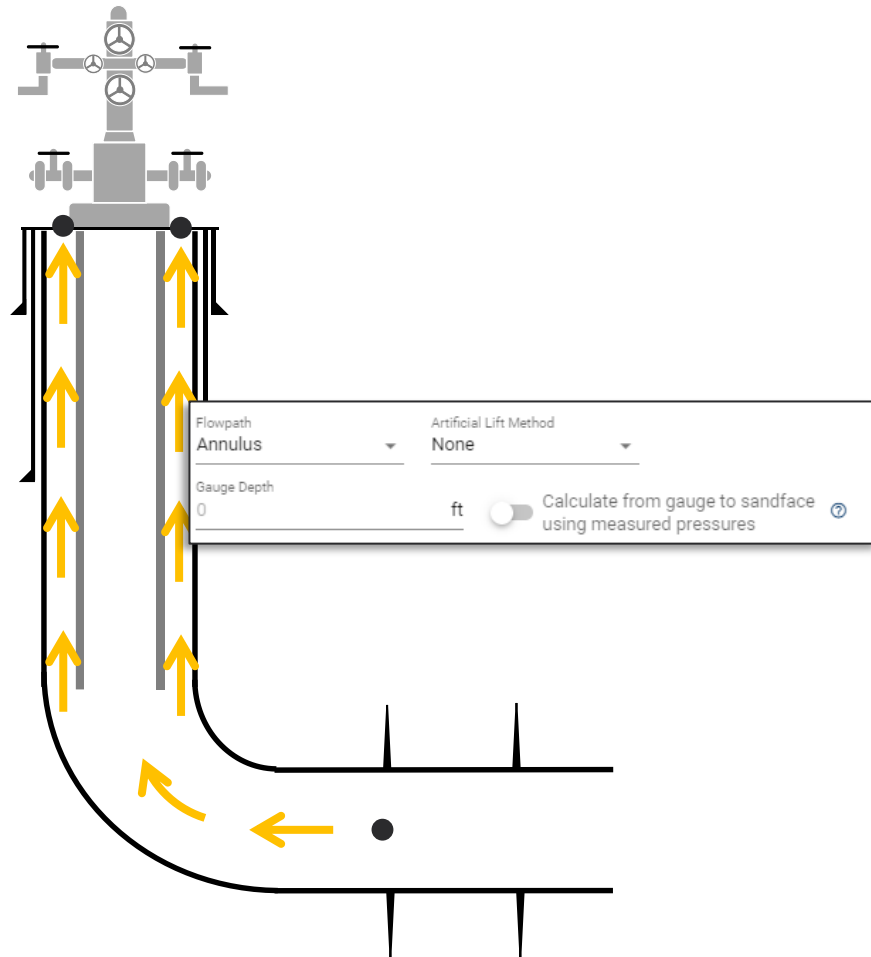


From gauge to top perf.

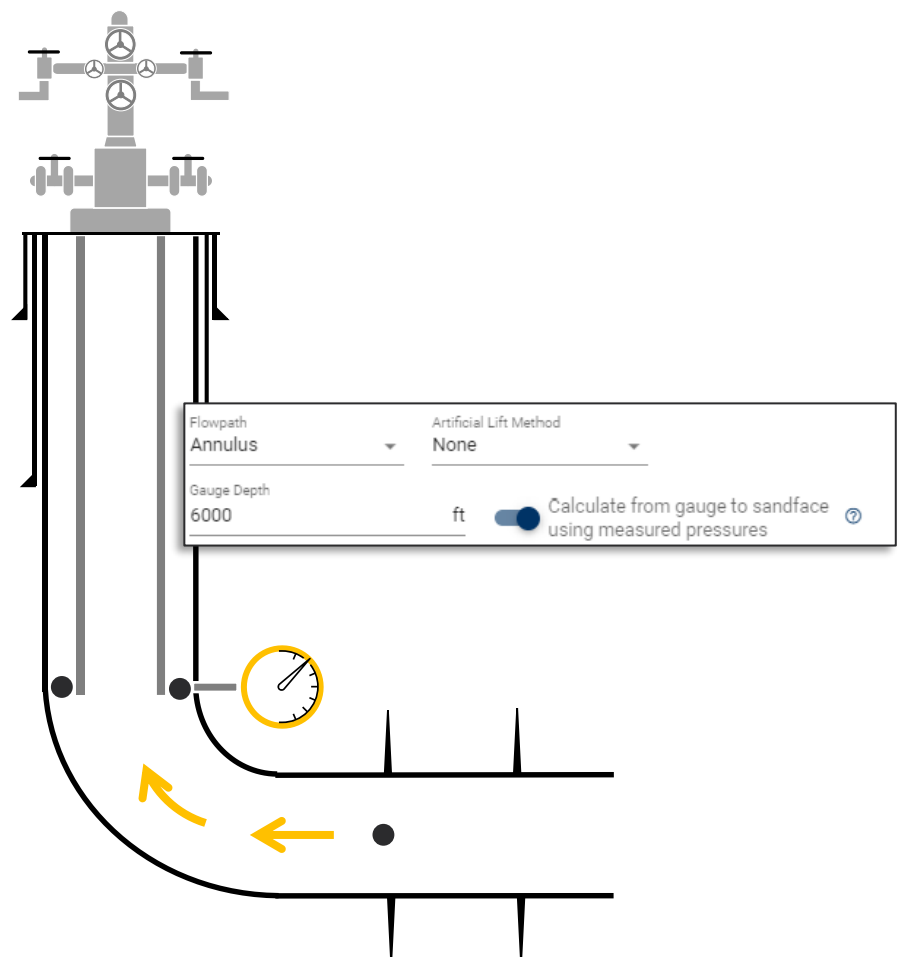


Flow Paths—Annulus

From wellhead to top perf.

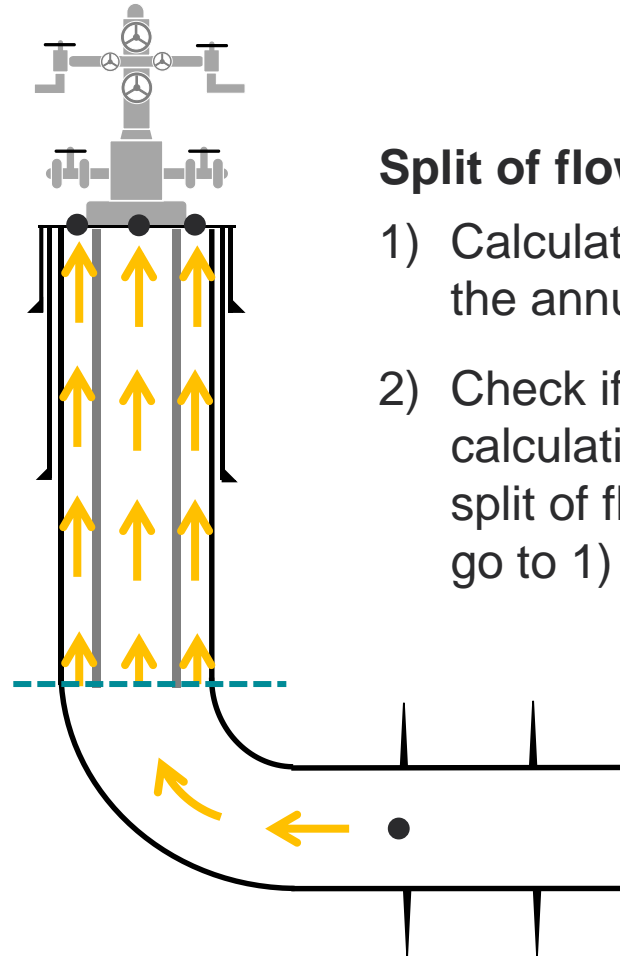


From gauge to top perf.



Flow Path—Tubing and Annulus (Parallel)

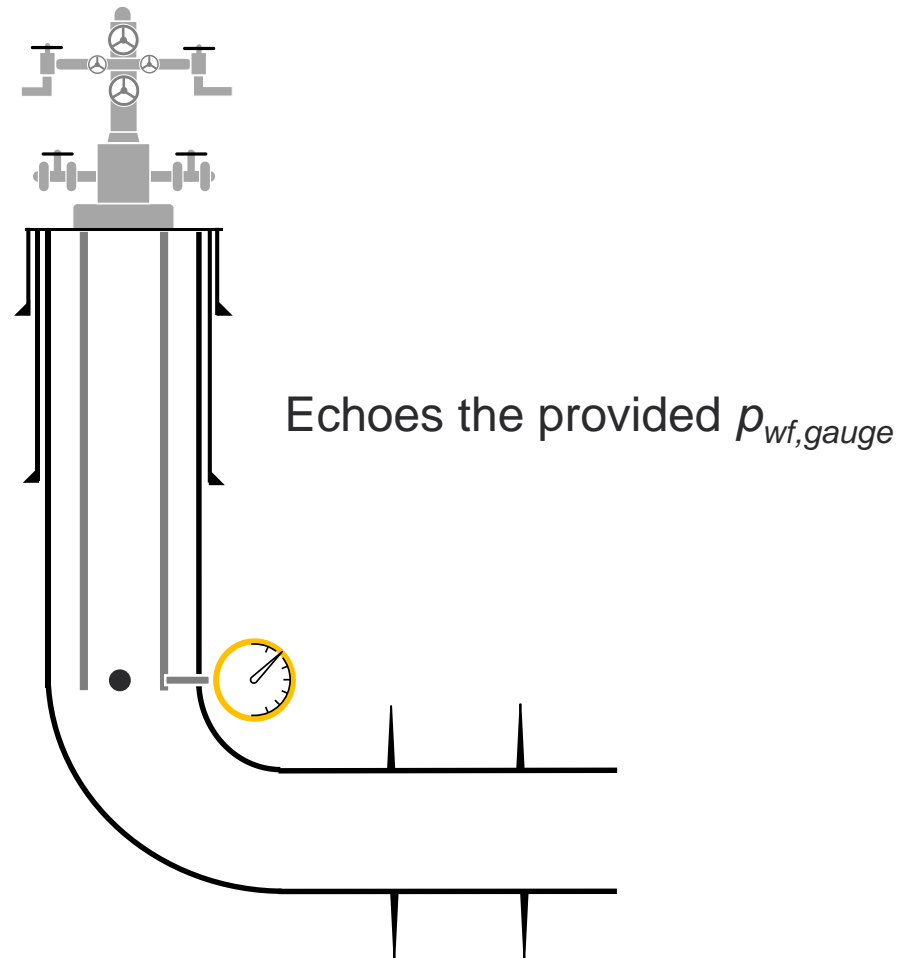
From wellhead to top perf.



Split of flow is calculated at EOT

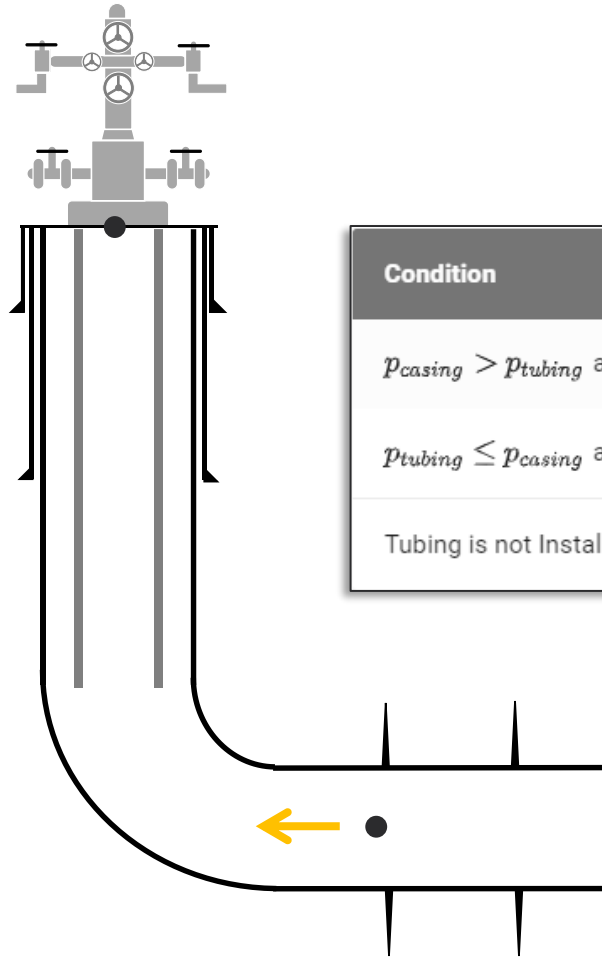
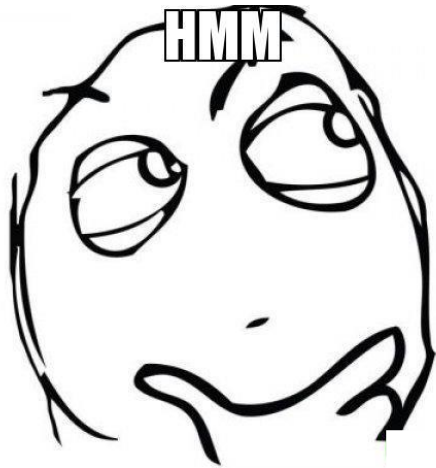
- 1) Calculate the pressure profile down the annulus and tubing
- 2) Check if pressure at EOT from each calculation is equal for a specified split of flow. If not, change split, and go to 1)

Flow Paths—Measured BHP



Flow Path—Unknown

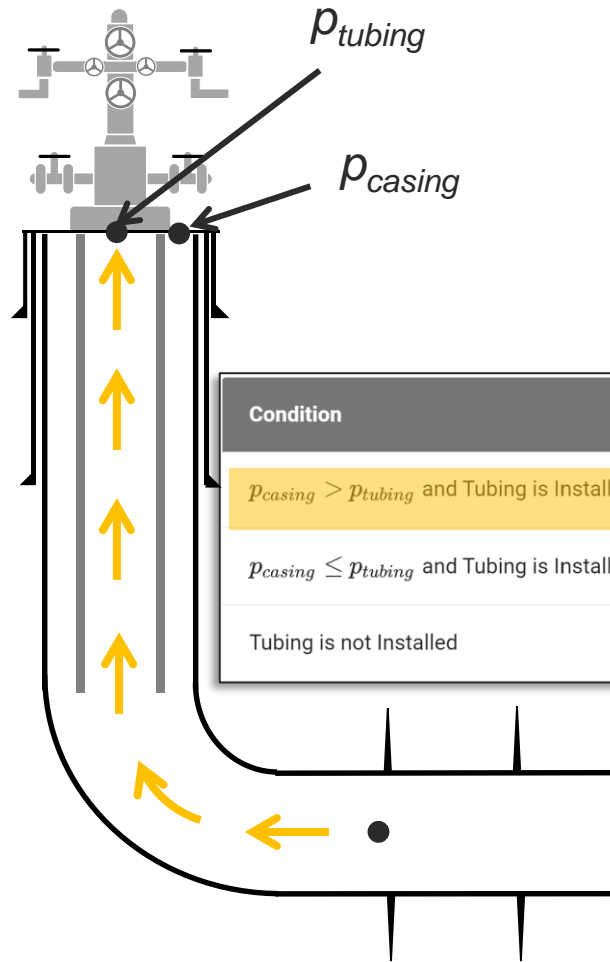
From wellhead to top perf.



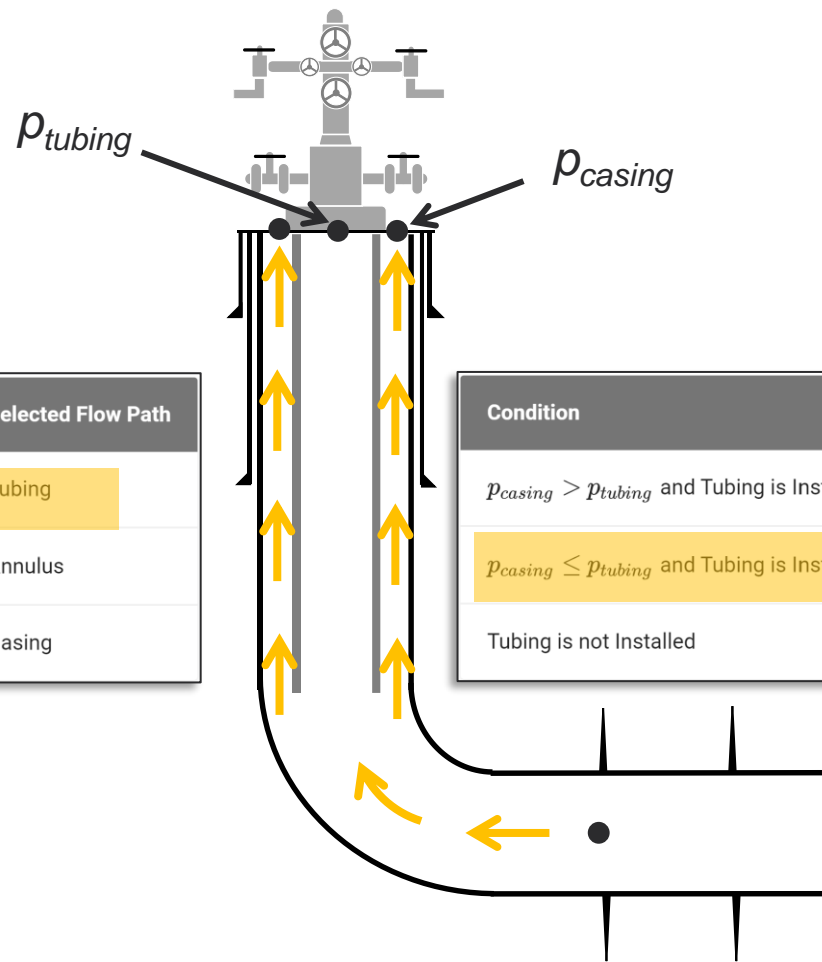
Condition	Selected Flow Path
$p_{casing} > p_{tubing}$ and Tubing is Installed	Tubing
$p_{tubing} \leq p_{casing}$ and Tubing is Installed	Annulus
Tubing is not Installed	Casing

Flow Path—Unknown

Tubing Installed



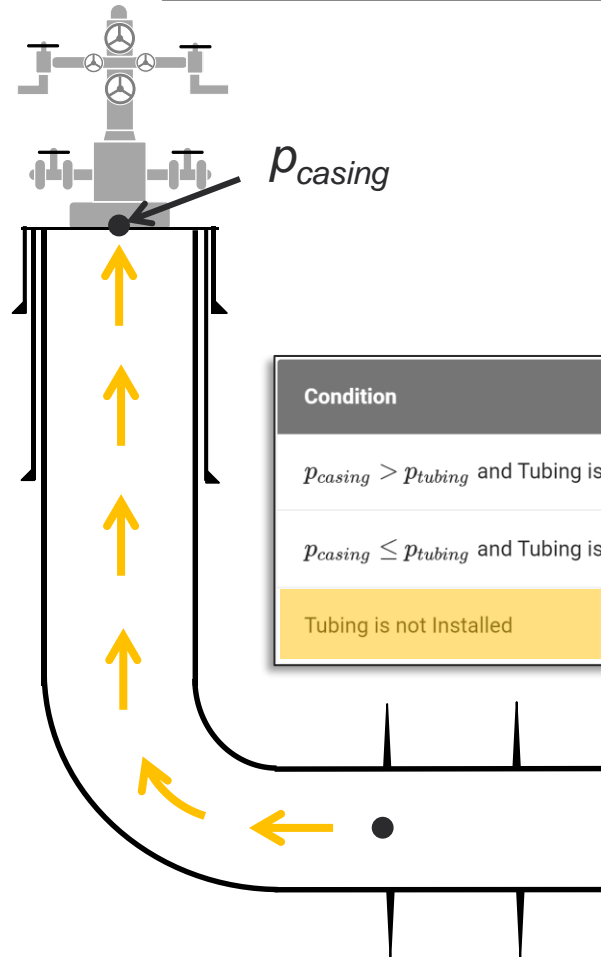
Condition	Selected Flow Path
$p_{casing} > p_{tubing}$ and Tubing is Installed	Tubing
$p_{casing} \leq p_{tubing}$ and Tubing is Installed	Annulus
Tubing is not Installed	Casing



Condition	Selected Flow Path
$p_{casing} > p_{tubing}$ and Tubing is Installed	Tubing
$p_{casing} \leq p_{tubing}$ and Tubing is Installed	Annulus
Tubing is not Installed	Casing

Flow Path—Unknown

No Tubing Installed



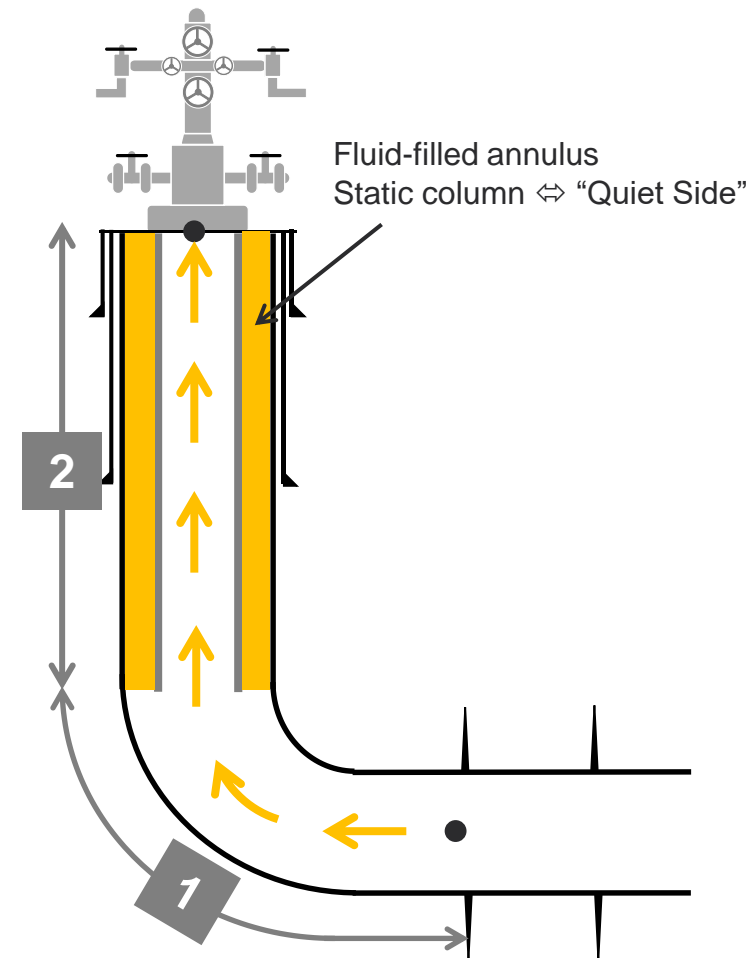
Condition	Selected Flow Path
$p_{casing} > p_{tubing}$ and Tubing is Installed	Tubing
$p_{casing} \leq p_{tubing}$ and Tubing is Installed	Annulus
Tubing is not Installed	Casing

Flowing vs Quiet Side Calculations

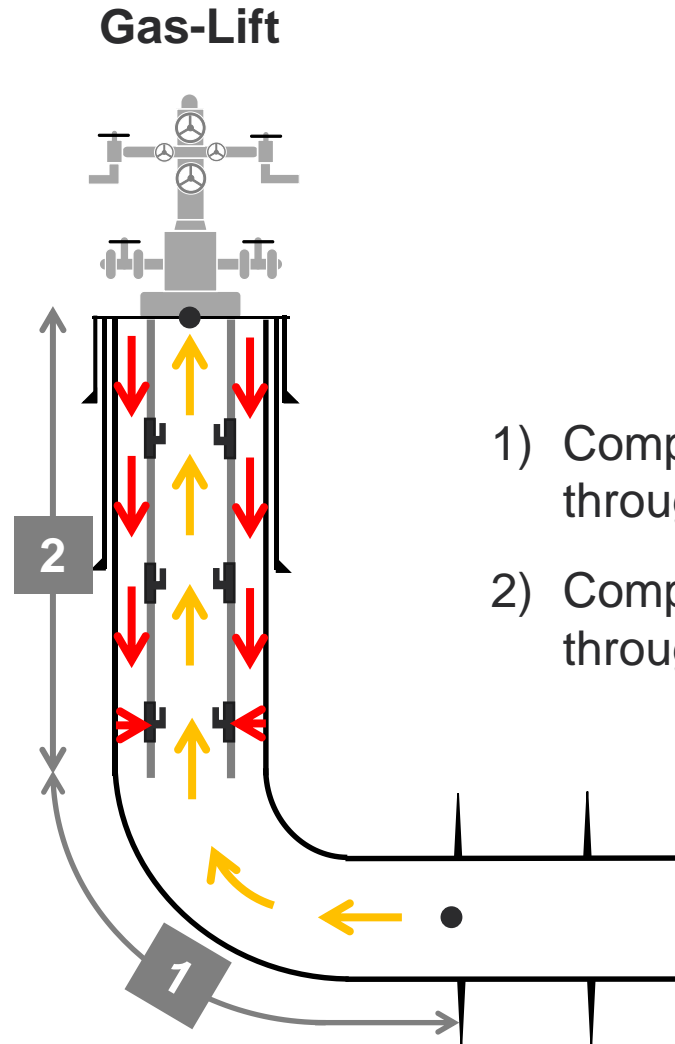
BHP Calculations Using the “Quiet Side”

Quiet Side:

- Annulus assumed filled with a single-phase fluid with communication to the flowing side at end of tubing (EOT), i.e. no isolation packer.
- Compute BHP by splitting the well into two segments
 1. Multiphase flow from top perforation (TP) to EOT
 2. Static fluid column from EOT to WH



BHP Calculations Using the “Quiet Side”



- 1) Compute the well pressure from TP to valve through the *multiphase* wellstream
- 2) Compute the well pressure from valve to WH through the *single-phase* lift-gas column

Artificial Lift Methods

Artificial Lift Methods

Well Data

1 Well Deviation Survey

2 Well Data

Configuration 1

Flowpath: Tubing

Artificial Lift: Gas Lift

1 Wellbore Configuration 1 (Initial)

Casing Data

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)
1	0	20184	4.67	0.0006

Tubing Data

Pipe No. (#)	Bottom MD (ft)	ID (in)	OD (in)	Roughness (in)
1	13128	1.995	2.375	0.0006

Flowpath
Tubing

Compute Through
Flowing Side

Gauge Depth (MD)
0

Artificial Lift Method
Gas Lift

Gas Lift Configuration
Poor-Boy

from gauge to sandface
measured pressures

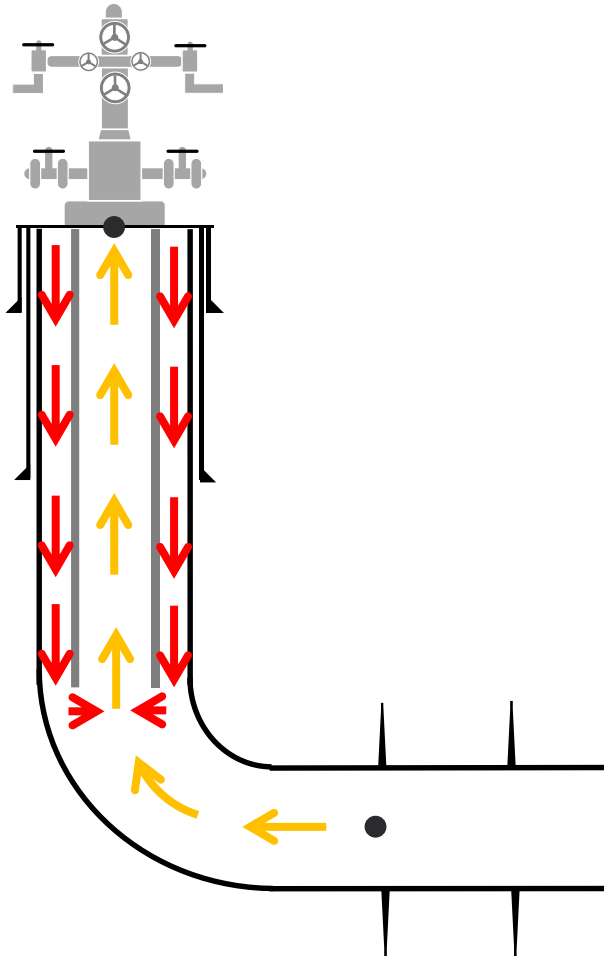
SAVE

Artificial Lift—Gas Lift

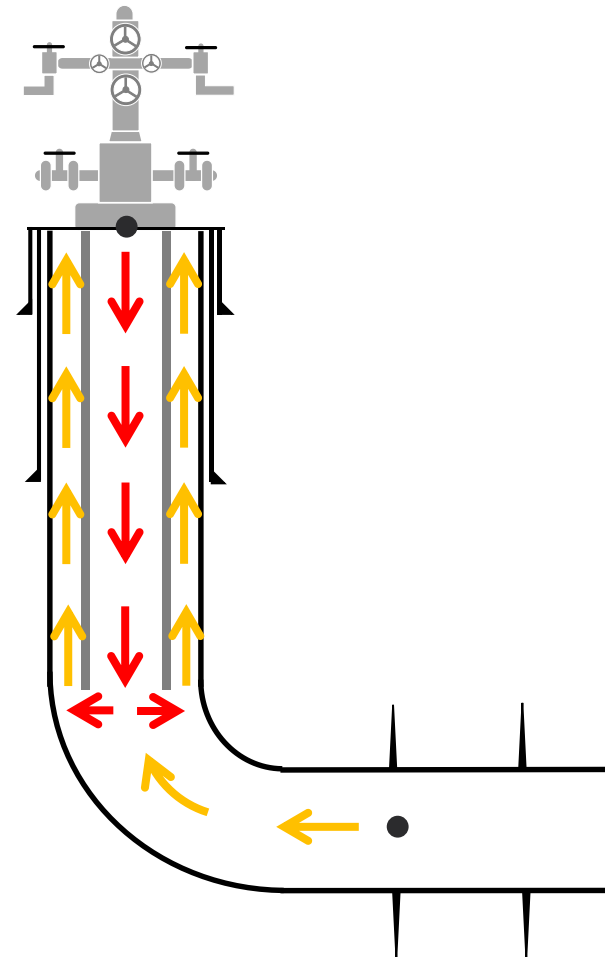
- Three types of gas-lift configurations:
 - Poor-Boy—Injection at EOT
 - Valves—Injection through the first open valve based on the surface pressure
 - Automatic—Injection at equal-pressure point in the tubing and annulus

Artificial Lift—Gas Lift | Poor-Boy

Flow Path: Tubing

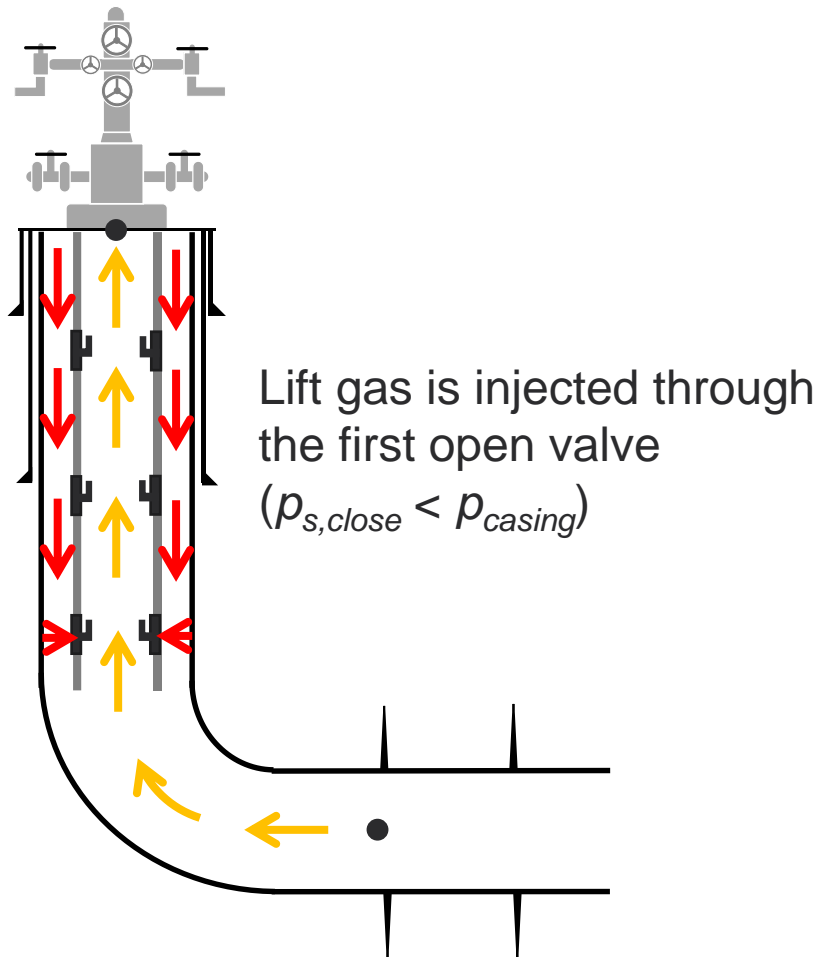


Flow Path: Annulus (*Reversed gas lift*)

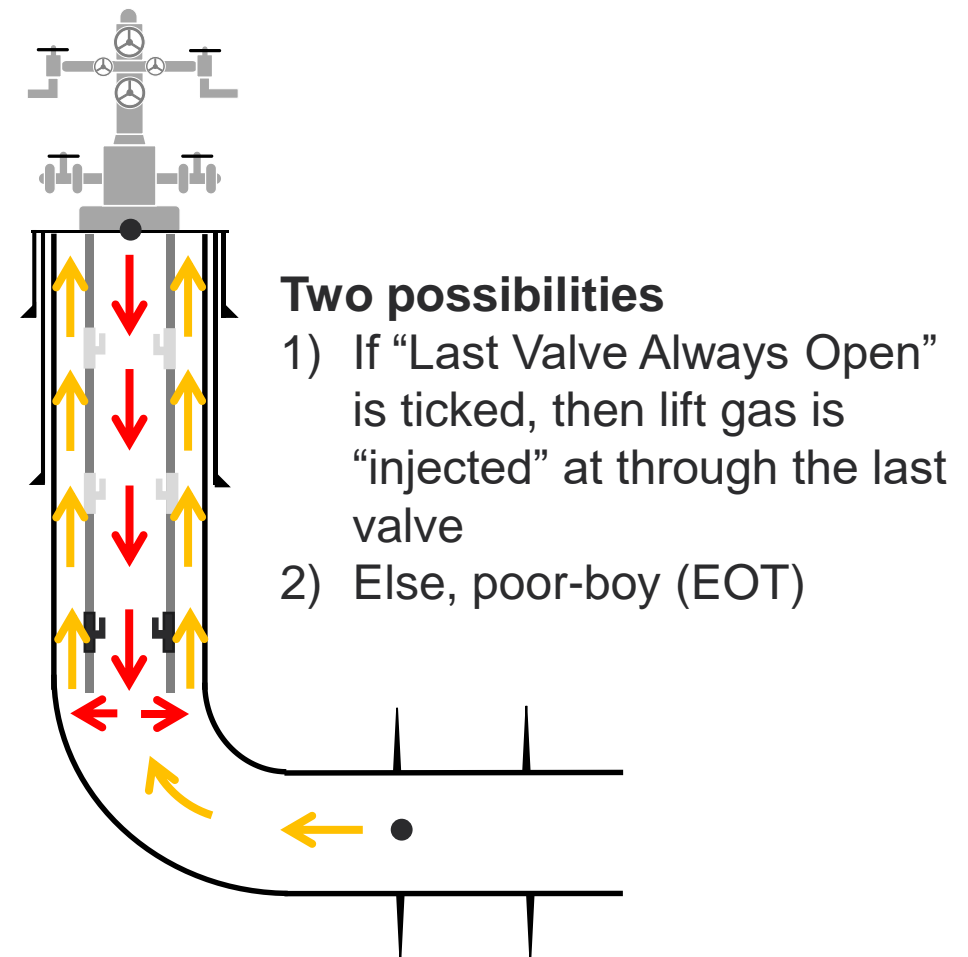


Artificial Lift—Gas Lift | Valves

Flow Path: Tubing

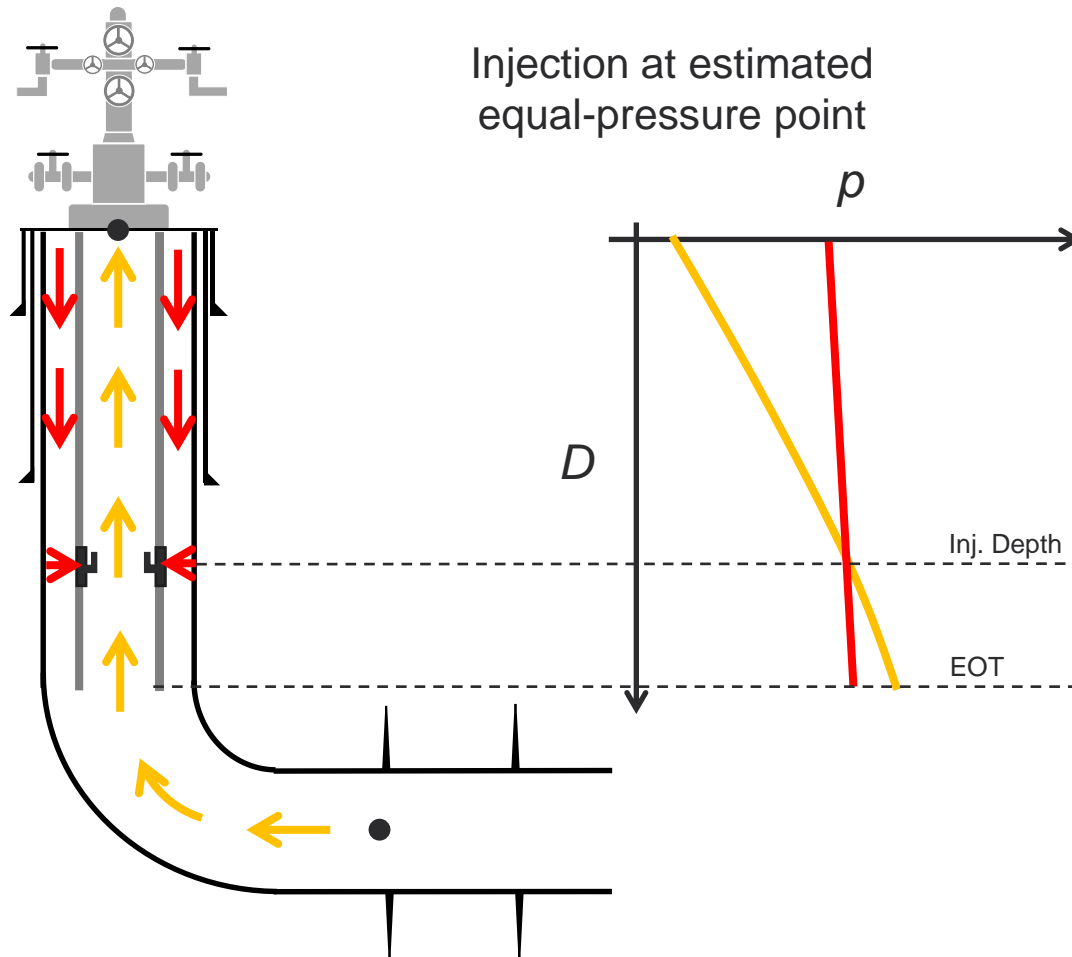


Flow Path: Annulus (*Reversed gas lift*)

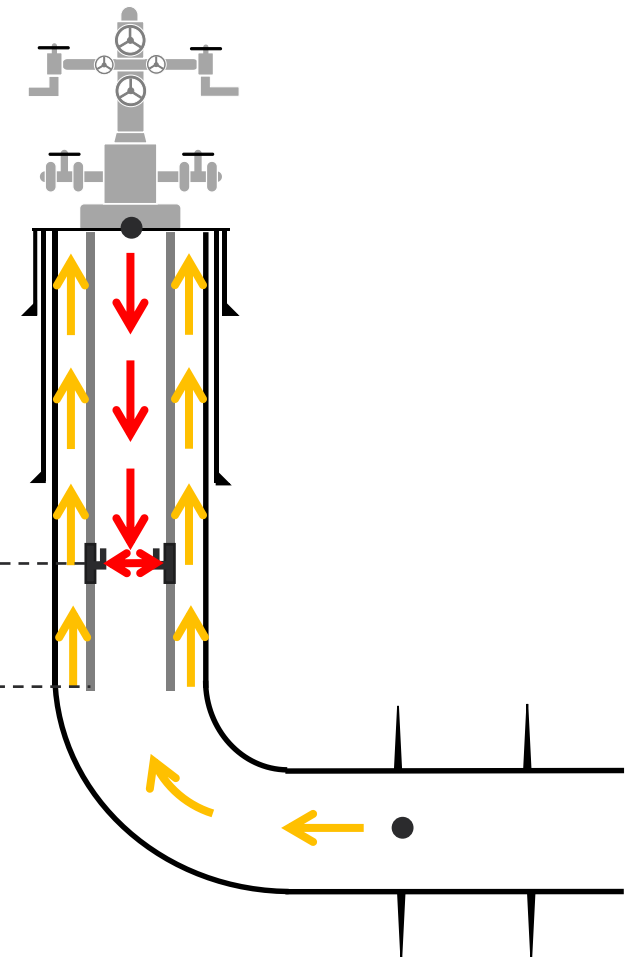


Artificial Lift—Gas Lift | Automatic

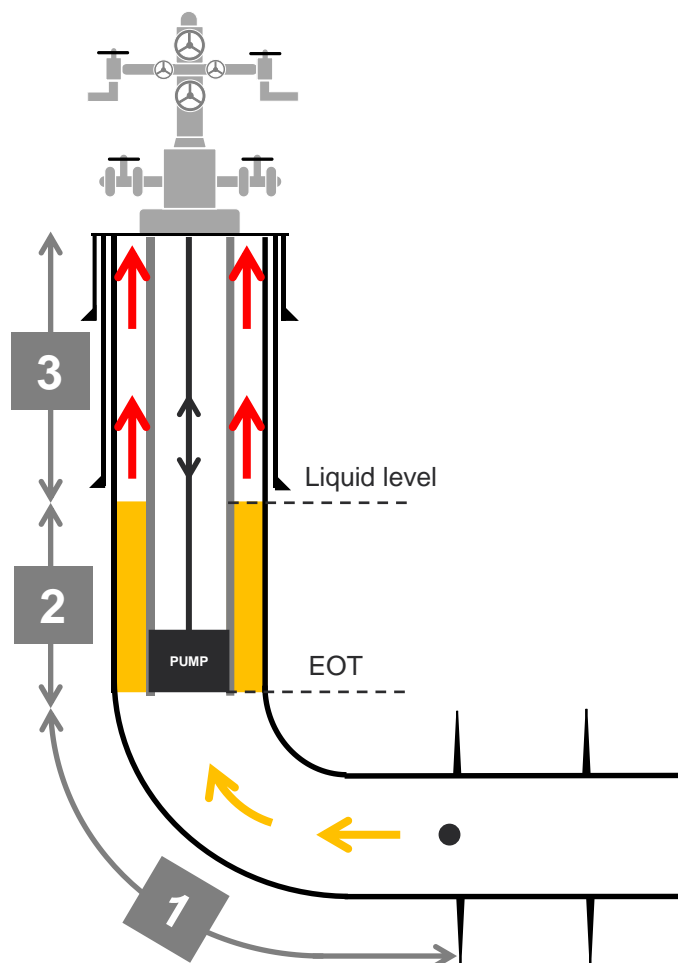
Flow Path: Tubing



Flow Path: Annulus (*Reversed gas lift*)



Artificial Lift—Rod Pump



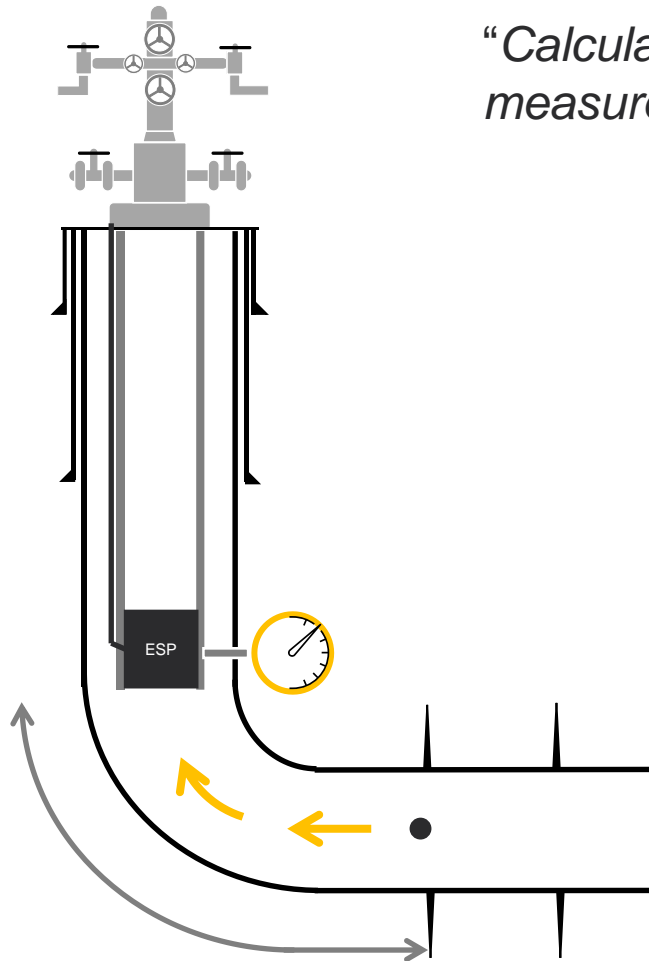
Three Well Segments

- 1) Top Perforation to EOT:
Regular multiphase pipe flow
- 2) EOT to Liquid Level in Annulus:
Stagnant column of liquid and gas
- 3) Liquid Level in Annulus to Wellhead
Single-phase gas flow

Artificial Lift—ESP

The measured pressures from the ESP gauge can be used with the option:

“Calculate from gauge to sandface using measured pressures”.



Well Data

1 Well Deviation Survey 2 Well Data

Configuration 1
Flowpath: Tubing
Artificial Lift: ESP

1 Wellbore Configuration 1 (Initial)

Casing Data

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)
1	0	7940	4.778	0.0006
2	0	19216	4.276	0.0006

Tubing Data

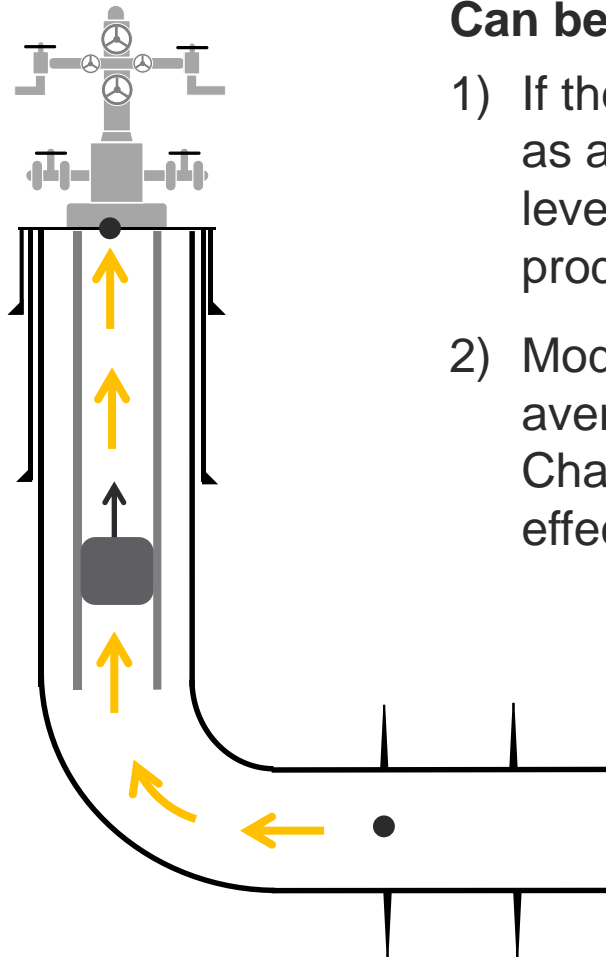
Pipe No. (#)	Bottom MD (ft)	ID (in)	OD (in)	Roughness (in)
1	8000	1.995	2.375	0.0006

Flowpath: Tubing Artificial Lift Method: ESP

Gauge Depth: 0 ft ☒ Calculate from gauge to sandface using measured pressures

SAVE

Artificial Lift—Plunger Lift

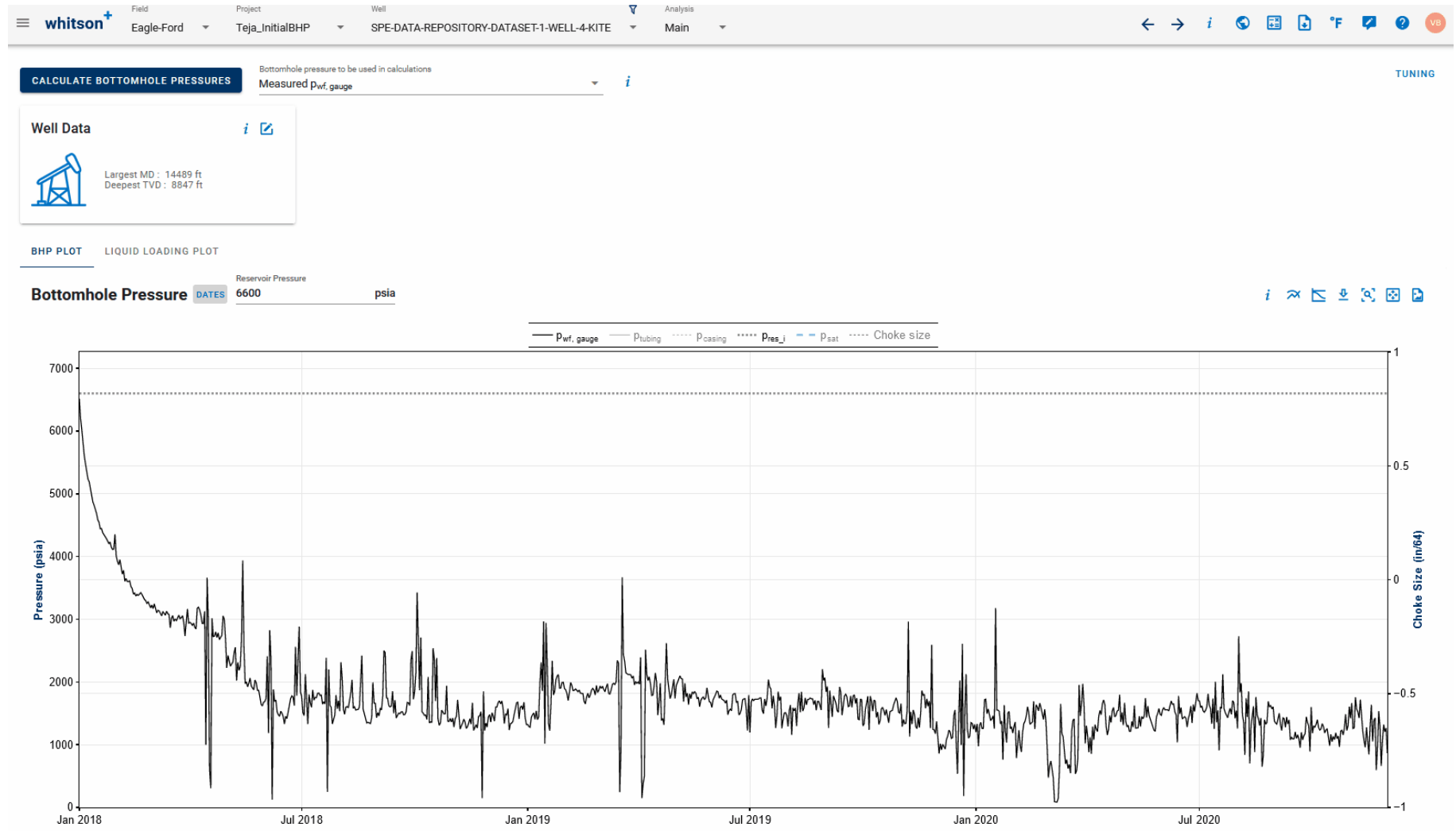


Can be modeled in two ways:

- 1) If the liquid level is measured, it can be modeled as a rod pump configuration provided the liquid level corresponds to times when the well is producing.
- 2) Model as if plunger lift is not installed by using average rates from the production period. Change the OGR of the well to capture the effect of less liquid in the tubing.

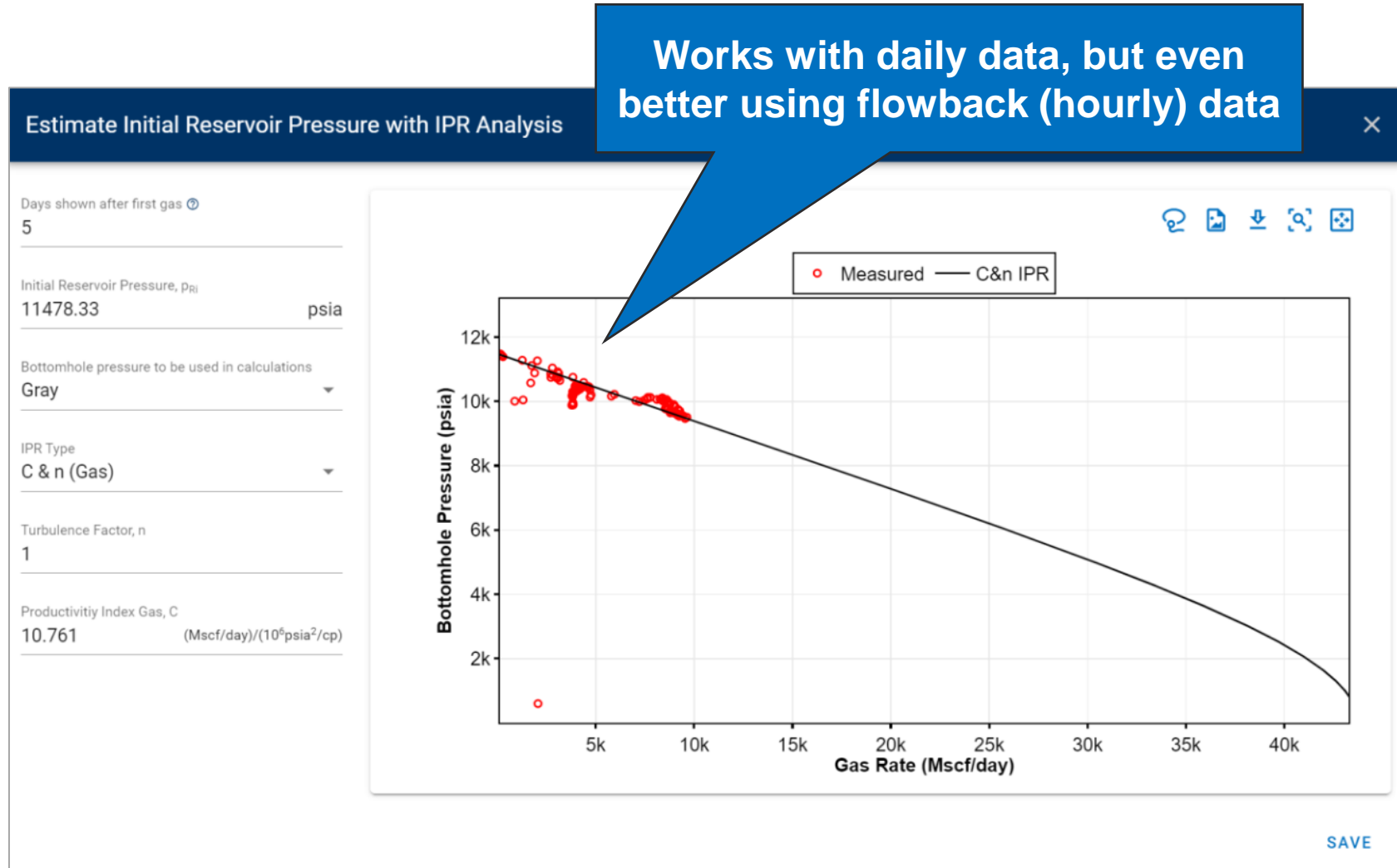
**Estimate initial reservoir
pressure with IPR**

Estimate Initial Reservoir Pressure from IPR



Case study can be found here: <https://youtu.be/PkR-AI0DPj4?feature=shared&t=6298>

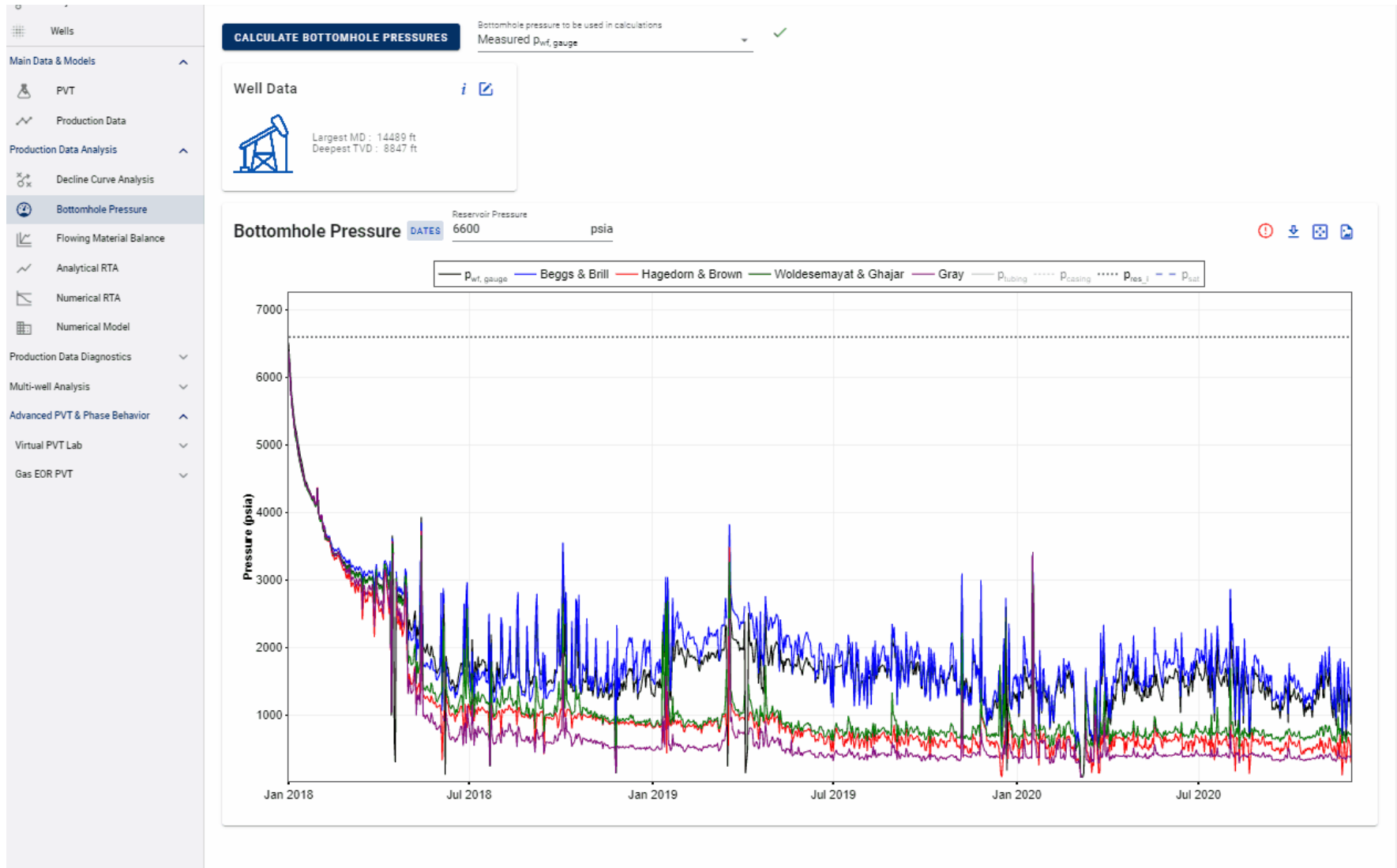
Estimate Initial Reservoir Pressure from IPR



Case study can be found here: <https://youtu.be/PkR-AI0DPj4?feature=shared&t=6298>

BHP Smoothing

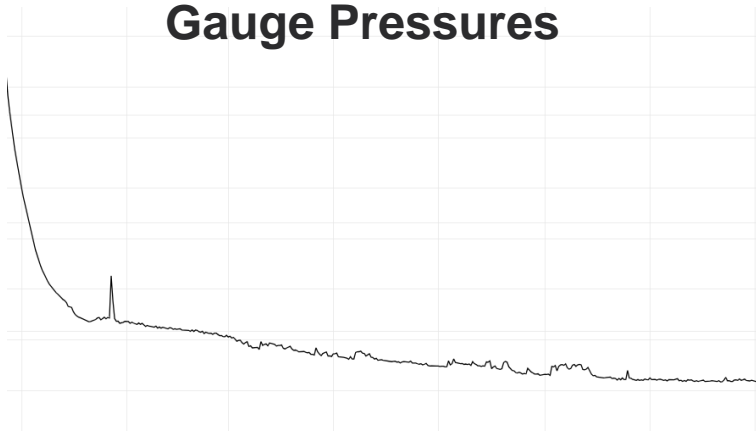
BHP Smoothing



Examples: Gauge Pressures are Smooth!

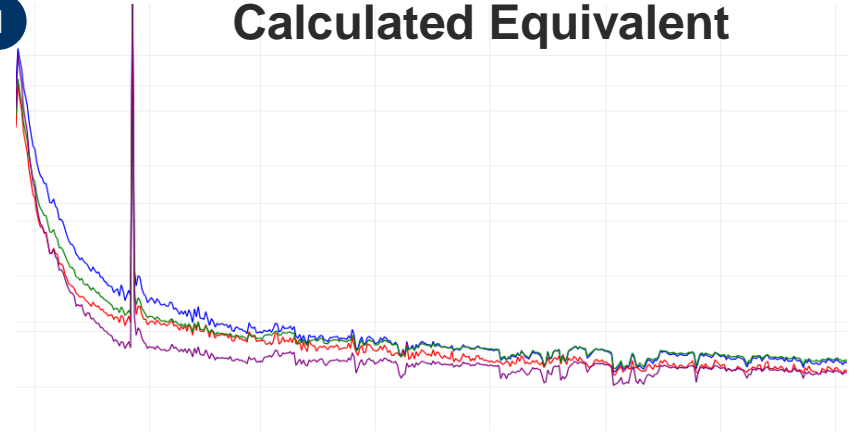
1

Gauge Pressures



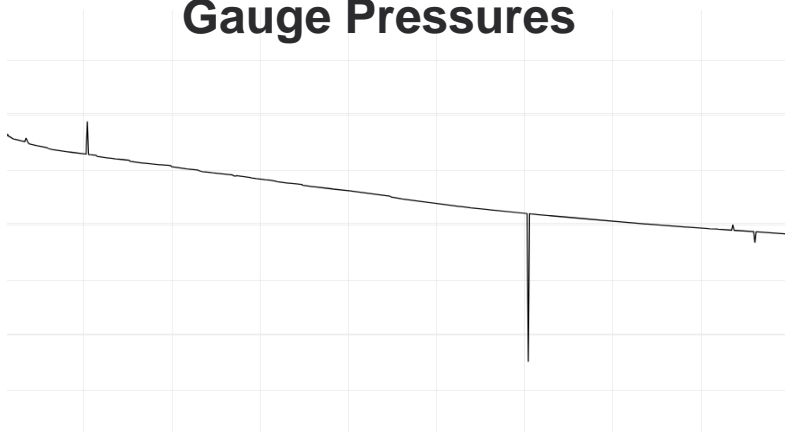
1

Calculated Equivalent



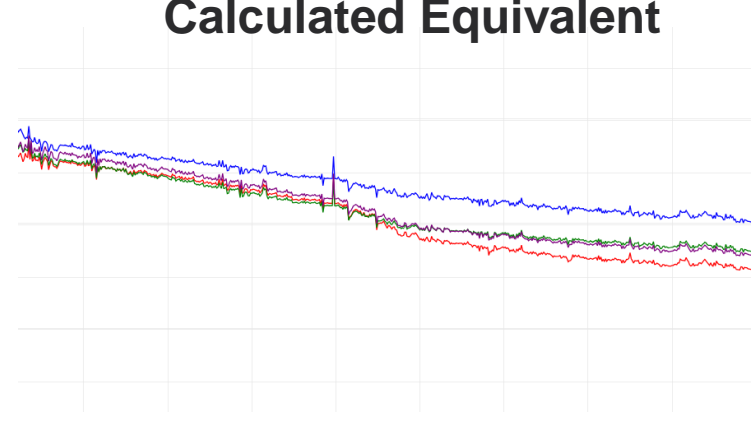
2

Gauge Pressures



2

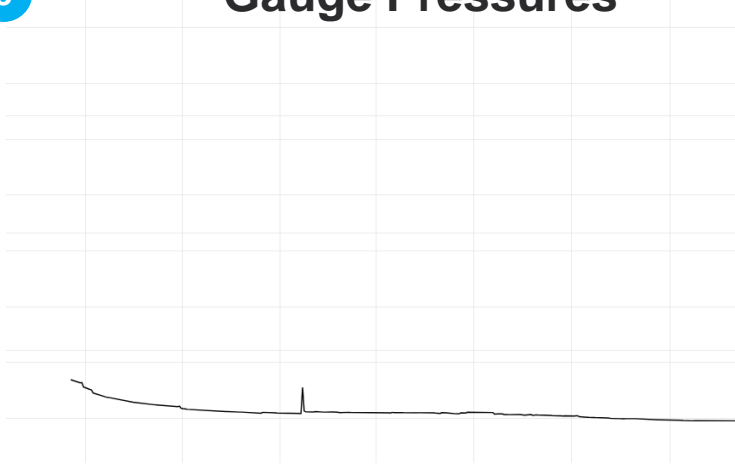
Calculated Equivalent



Examples: Gauge Pressures are Smooth!

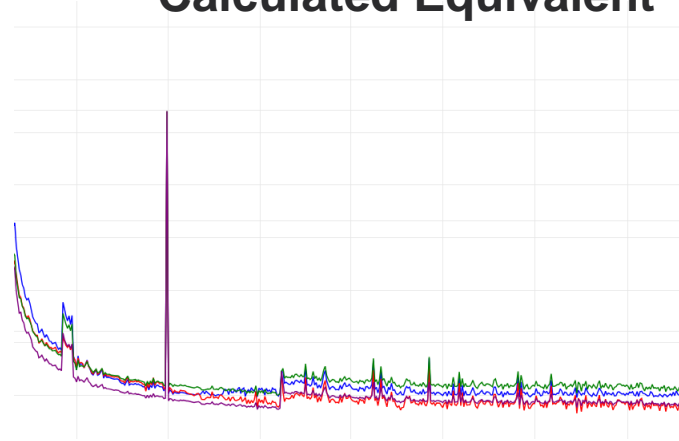
3

Gauge Pressures



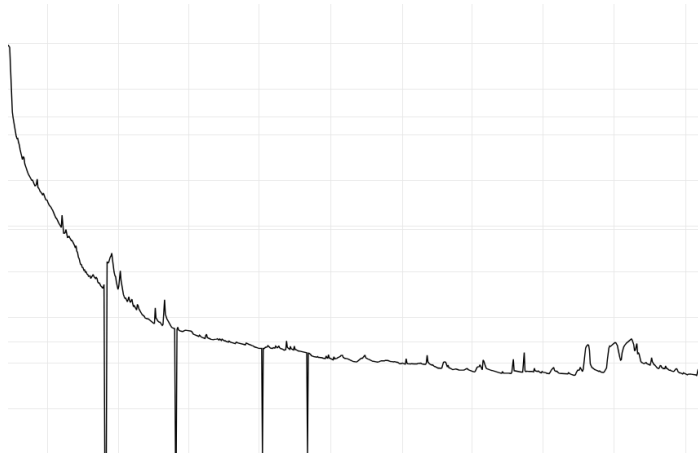
3

Calculated Equivalent



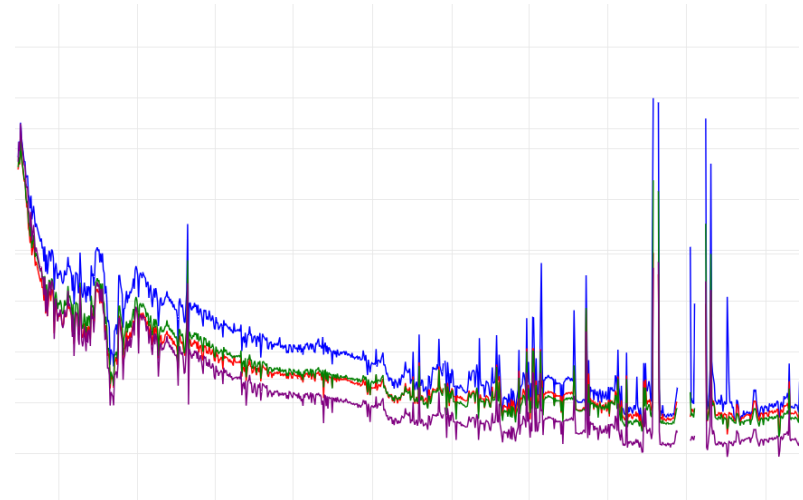
4

Gauge Pressures



4

Calculated Equivalent



BHP Tuning

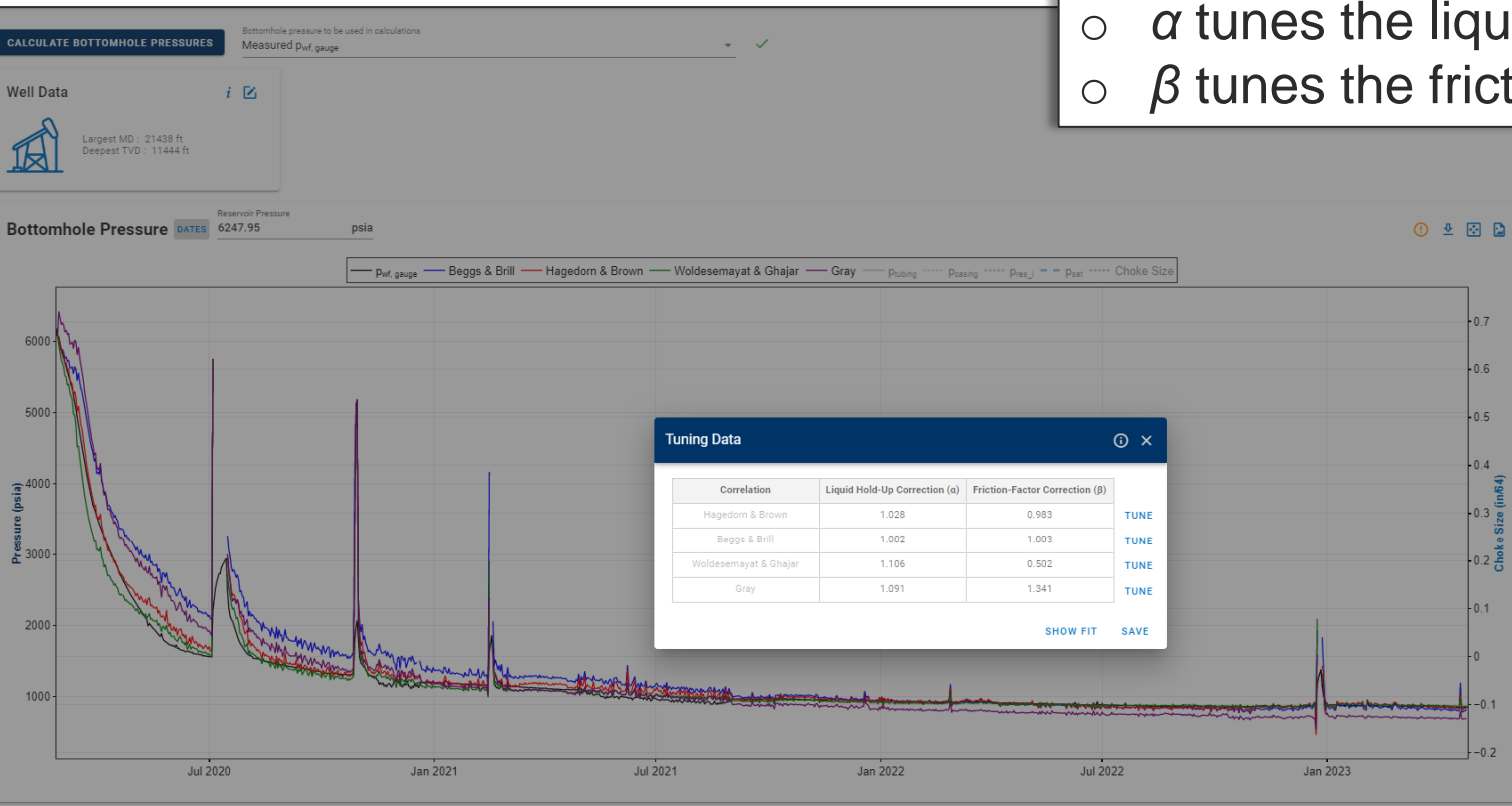
Tuning of Correlations

- The multiphase flow correlations can be tuned against measured pressures

Two-parameter tuning:

- α tunes the liquid hold-up
- β tunes the friction factor

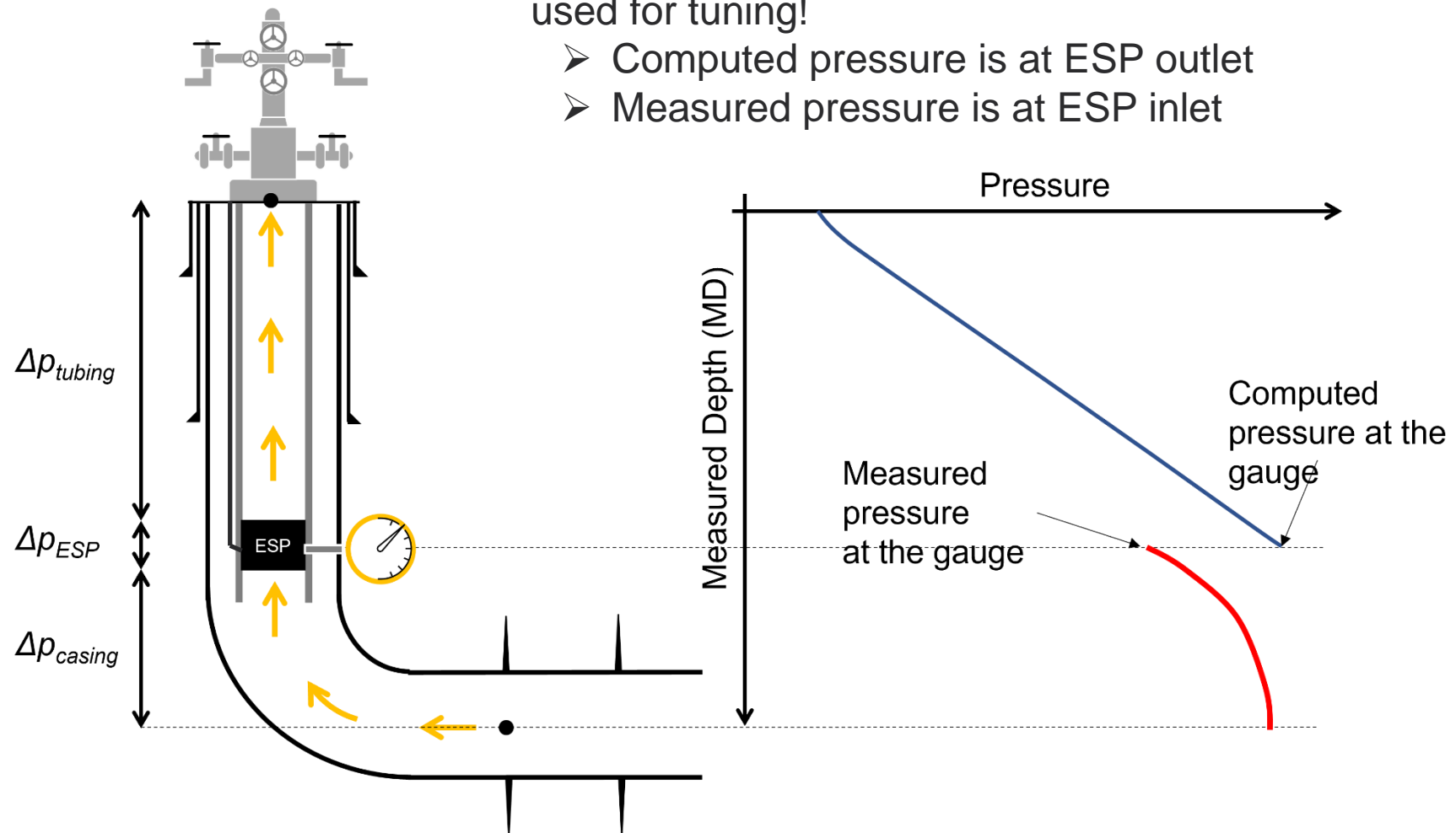
TUNING



Tuning of Correlations—ESP

Caution

- Measured pressures from an ESP should not be used for tuning!
 - Computed pressure is at ESP outlet
 - Measured pressure is at ESP inlet



References

Wiki and Manual


- Pipe-flow theory and correlations

- https://wiki.whitson.com/pipeflow/well_pressure_calculations/

whitson wiki Home Glossary Phase Behavior > Equation of States (EOS) > Black-Oil PVT > Pipe Flow > Well Pressure Calculations Correlations > Contribute About	<h2>Pipe-Flow Calculations</h2> <p>Pipe flow calculations involve estimating the pressure and temperature along the pipe using correlations to describe the fluid- and flow properties. For petroleum engineering applications, particularly calculations in the wellbore, it is common to use a so-called drift-flux model to express the fluid properties in the pressure gradient. The drift-flux model is a type of homogenous model where the phases are lumped together such that single-phase flow equations can be applied, but where it is accounted for gas generally flowing faster than liquid, a concept referred to as slip. This concept was first introduced by Zuber and Findlay (1965)¹. Drift-flux type models are often used because of the simplicity that they offer. The alternative is to solve the momentum- and energy equations for each phase separately which is commonly</p>	Table of contents Base Two-Phase Flow Expressions Local Rates Fluid Fractions Hydraulic Properties Fluid Properties Friction Factor Pressure Profile Gravity Pressure Gradient Friction Pressure Gradient Acceleration Pressure Gradient
---	---	---

- BHP calculations in **whitson⁺**

- <https://manual.whitson.com/modules/well-performance/bottomhole-pressure-calculations/>

whitson⁺ - User Manual Home Onboarding > Modules > Main Data & Models > Production Data Analysis > Decline Curve Analysis Bottomhole Pressure Calculations Analytical RTA Numerical RTA Numerical Model Flowing Material Balance > Production Data Diagnostics > PVT & Phase Behavior >	<h2>Bottomhole Pressure Calculations</h2>  <p>whitson^{BHP}</p>	Table of contents 1. Input 1.1 Production data 1.2 Well deviation survey 1.3 Well data 1.4 Temperature Data 1.5 Artificial-Lift Data 2. Output 2.1 Output Curves 2.2 Curve Smoothing 3. Technical Features 3.1 Governing Equations 3.2 Artificial-Lift Methods 3.2.1 Gas Lift 3.2.2 Rod Pump
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Exercises

Exercise – Agenda

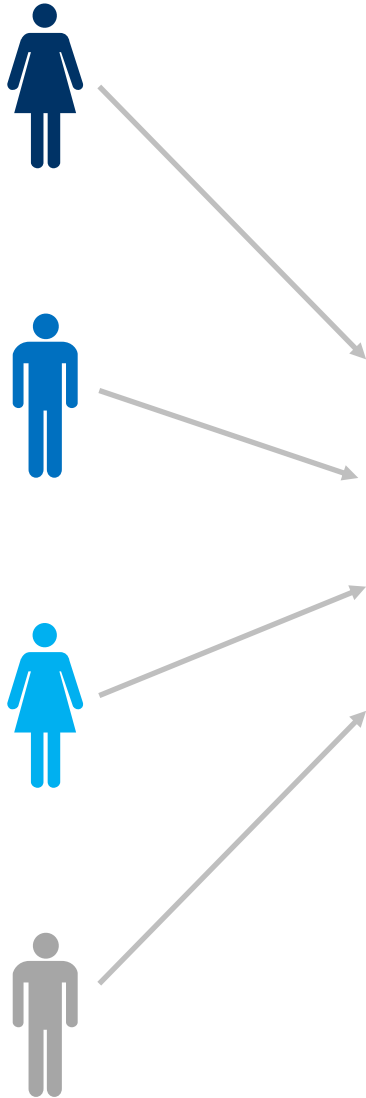
1. Key Features & Functionality:

- a. BHP calculation for well on gas lift
 - Poorboy
 - Valves
 - Automatic (flowing & quiet side)
- b. Custom BHP / BHP smoothing
- c. BHP calculation setting
- d. BHP calculation for well with rod pump
- e. BHP calculation for well on ESP
- f. BHP calculation for dry gas well / Liquid loading

2. BHP tuning exercise

3. Advanced: BHP using Mass Upload Sheet

Access to whitson+



DO NOT USE COMPANY DOMAIN!
Not same as your company domain

<https://courses.whitson.com/>

Username: your e-mail

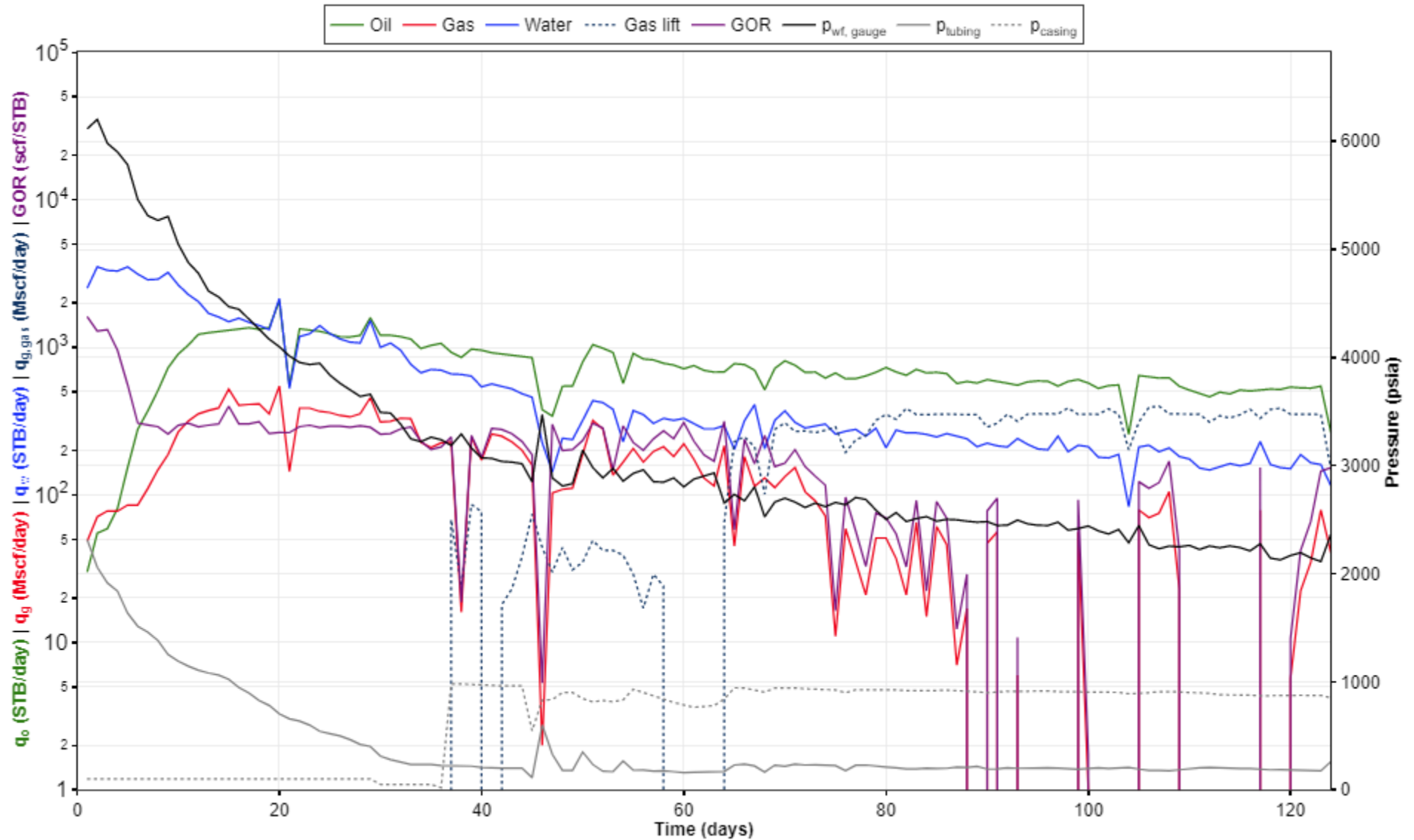
Password: WhitsonBHP2024

*Send an e-mail to support@whitson.com if you need help to login.
Need to use Google Chrome, Firefox or Microsoft Edge.
Internet Explorer won't work.

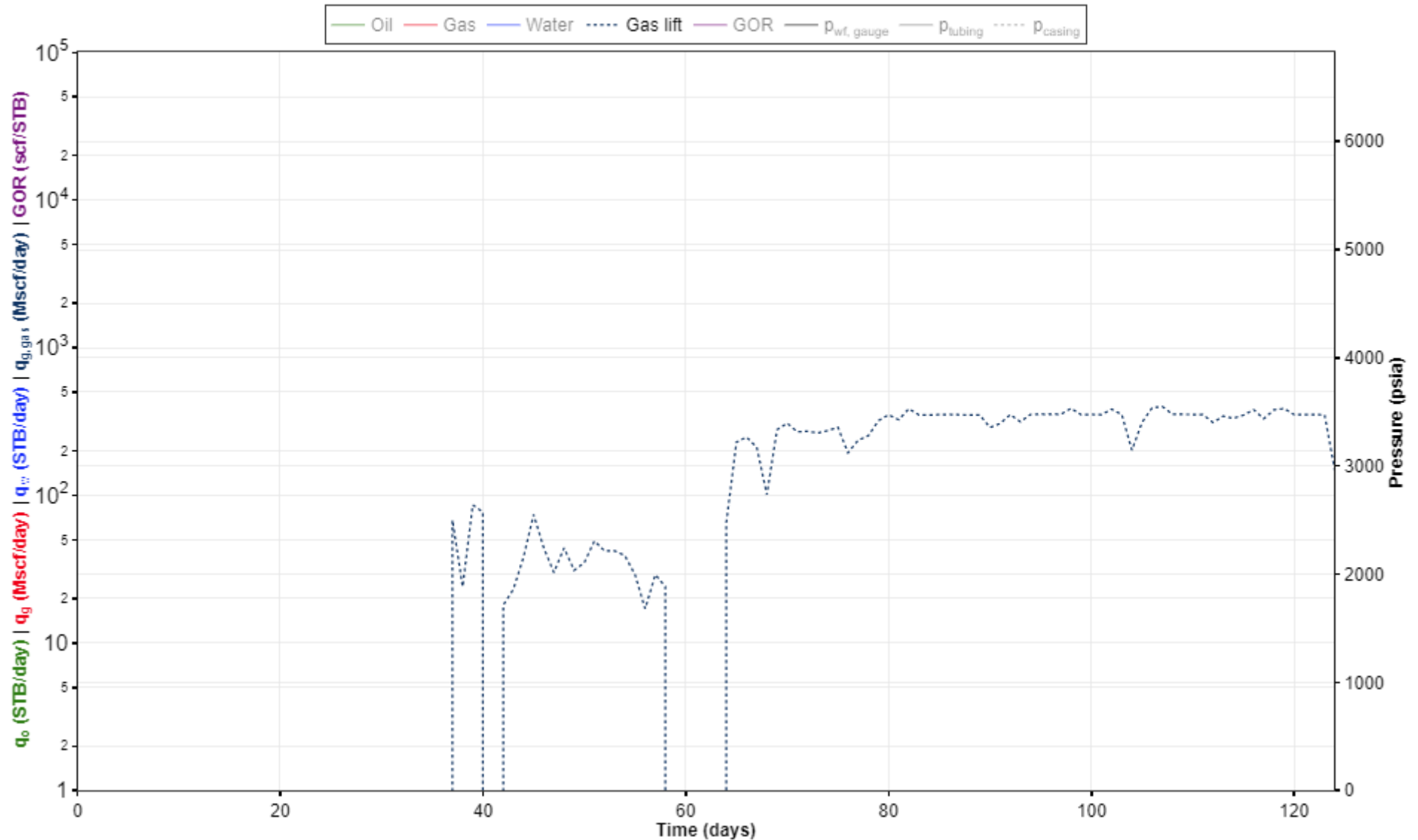
Exercise 1.a

**BHP Calculations
well on gas lift
(Poorboy)**

Gas Lift – Poorboy Configuration



Gas Lift – Poorboy Configuration



Well Deviation Survey

Well Data

1 Well Deviation Survey

2 Well Data

Perforated Interval ?

Top Perforation MD

7600

ft

Bottom Perforation MD

18400

ft

Top Perforation TVD

7515

ft

Bottom Perforation TVD

7598.45

ft

Deviation Survey

(Input entire survey, table expands with input)

CLEAR

Measured Depth (MD) (ft)	True Vertical Depth (TVD) (ft)
0	0
150	150
7600	7515
18600	7600

SAVE

Top & Bottom Perforation Depths

Well Data

1 Well Deviation Survey

2 Well Data

Perforated Interval ?

Top Perforation MD

7600

ft

Bottom Perforation MD

18400

ft

Top Perforation TVD

7515

ft

Bottom Perforation TVD

7598.45

ft

Deviation Survey

(Input entire survey, table expands with input)

CLEAR

Measured Depth (MD) (ft)	True Vertical Depth (TVD) (ft)
0	0
150	150
7600	7515
18600	7600

SAVE

Wellbore Configuration – Casing & Tubing Data

Well Data

1 Well Deviation Survey

2 Well Data

Configuration 1

Flowpath: Unknown

Artificial Lift: None

1 Wellbore Configuration 1 (Initial)

Casing Data

2

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)
1	0	7549	4.778	0.0006
2	0	18598	4.276	0.0006

Tubing Data

1

Pipe No. (#)	Bottom MD (ft)	ID (in)	OD (in)	Roughness (in)
1	7325	1.995	2.375	0.0006

Flowpath
Unknown

Artificial Lift Method
None

Compute Through
Flowing Side

Gauge Depth (MD)
ft

Calculate from gauge to sandface
using measured pressures

+

SAVE

Using the Tubing / Casing Catalogue

Well Data

1 Well Deviation Survey 2 Well Data 3 Temperatures 4 Artificial Lift Data

Tubing Catalogue

OD (in)	Weight (lb/ft)	ID (in)	OD (cm)	Weight (kg/m)	ID (cm)
1.9	5.15	1.3	4.83	7.664	3.306
2.063	3.25	1.751	5.24	4.837	4.448
2.063	4.5	1.613	5.24	6.697	4.096
2.375	4	2.041	6.03	5.953	5.182
2.375	4.6	1.995	6.03	6.846	5.064
2.375	5.8	1.867	6.03	8.631	4.74
2.375	6.6	1.785	6.03	9.822	4.532
2.375	7.35	1.703	6.03	10.938	4.324
2.875	6.4	2.441	7.3	9.524	6.198
2.875	7.8	2.323	7.3	11.608	5.898
2.875	8.6	2.259	7.3	12.798	5.736
2.875	9.35	2.195	7.3	13.914	5.572
2.875	10.5	2.091	7.3	15.626	5.308
2.875	11.5	1.995	7.3	17.114	5.064
3.5	7.7	3.068	8.89	11.459	7.792
3.5	9.2	2.992	8.89	13.691	7.6
3.5	10.2	2.922	8.89	15.179	7.422
3.5	12.7	2.75	8.89	18.9	6.986

SAVE

Wellbore Configuration

1 Well Deviation Survey

2 Well Data

▼ Configuration 1



Flowpath: Tubing

Artificial Lift: Gas Lift

1 Wellbore Configuration 1 (Initial)

Casing Data

− 2 +

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)	
1	0	7549	4.778	0.0006	
2	0	18598	4.276	0.0006	

Tubing Data

− 1 +

Pipe No. (#)	Bottom MD (ft)	ID (in)	OD (in)	Roughness (in)	
1	7325	1.995	2.375	0.0006	

Flowpath

Tubing



Artificial Lift Method

Gas Lift

Gas Lift Configuration

Poor-Boy



Compute Through

Flowing Side



Gauge Depth (MD)

ft



Calculate from gauge to sandface
using measured pressures



Exercise 1.a

**BHP Calculations
well on gas lift
(Valves)**

Gas Lift – Single Valve Depth

1 Well Deviation Survey

2 Well Data

Configuration 1

Flowpath: Tubing

Artificial Lift: Gas Lift

1 Wellbore Configuration 1 (Initial)

Casing Data

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)
				006
				006

Valve Data

Joints: - 1 +

Valve MD
(ft)

17000

SAVE

Flowpath
Tubing

Artificial Lift Method
Gas Lift

Gas Lift Configuration
Valves

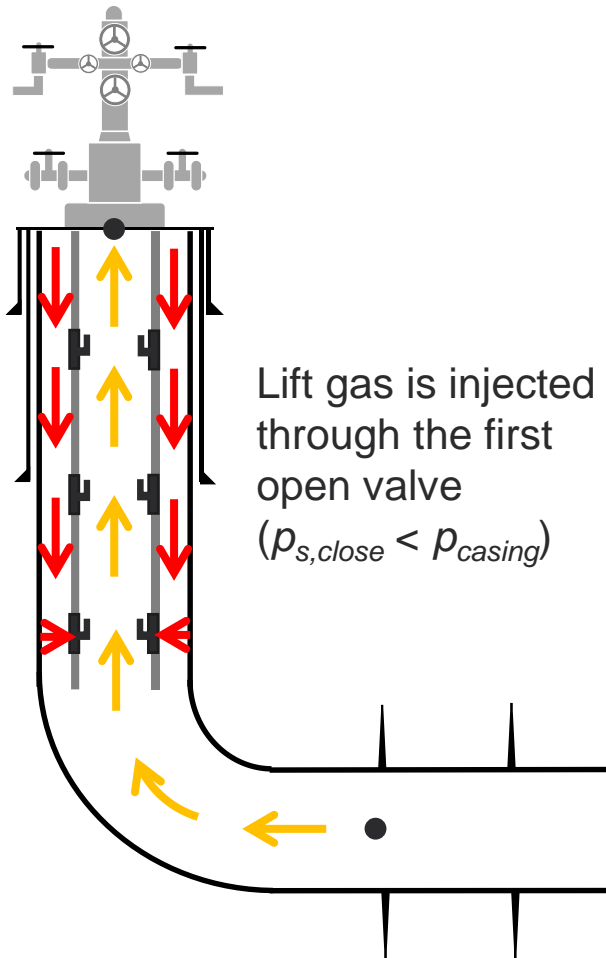
Compute Through
Flowing Side

Gauge Depth (MD) ft

Calculate from gauge to sandface
using measured pressures

Gas Lift – Multiple Valves vs Depth

Flow Path: Tubing



Well Data

1 Well Deviation Survey 2 Well Data

Configuration 1

Flowpath: Tubing

Artificial Lift: Gas Lift

1 Wellbore Configuration 1 (Initial)

Casing Data

Valve Data

☒ Last Valve Always Open

Joints: - 3 +

	Valve MD (ft)	PSO (psia)	PSC (psia)
3	3000	1100	942
2	5000	854	834
1	7000	782	762

SAVE

Flowpath: Tubing

Artificial Lift Method: Gas Lift

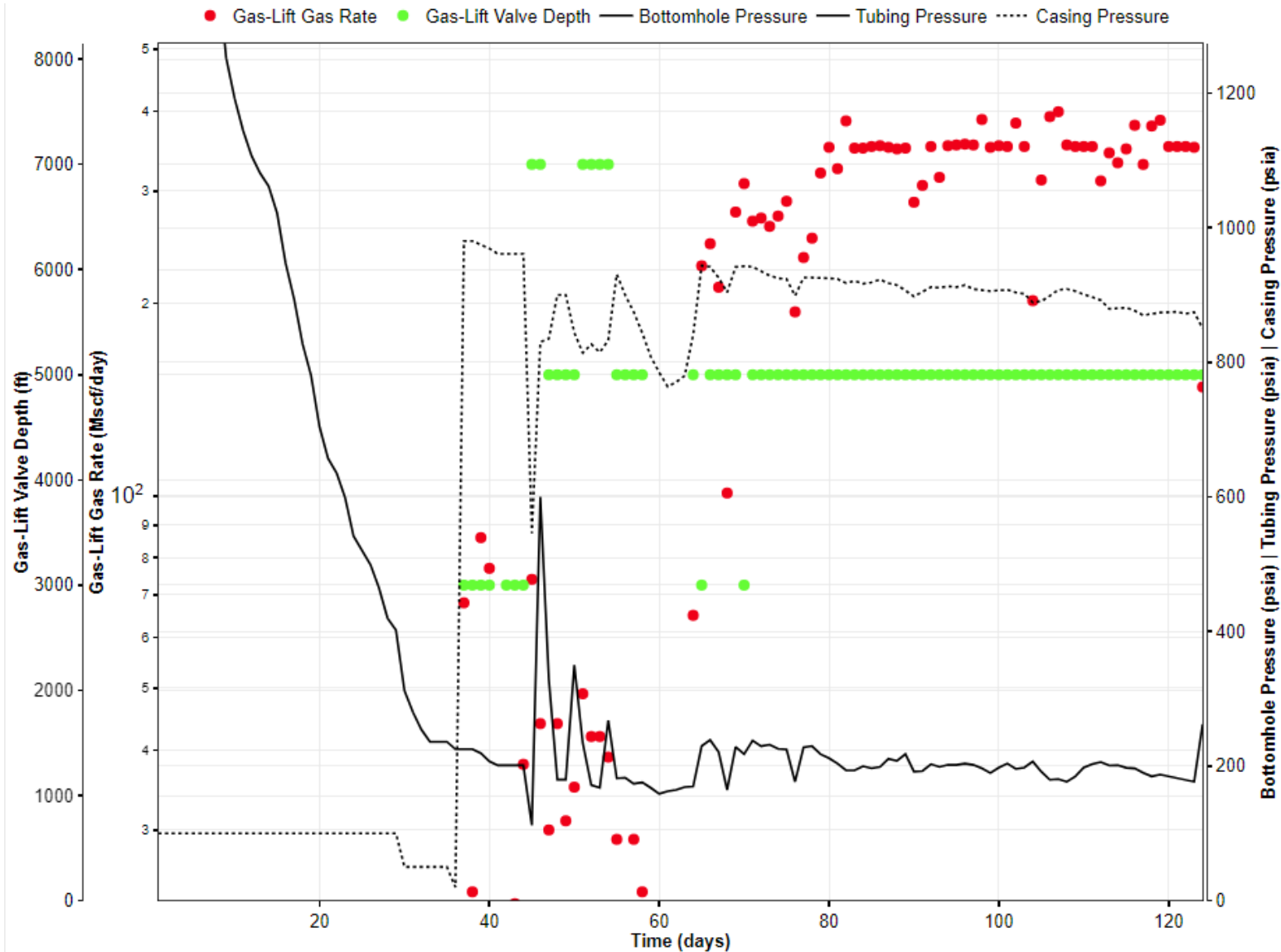
Gas Lift Configuration: Valves

Gauge Depth: 0 ft

Calculate from gauge to sandface using measured pressures

SAVE

Gas Lift – Multiple Valves vs Depth

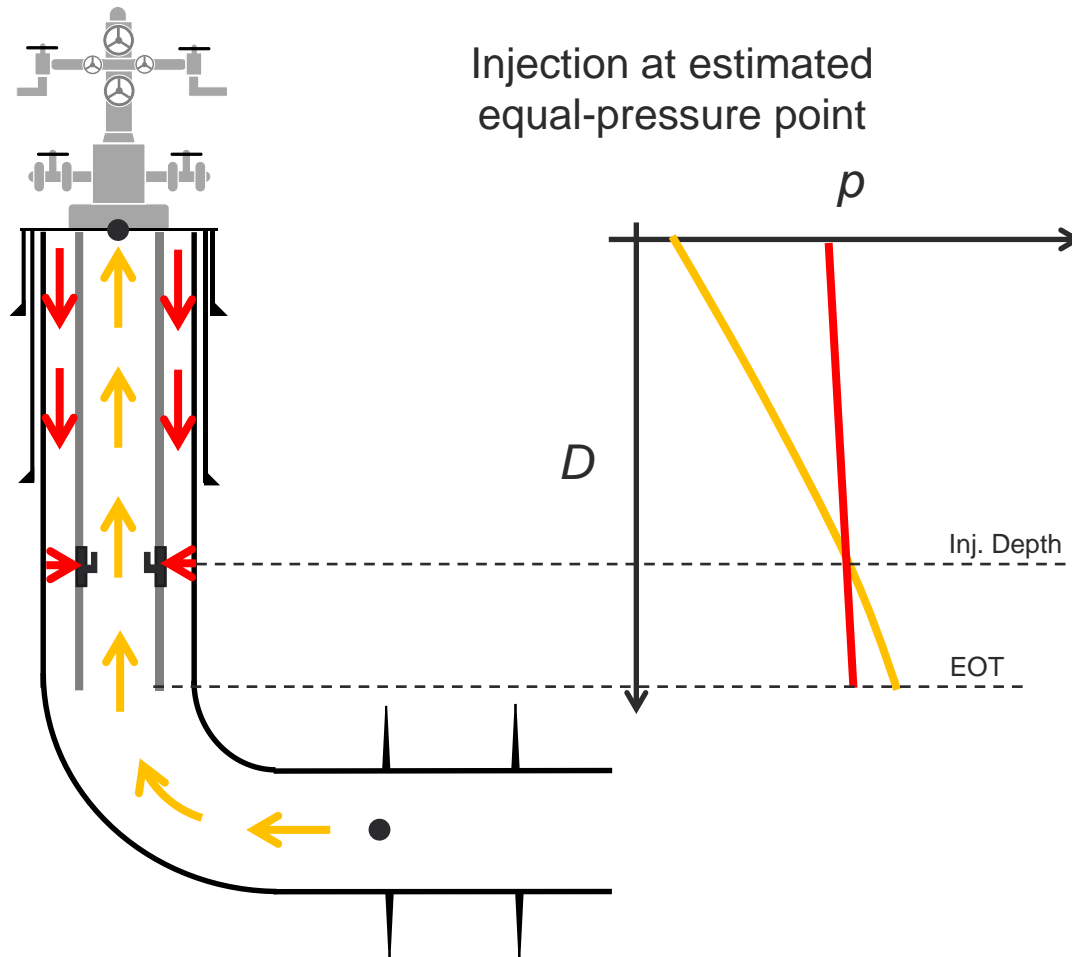


Exercise 1.a

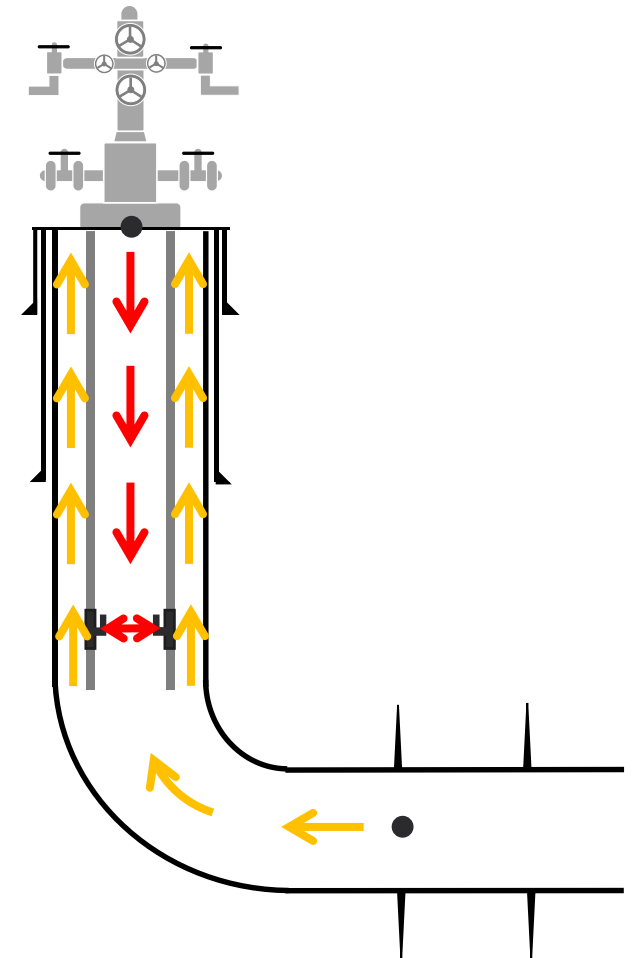
**BHP Calculations
well on gas lift
(Automatic)**

Artificial Lift—Gas Lift | Automatic

Flow Path: Tubing



Flow Path: Annulus (*Reversed gas lift*)



Gas Lift – Automatic

Well Data

1 Well Deviation Survey

2 Well Data

Configuration 1

Flowpath: Tubing

Artificial Lift: Gas Lift

1 Wellbore Configuration 1 (Initial)

Casing Data

2

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)
1	0	7549	4.778	0.0006
2	0	18598	4.276	0.0006

Tubing Data

1

Pipe No. (#)	Bottom MD (ft)	ID (in)	OD (in)	Roughness (in)
1	7325	1.995	2.375	0.0006

Flowpath
Tubing

Artificial Lift Method
Gas Lift

Gas Lift Configuration
Automatic

Gauge Depth
0

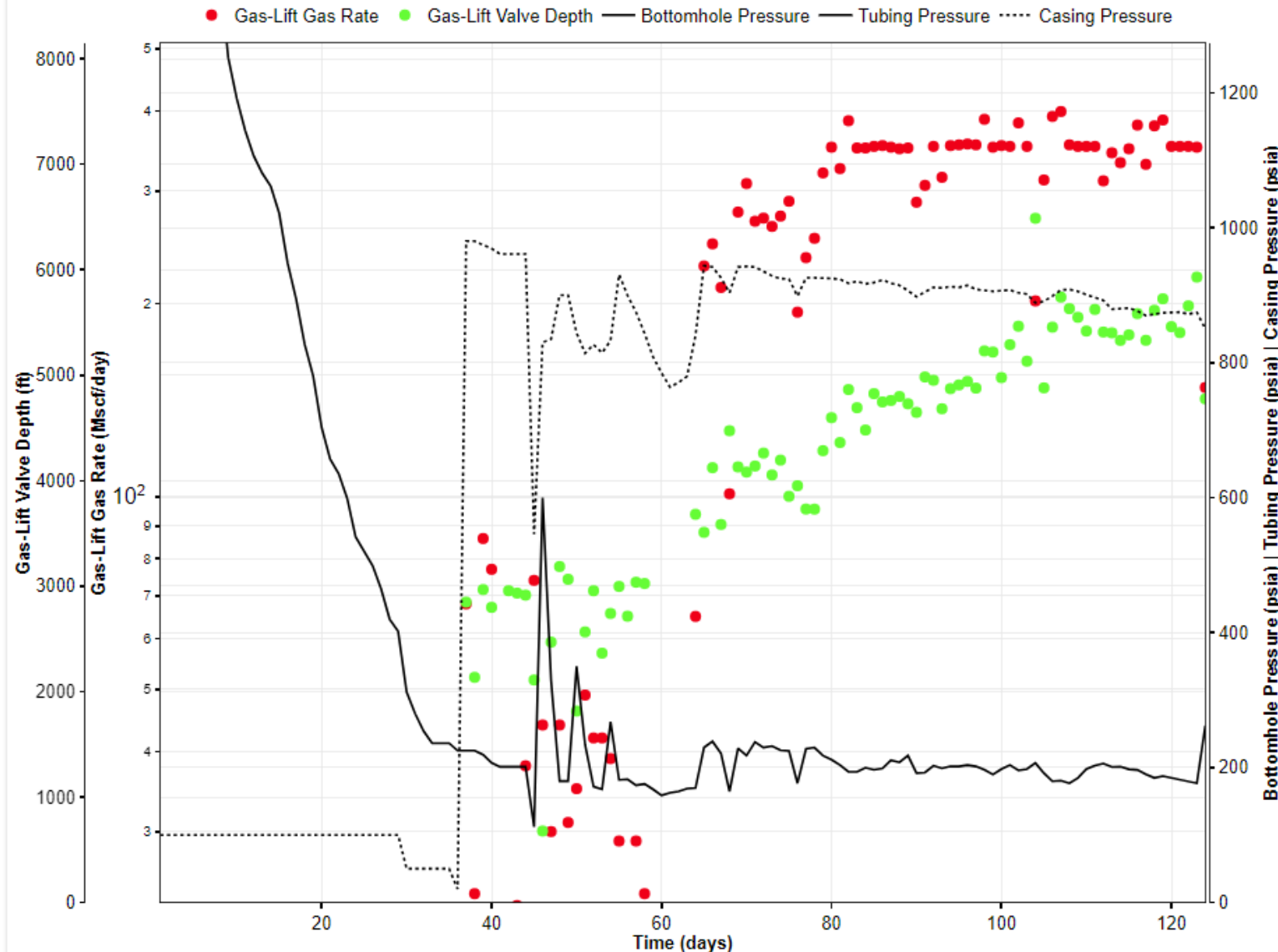
ft

Calculate from gauge to sandface
using measured pressures

+

SAVE

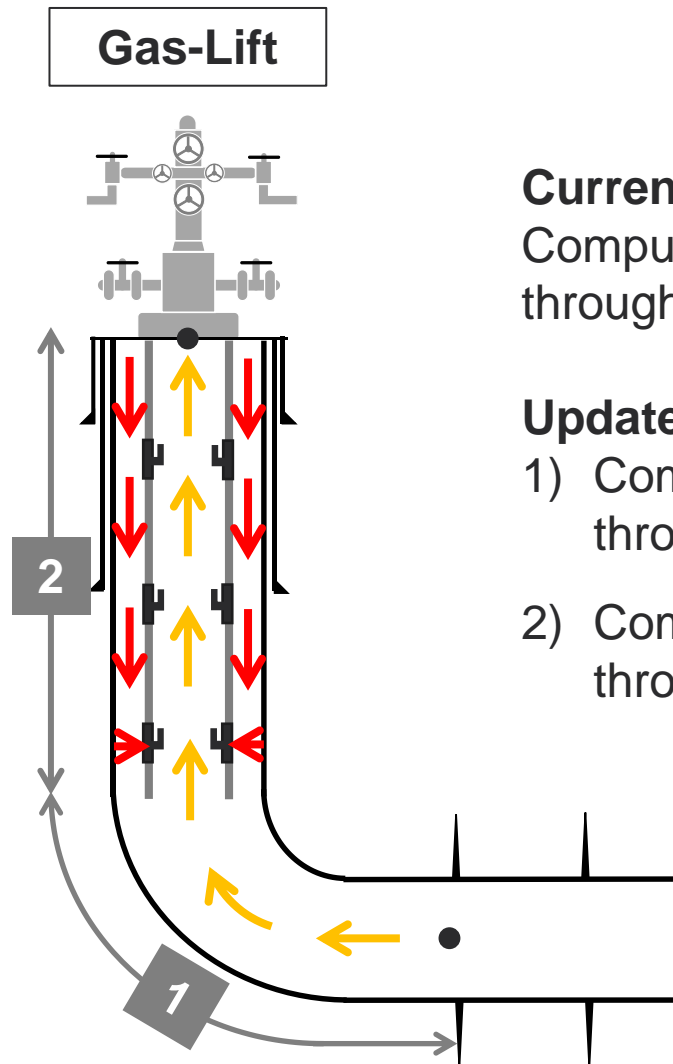
Gas Lift – Multiple Valves vs Depth



Exercise 1.a

**BHP Calculations
well on gas lift
(Quiet / Silent Side)**

BHP Calculations Using the “Quiet Side”



Current:

Compute the well pressure from TP to WH through the multiphase wellstream

Update:

- 1) Compute the well pressure from TP to valve through the *multiphase* wellstream
- 2) Compute the well pressure from valve to WH through the *single-phase* lift-gas column

Gas Lift – Automatic

Well Data

1 Well Deviation Survey

2 Well Data

Configuration 1

Flowpath: Tubing

Artificial Lift: Gas Lift

1 Wellbore Configuration 1 (Initial)

Casing Data

2

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)
1	0	7549	4.778	0.0006
2	0	18598	4.276	0.0006

Tubing Data

1

Pipe No. (#)	Bottom MD (ft)	ID (in)	OD (in)	Roughness (in)
1	7325	1.995	2.375	0.0006

Flowpath
Tubing

Artificial Lift Method
Gas Lift

Gas Lift Configuration
Automatic

Compute Through
Static (Quiet) Side

Compute Static Down To
Gas-Lift Valve

Gauge Depth (MD)

ft

☐

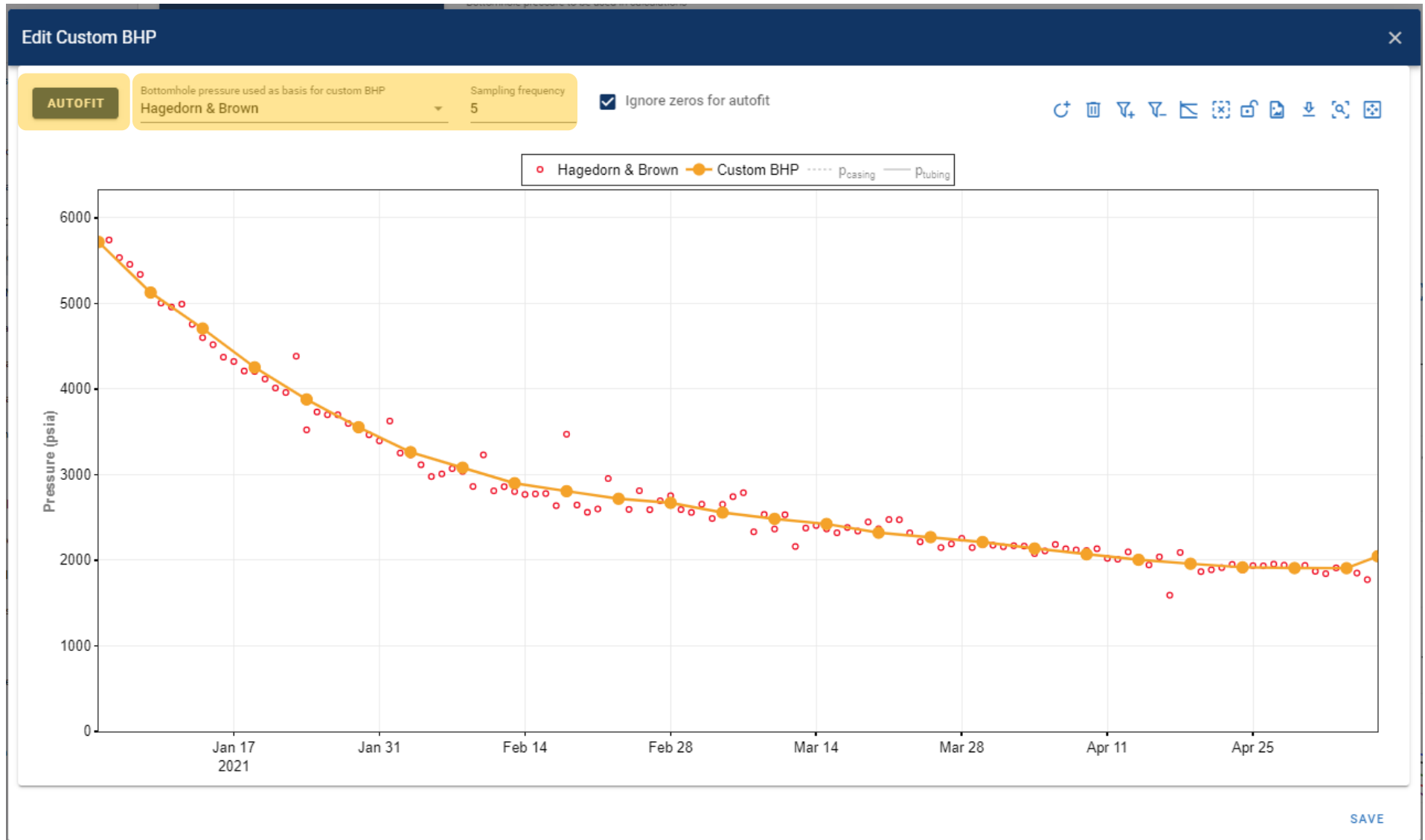
Calculate from gauge to sandface
using measured pressures

SAVE

Exercise 1.b

Custom p_{wf}
 p_{wf} Smoothing

Custom p_{wf} / p_{wf} Smoothing



Exercise 1.c

BHP Calculation Settings

BHP Calculation Settings

Well Data

1 Well Deviation Survey 2 Well Data

Configuration 1
Flowpath: Tubing
Artificial Lift: ESP

1 Wellbore Configuration 1 (Initial)

Casing Data

Pipe No	Top MD	Bottom MD	ID	Roughness (in)
				0.0006
				0.0006

Artificial-Lift Settings

- ☒ Gas Lift: Compute when Gas-Lift Rate is 0
- ☒ Rod Pump: Compute when Liquid Level is 0
- ☐ ESP: Compute when Gauge Pressure is 0

SAVE

Flowpath: Tubing
Artificial Lift Method: ESP

Gauge Depth: 8332 ft

Calculate from gauge to sandface using measured pressures

SAVE

Exercise 1.d

BHP Calculations well with rod pump

Well Data – Add New Configuration

Well Data

1 Well Deviation Survey

2 Well Data

Configuration 1

Flowpath: Casing

Artificial Lift: None

1 Wellbore Configuration 1 (Initial)

Casing Data

– 1 +

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)
1	0	13915	4	0.0006

Tubing Data

– 0 +

Flowpath

Casing

Gauge Depth

0

ft

Calculate from gauge to sandface using measured pressures

SAVE

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Well Data – Select Rod Pump AL Method

Well Data

1 Well Deviation Survey

2 Well Data

▼ Configuration 1

Flowpath: Casing

Artificial Lift: None

▼ Configuration 2

Flowpath: Tubing

Artificial Lift: Rod Pump

1 Wellbore Configuration 1 (Initial)

2 Wellbore Configuration 2

Use From Date (mm/dd/yyyy)

03/05/2015

Casing Data

–

1

+

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)
1	0	13915	4	0.0006

Tubing Data

–

1

+

Pipe No. (#)	Bottom MD (ft)	ID (in)	OD (in)	Roughness (in)
1	7022	2.441	2.875	0.0006

Flowpath
Tubing

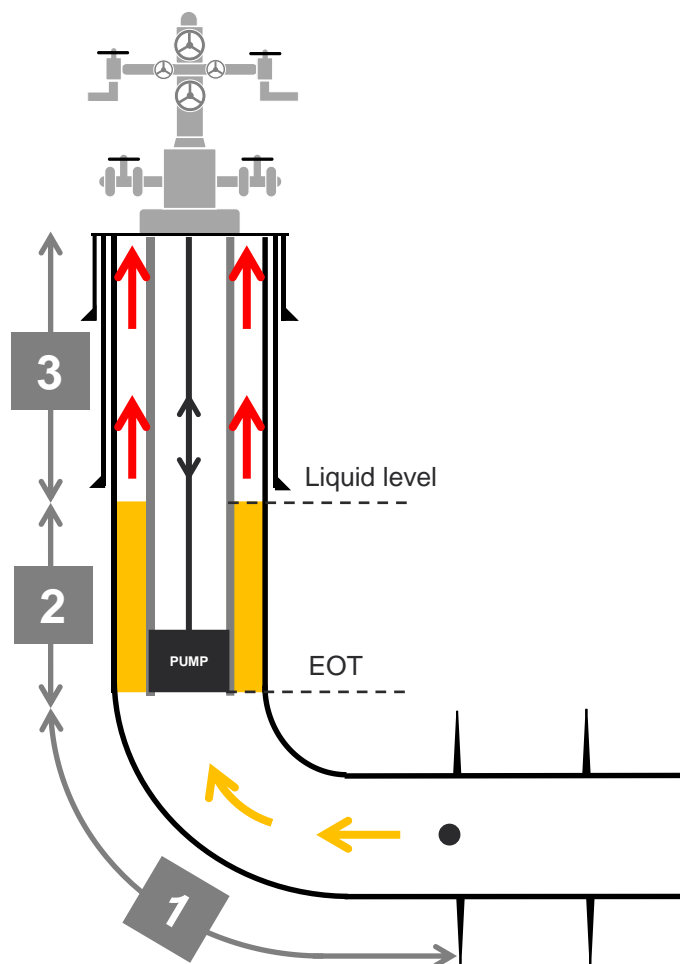
Artificial Lift Method
Rod Pump

Gauge Depth
0

ft

Calculate from gauge to sandface
using measured pressures

Artificial Lift—Rod Pump



Three Well Segments

- 1) Top Perforation to EOT:
Regular multiphase pipe flow
- 2) EOT to Liquid Level in Annulus:
Stagnant column of liquid and gas
- 3) Liquid Level in Annulus to Wellhead
Single-phase gas flow

Quiz !



Quiz !



BHP Calculation Settings

Well Data

1 Well Deviation Survey 2 Well Data

Configuration 1
Flowpath: Tubing
Artificial Lift: ESP

1 Wellbore Configuration 1 (Initial)

Casing Data

Pipe No	Top MD	Bottom MD	ID	Roughness (in)
				0.0006
				0.0006

Artificial-Lift Settings

- ☒ Gas Lift: Compute when Gas-Lift Rate is 0
- ☒ Rod Pump: Compute when Liquid Level is 0
- ☐ ESP: Compute when Gauge Pressure is 0

SAVE

Flowpath: Tubing
Artificial Lift Method: ESP

Gauge Depth: 8332 ft

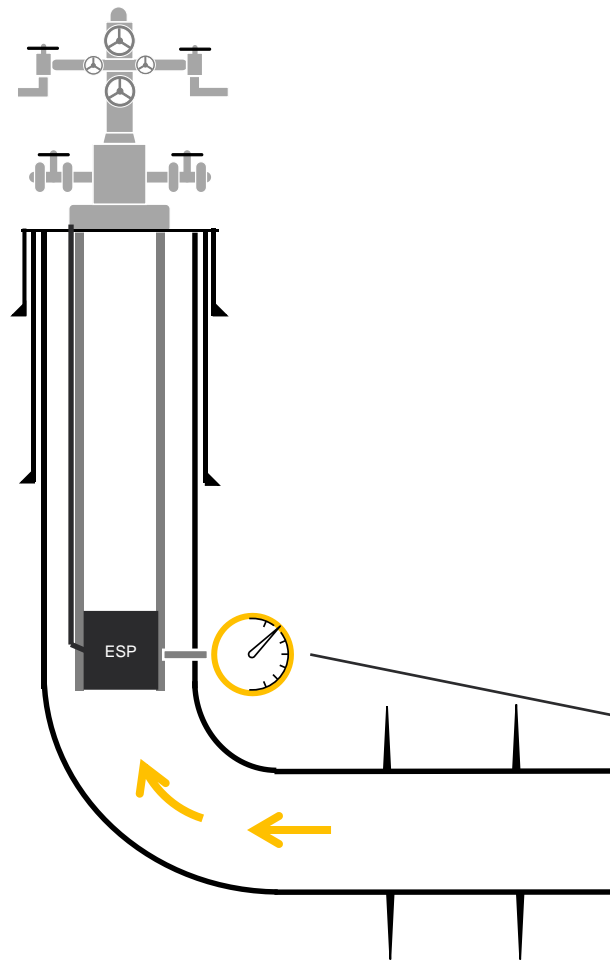
Calculate from gauge to sandface using measured pressures

SAVE

Exercise 1.e

**BHP Calculations
well on ESP**

BHP Calculation – Well on ESP



Well Data

1 Well Deviation Survey

2 Well Data

Configuration 1

Flowpath: Tubing

Artificial Lift: ESP

1 Wellbore Configuration 1 (Initial)

Casing Data

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)
1	0	8384	4.67	0.0006
2	6138	14522	4.276	0.0006

Tubing Data

Pipe No. (#)	Bottom MD (ft)	ID (in)	OD (in)	Roughness (in)
1	8332	2.441	2.875	0.0006

Flowpath

Tubing

Artificial Lift Method

ESP

Gauge Depth

8332

ft

Calculate from gauge to sandface using measured pressures

+

SAVE

Exercise 1.f

BHP Calculations on a Dry Gas Well (Liquid Loading)

BHP Calculation – Well on ESP

BHP PLOT

LIQUID LOADING PLOT

Liquid Loading

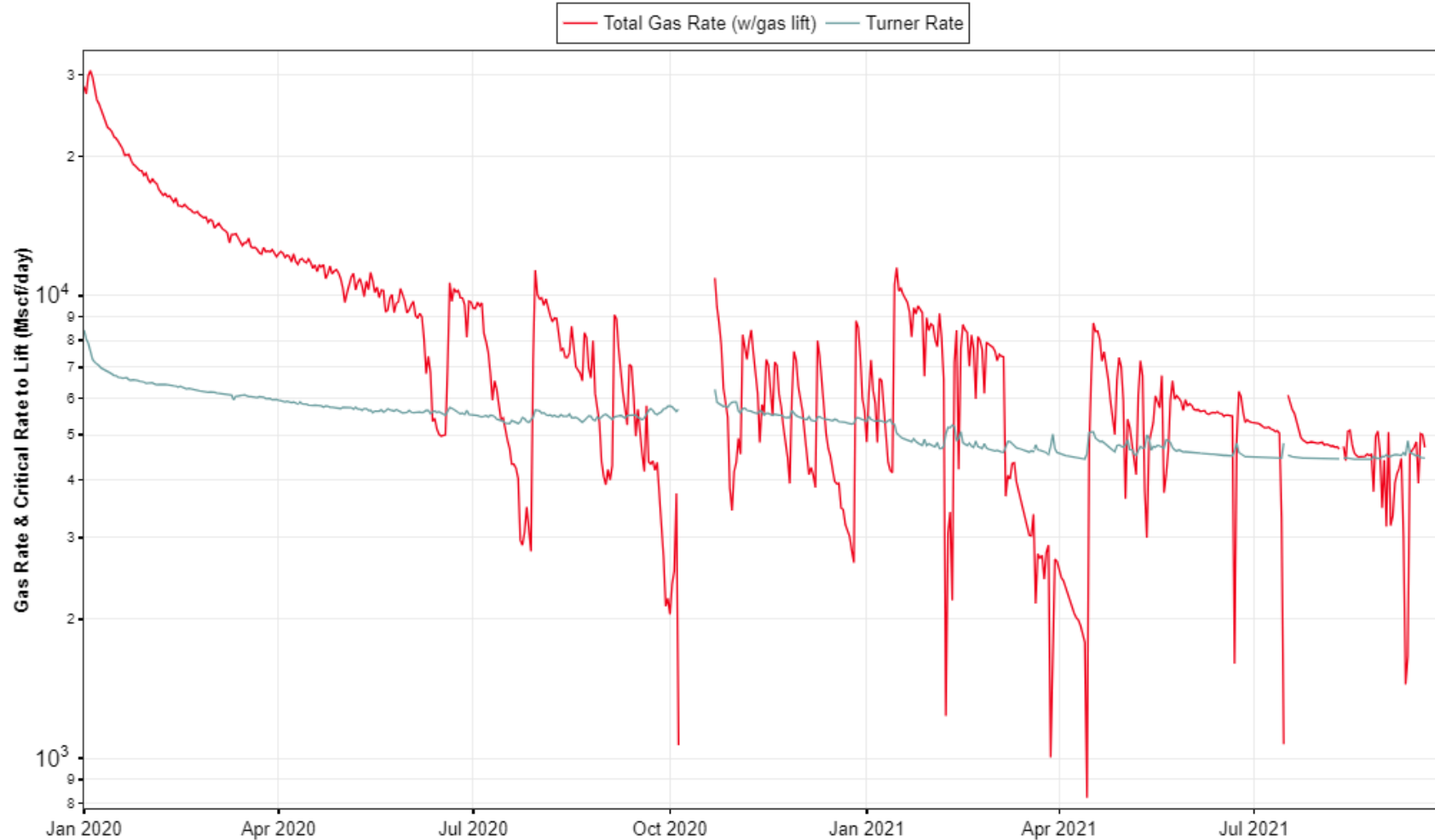
LOG Y

DATES

Critical Rate Correlation
Turner

Critical Rate Depth Type
Top Perforation

Critical Rate Depth Value
7542 ft



The Whitson logo, consisting of the word "whitson" in a bold, dark blue, sans-serif font, is positioned in the upper right corner of the slide. It is set against a white rectangular background that partially overlaps the city skyline image.

whitson

whitson⁺

Nodal Analysis

Graham Helfrick

2 October 2024

½ Day Course

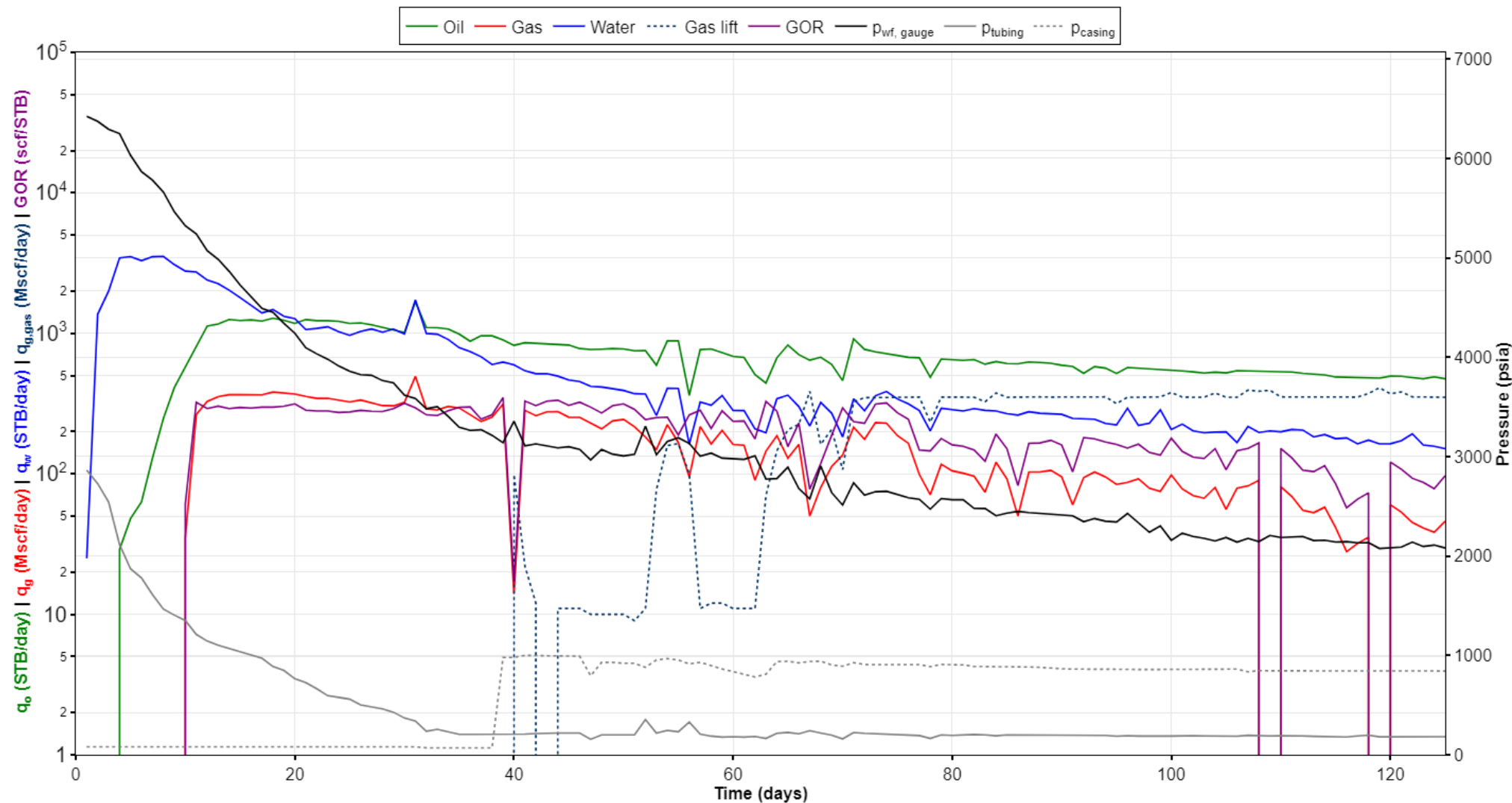
(Included in your subscription!)



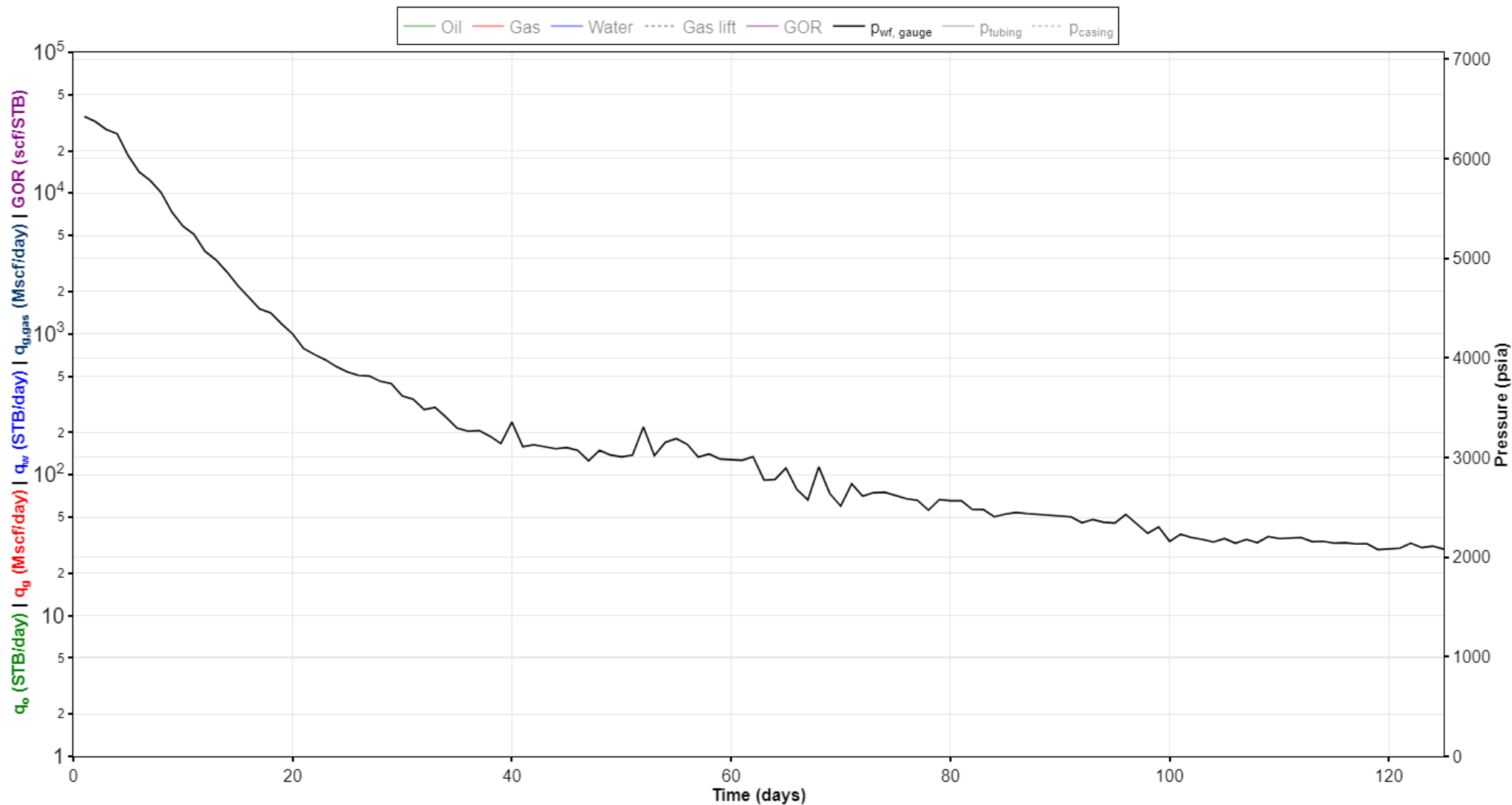
Exercise 2

BHP Correlation Tuning to Measured Gauge Data

BHP Tuning – Measured Gauge Pressures



BHP Tuning – Measured Gauge Pressures



BHP Tuning – Gauge Depth

Well Data

1 Well Deviation Survey

2 Well Data

Configuration 1

Flowpath: Tubing

Artificial Lift: Gas Lift

1 Wellbore Configuration 1 (Initial)

Casing Data

2

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)
1	0	7499	4.778	0.0006
2	10541	18040	4.276	0.0006

Tubing Data

1

Pipe No. (#)	Bottom MD (ft)	ID (in)	OD (in)	Roughness (in)
1	7595	1.995	2.375	0.0006

Flowpath
Tubing

Artificial Lift Method
Gas Lift

Gas Lift Configuration
Valves

Gauge Depth
7595

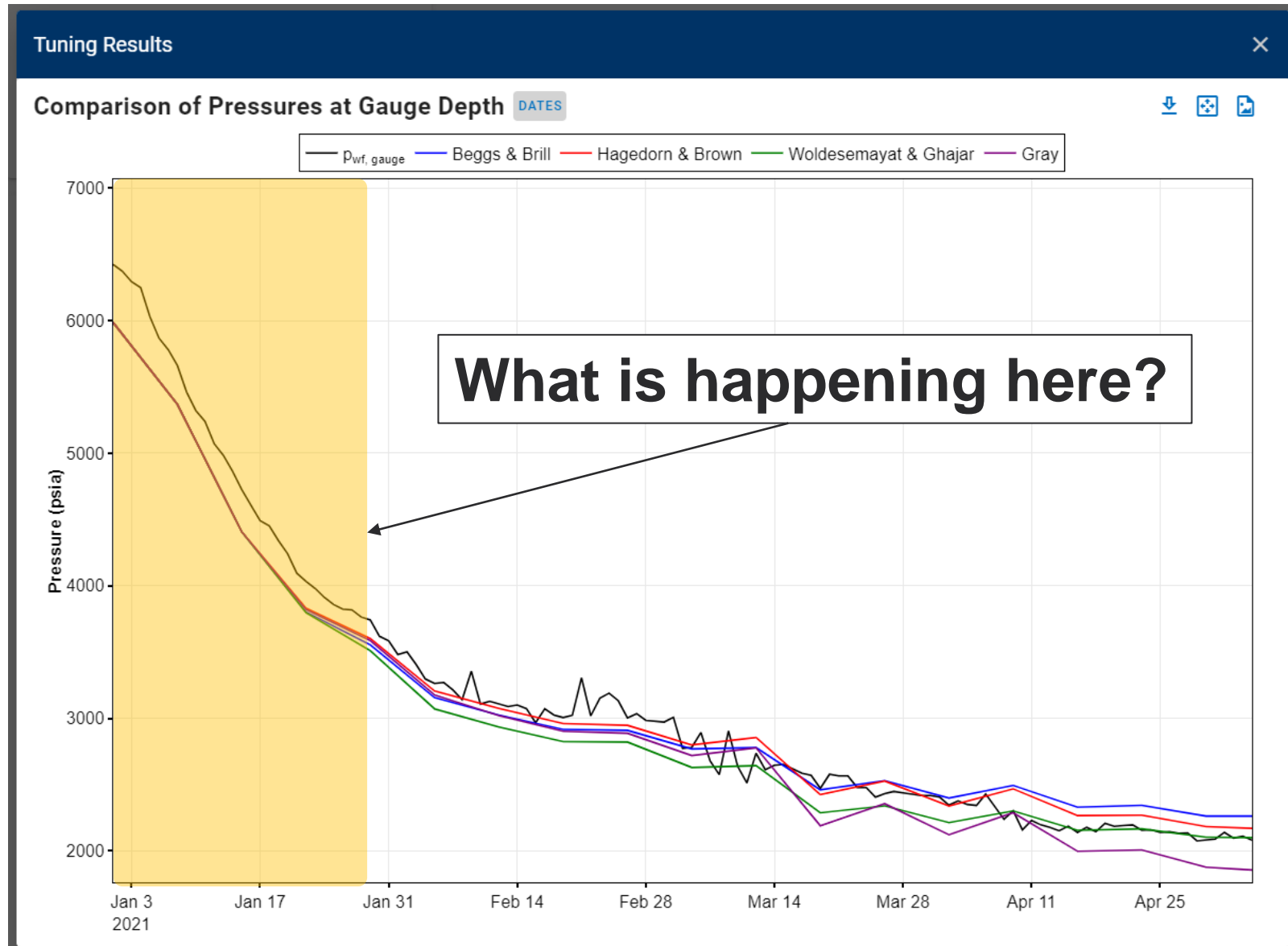
ft

Calculate from gauge to sandface
using measured pressures

+

SAVE

BHP Tuning – 1st Iteration



BHP Tuning – 1st Iteration

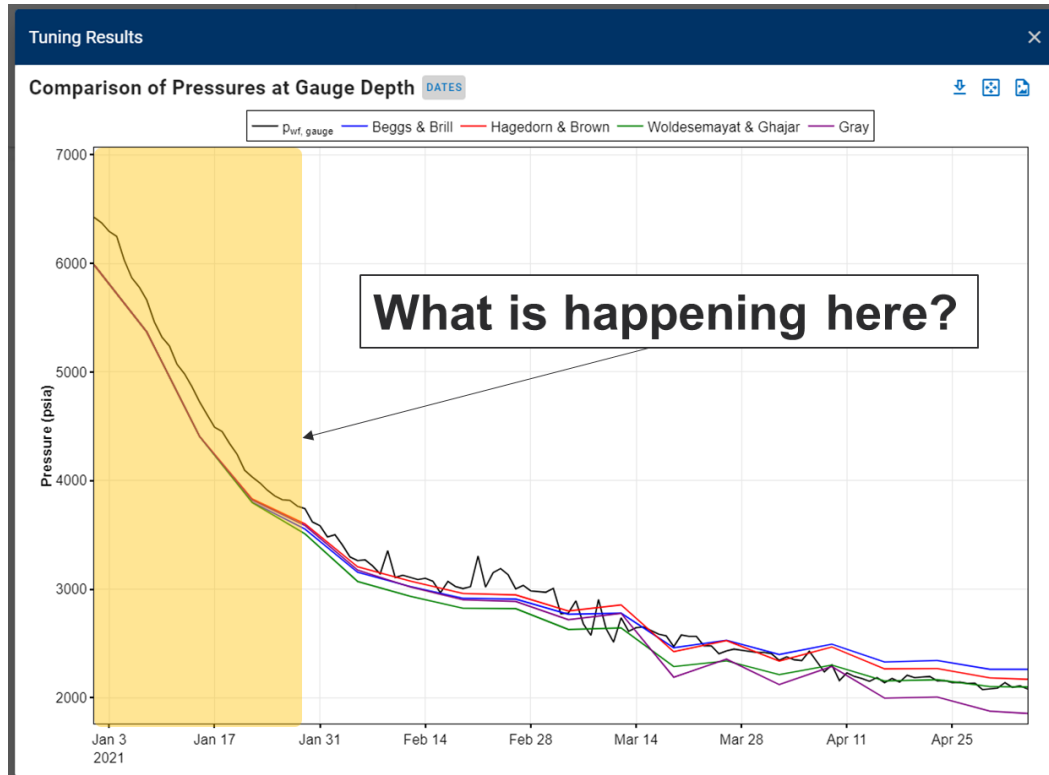
This is the region where the wellbore is still filled with **single phase fluid**.

For this **single phase** region, tuning the **multiphase correlations** doesn't make much sense.

Instead we need to adjust the fluid densities which is done through:

- PVT (for oil & gas densities)
- water salinity (for water density)

Always start with salinity if you have a single phase region.



BHP Tuning – 2nd Iteration (Salinity)

Adjust salinity iteratively until the single phase region gives a better match.

For this exercise, we can focus on the **Hagedorn & Brown** correlation only.

As a reference

- **Sea water salinity:** 10k – 35k ppm
- **Brine salinity:** 35k – 250k ppm

The screenshot shows the 'Well Data' interface with a 'Well Deviation Survey' tab. A 'Perforated Interval' section displays top and bottom perforation measurements in MD and TVD. A 'Water PVT & Viscosity' dialog box is open, showing a 'Water Salinity' input field set to 0 ppm. Below this, it displays calculated 'Density at p_{sc}, T_{sc}' as 62.3718 lb/ft³ and 'Viscosity at p_{sc}, T_{sc}' as 0.2736 cp. A 'SAVE' button is visible at the bottom right of the dialog. The background interface includes a table with two columns of numerical data.

Top Perforation MD	Bottom Perforation MD
7828	17825

Top Perforation TVD	Bottom Perforation TVD
7485.69	7212.89

Water Salinity
0 ppm

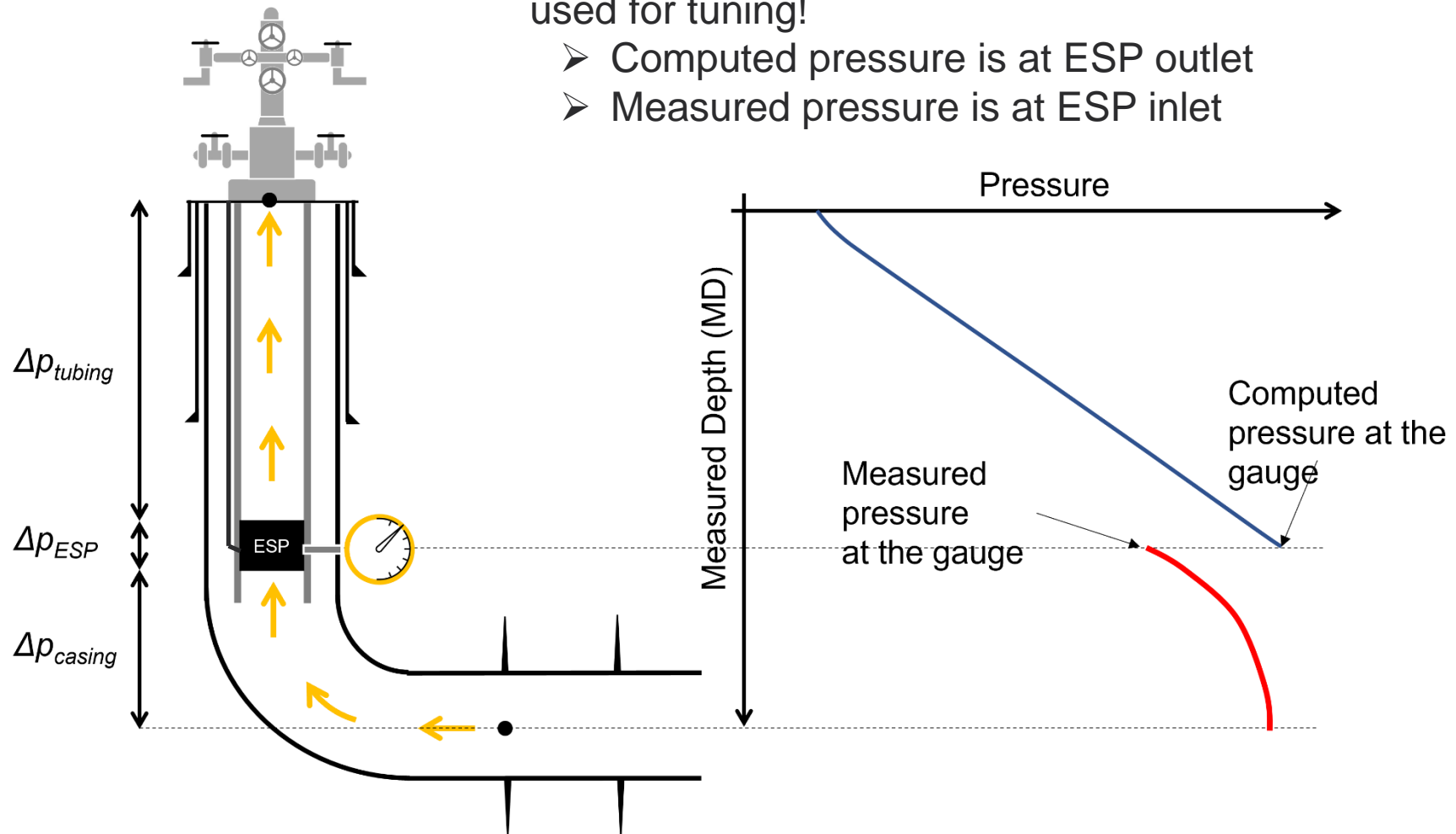
Density at p _{sc} , T _{sc}	Viscosity at p _{sc} , T _{sc}
62.3718 lb/ft³	0.2736 cp

Top Perforation MD	Bottom Perforation MD
340	340
529	528.99
717	716.97
812	811.96
907	906.95
1001	1000.94
1095	1094.93

REMINDER: Tuning of Correlations with ESP

Caution

- Measured pressures from an ESP should not be used for tuning!
 - Computed pressure is at ESP outlet
 - Measured pressure is at ESP inlet



Exercise 3

BHP using Mass Upload Sheet

(Multiple Wells)

Mass Upload – Production Data

	A	B	C	D	E	K	L	M	N
1	Well	Time	Stock Tank Rates			Measured Pressures, Temperatures and Gas-Lift Rates			
2	Name	Date	q _o	q _g	q _w	P _{wf}	P _{tubing}	P _{casing}	q _{g, gas lift}
3	-	-	STB/d	Mscf/d	STB/d	psia	psia	psia	Mscf/d
4	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-01 00:00	504.39	145.0	718	5050	15	2065	
5	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-02 00:00	564.76	186.0	922	5010	15	1990	
6	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-03 00:00	653.51	231.0	753	4796	15	1865	
7	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-04 00:00	740.71	268.0	700	4697	15	1815	
8	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-05 00:00	678.06	261.0	530	4547	15	1715	
9	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-06 00:00	789.29	329.0	580	4886	15	2065	
10	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-07 00:00	915.05	303.0	700	4106	15	1285	
11	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-08 00:00	797.53	260.0	590	3994	15	1185	
12	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-09 00:00	777.06	252.0	530	3853	15	1065	
13	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-10 00:00	710.58	236.0	429	3754	15	995	
14	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-11 00:00	675.50	223.0	380	3658	15	915	
15	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-12 00:00	635.51	210.0	343	3589	15	855	
16	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-13 00:00	705.49	237.0	360	3445	15	725	
17	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-14 00:00	638.78	208.0	332	3388	15	665	
18	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-15 00:00	735.32	247.0	392	3203	15	505	
19	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-01-16 00:00	624.34	204.0	328	3163	15	455	

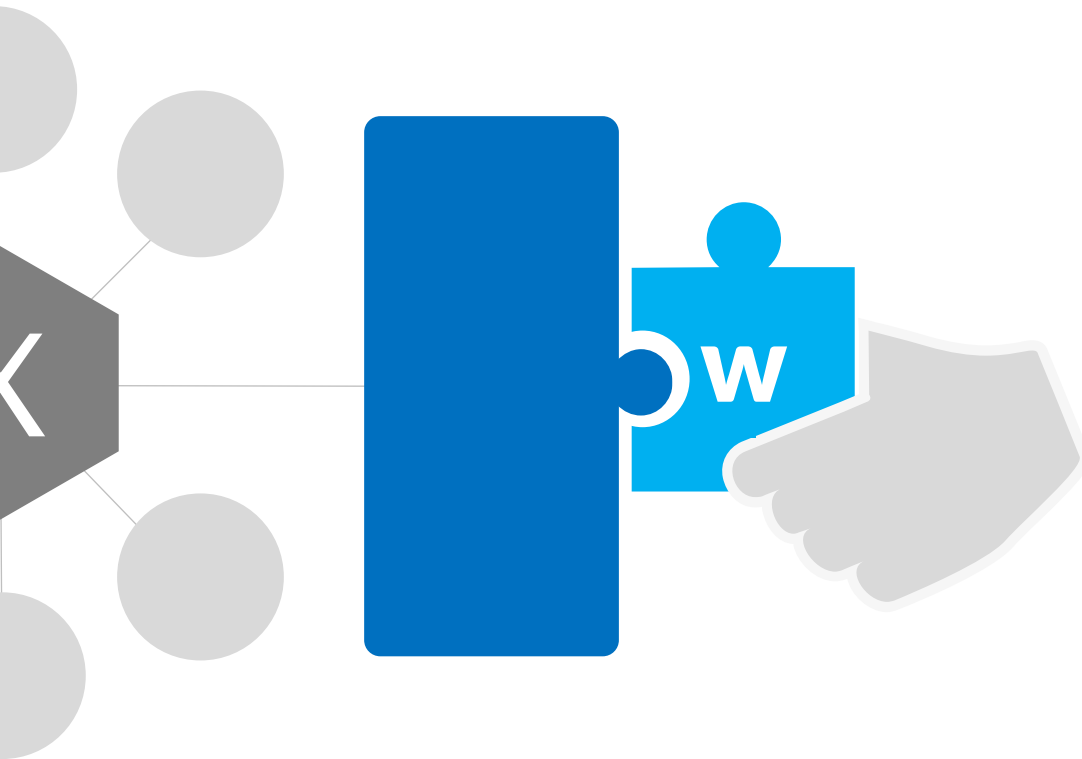
Mass Upload – Deviation Survey

	A	B	C
1	Well Name	MD	TVD
2	-	ft	ft
3	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	0	0
4	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	95.1	95.1
5	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	153.6	153.6
6	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	214.8	214.8
7	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	273.1	273.1
8	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	333.9	333.9
9	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	393	393
10	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	454	454
11	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	513.6	513.6
12	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	576.8	576.8
13	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	640	640
14	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	703.3	703.3
15	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	766.3	766.3
16	SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	829.5	829.5

Mass Upload – Wellbore Data

A1									
Well Name									
A	E	F	G	H	I	J	K	L	M
Well Name	Use from Date	Flowpath	Wellhead Temperature	Tubing Bottom MD	Tubing ID	Tubing OD	Tubing Roughness	Casing 1 Top MD	Casing 1 Bottom MD
-	yyyy-mm-dd or empty	select from list	F	ft	in	in	in	ft	ft
SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY		Casing	70					0	13915
SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2015-03-05	Tubing	70	7022	2.441	2.875	0.0006	0	7029
SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2018-01-05	Tubing	70	6764	2.441	2.875	0.0006	0	6941
SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2018-07-26	Tubing	70	6825	2.441	2.875	0.0006	0	6941
SPE-DATA-REPOSITORY-DATASET-1-WELL-1-OSPREY	2019-05-22	Tubing	70	6764	2.441	2.875	0.0006	0	6941
SPE-DATA-REPOSITORY-DATASET-1-WELL-2-HAWK	2021-01-01	Tubing	60	7325	1.995	2.375	0.0006	0	7549
SPE-DATA-REPOSITORY-DATASET-1-WELL-3-EAGLE	2017-01-01	Tubing	60	7500	2.441	2.875	0.0006	0	15493
SPE-DATA-REPOSITORY-DATASET-1-WELL-4-KITE	2018-01-01	Tubing	65	8332	2.441	2.875	0.0006	0	8384
SPE-DATA-REPOSITORY-DATASET-1-WELL-5-SWIFT	2018-01-01	Tubing	70	7626	2.441	2.875	0.0006	0	7693
SPE-DATA-REPOSITORY-DATASET-1-WELL-5-SWIFT	2020-06-17	Tubing	70	7626	2.441	2.875	0.0006	0	7693
SPE-DATA-REPOSITORY-DATASET-1-WELL-6-SPARROW	2018-01-01	Tubing	70	7682	2.441	2.875	0.0006	0	7559
SPE-DATA-REPOSITORY-DATASET-1-WELL-6-SPARROW	2020-06-12	Tubing	70	7682	2.441	2.875	0.0006	0	7559
SPE-DATA-REPOSITORY-DATASET-1-WELL-7-LARK	2019-01-01	Tubing	70	8174	2.441	2.875	0.0006	0	7975
SPE-DATA-REPOSITORY-DATASET-1-WELL-7-LARK	2020-03-17	Tubing	70	8174	2.441	2.875	0.0006	0	7975
SPE-DATA-REPOSITORY-DATASET-1-WELL-8-CARDINAL	2019-01-01	Tubing	70	8211	2.441	2.875	0.0006	0	8031
SPE-DATA-REPOSITORY-DATASET-1-WELL-8-CARDINAL	2020-05-12	Tubing	70	8211	2.441	2.875	0.0006	0	8031
SPE-DATA-REPOSITORY-DATASET-1-WELL-9-JAY	2019-01-01	Tubing	70	8050	2.441	2.875	0.0006	0	7905
SPE-DATA-REPOSITORY-DATASET-1-WELL-9-JAY	2020-05-13	Tubing	70	8050	2.441	2.875	0.0006	0	7905
SPE-DATA-REPOSITORY-DATASET-1-WELL-10-CROW	2020-01-01	Tubing	70	8000	1.995	2.375	0.0006	0	7940
SPE-DATA-REPOSITORY-DATASET-1-WELL-11-FALCON	2021-02-09	Tubing	60	7595	1.995	2.375	0.0006	0	7499

API & Database



Plug-in API

Plug our API into already existing databases and solutions

DB Connection

Expose your DB tables to us and we will make the updates

Input & Output

Flexible API allows for two way communication and dataflow

Appendix

Multiphase Flow

No Slip:

- Assumes gas and liquid flow with the same velocity

$$v_g = v_L$$

- Define liquid-flux fraction

$$C_L = \frac{q_L}{q_L + q_g}$$

- Gas and liquid properties are averaged by

$$\rho_m = C_L \rho_L + (1 - C_L) \rho_g$$

$$\mu_m = C_L \mu_L + (1 - C_L) \mu_g$$

Slip:

- Assumes gas flows faster than liquid

$$v_g \geq v_L$$

- Define liquid hold-up (= 1 - void fraction)

$$H_L = \frac{A_L}{A_L + A_g}$$

$$H_L = \frac{q_L}{q_L + \frac{v_L}{v_g} q_g} \stackrel{v_g \geq v_L}{\geq} \frac{q_L}{q_L + q_g} = C_L$$

- Gas and liquid properties are averaged by

$$\rho_s = H_L \rho_L + (1 - H_L) \rho_g$$

$$\mu_s = H_L \mu_L + (1 - H_L) \mu_g$$

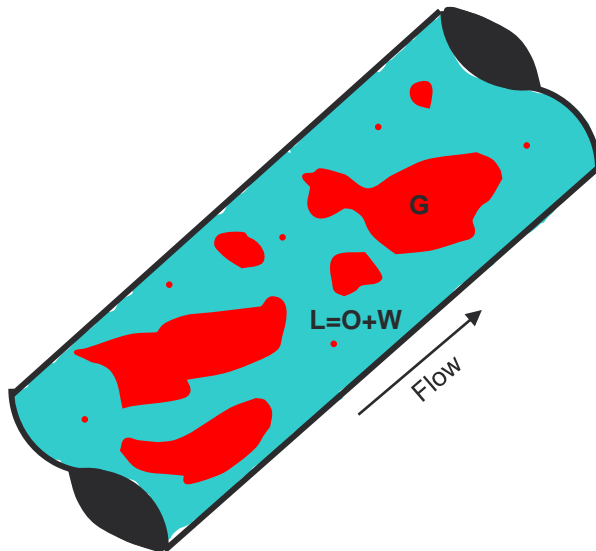
Multiphase Flow—Liquid Hold-Up

- The liquid hold-up represents the part of the pipe cross-sectional area occupied by liquid.

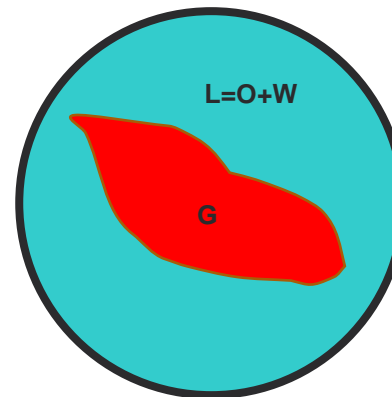
$$C_L = \frac{q_L}{q_L + q_g} = \frac{v_L A_L}{v_L A_L + v_g A_g} = \frac{A_L}{A_L + \frac{v_g}{v_L} A_g}$$



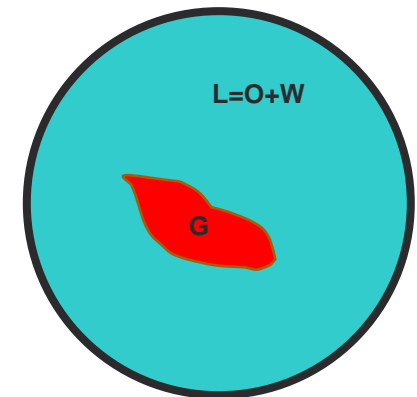
If $v_g > v_L$, then $C_L < H_L$,
 → Using C_L rather than H_L
 will account for too much gas
 in the cross-sectional area



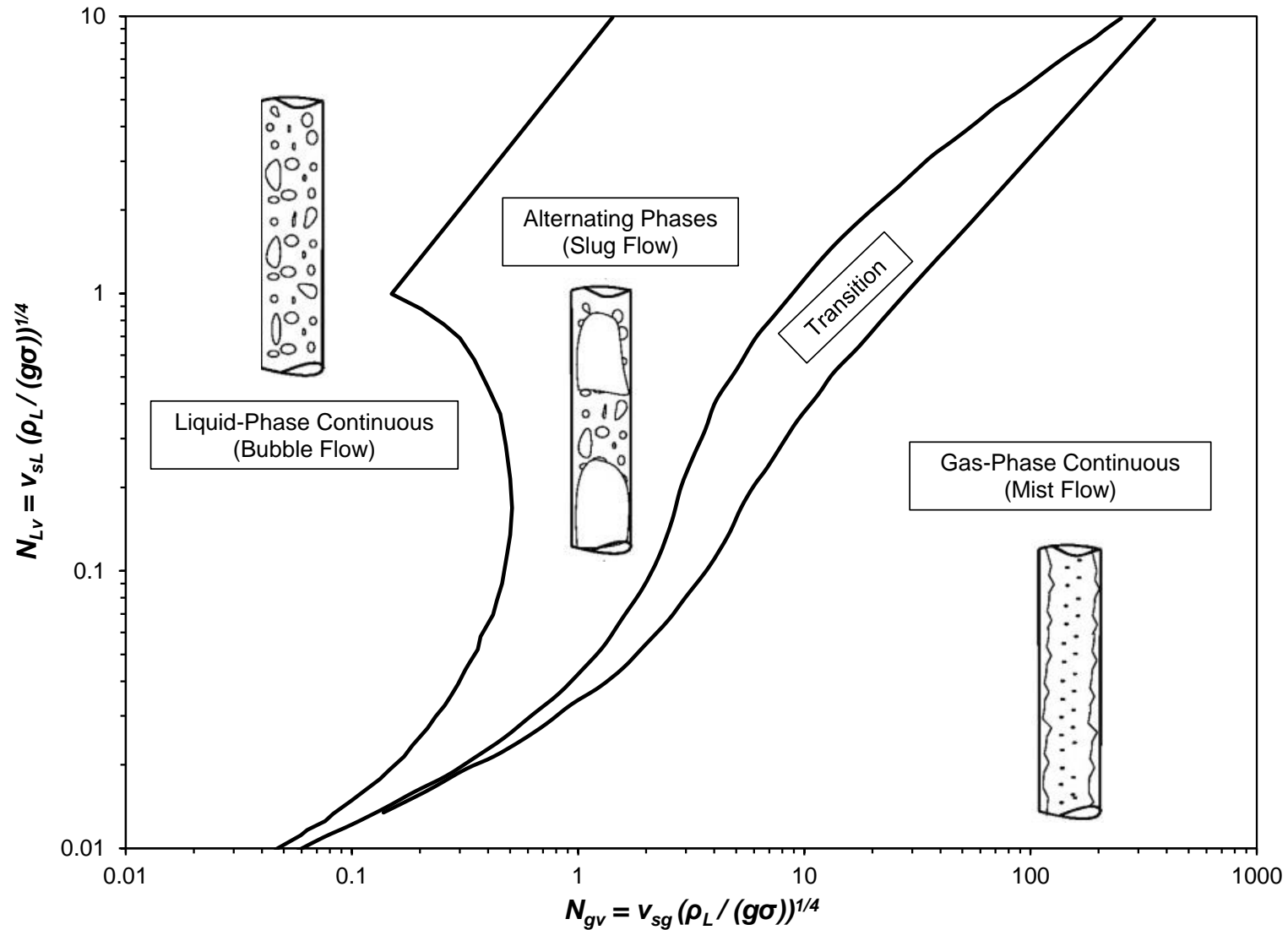
$$C_L = \frac{q_L}{q_g + q_L}$$



$$H_L = \frac{A_L}{A_g + A_L}$$



Flow Regimes—Gould et al. (1974)



Multiphase Flow—Pressure Gradient

- Velocity gradient in acceleration term is approximated as

$$\frac{dv_m}{ds} \approx -\frac{v_{sg}}{p} \frac{dp}{ds}$$

- Pressure gradient is rewritten to

$$-\frac{dp}{ds} = \frac{\rho_g \frac{g}{g_c} \cos(\theta) + \frac{f_{Ds} \rho_f v_m^2}{2d_h g_c}}{1 - \frac{\rho_a v_m v_{sg}}{g_c p}}$$

- The correlations provide the method of calculating the different terms in the equation

Multiphase Flow—Three Examples

- Same well configuration, three different fluids flowing

	BO	VO	GC
q_o (STB/d)	2000	1000	100
q_g (Mscf/d)	1000	2500	2500
q_w (STB/d)	100	100	5
p_{th} (psia)	200	200	200
T_{wh} (°F)	100	100	100
T_R (°F)	200	200	230
GOR (scf/STB)	500	2500	25000
WOR (STB/STB)	0.1	0.05	0.1

Multiphase Flow—Three Examples

- Same well configuration, three different fluids flowing

Well Data

1 Well Deviation Survey

2 Well Data

Perforated Interval

Top Perforation MD
7958 ft

Bottom Perforation MD
15439 ft

Deviation Survey

(Input entire survey, table expands with input)

Measured Depth (MD) (ft)	True Vertical Depth (TVD) (ft)
0.0	0.0
28	28
147	146.99
327	326.96
506	505.91
685	684.68
864	863.1
1043	1041.43
1222	1219.75
1401	1398.11

Well Data

1 Well Deviation Survey

2 Well Data

Configuration 1

Flowpath: Tubing

Artificial Lift: None

1 Wellbore Configuration 1 (Initial)

Casing Data

Pipe No. (#)	Top MD (ft)	Bottom MD (ft)	ID (in)	Roughness (in)
1	0	15493	4.778	0.0006

Tubing Data

Pipe No. (#)	Bottom MD (ft)	ID (in)	OD (in)	Roughness (in)
1	7000	2.441	2.875	0.0006

Flowpath
Tubing

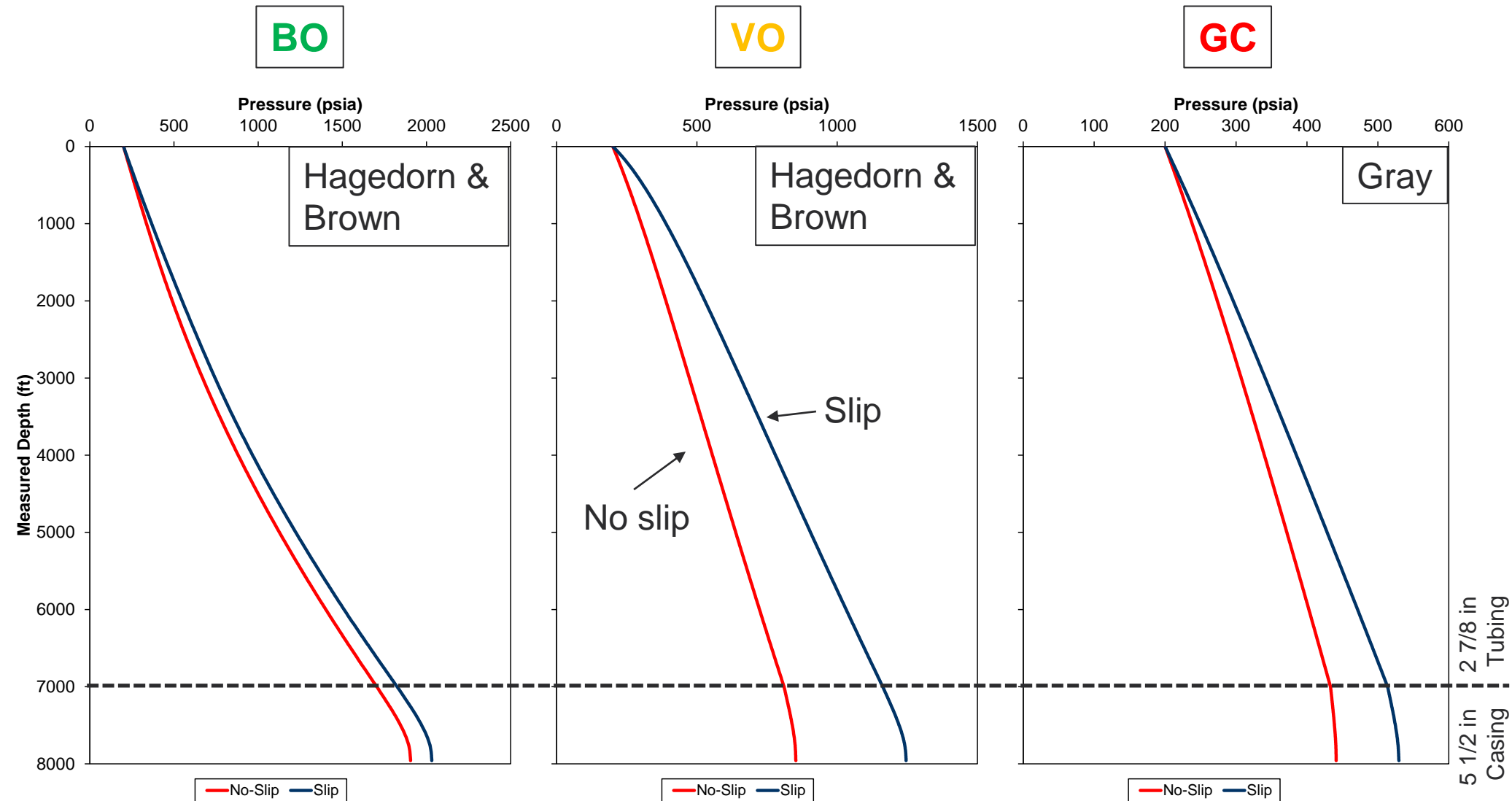
Artificial Lift Method
None

Gauge Depth
0 ft

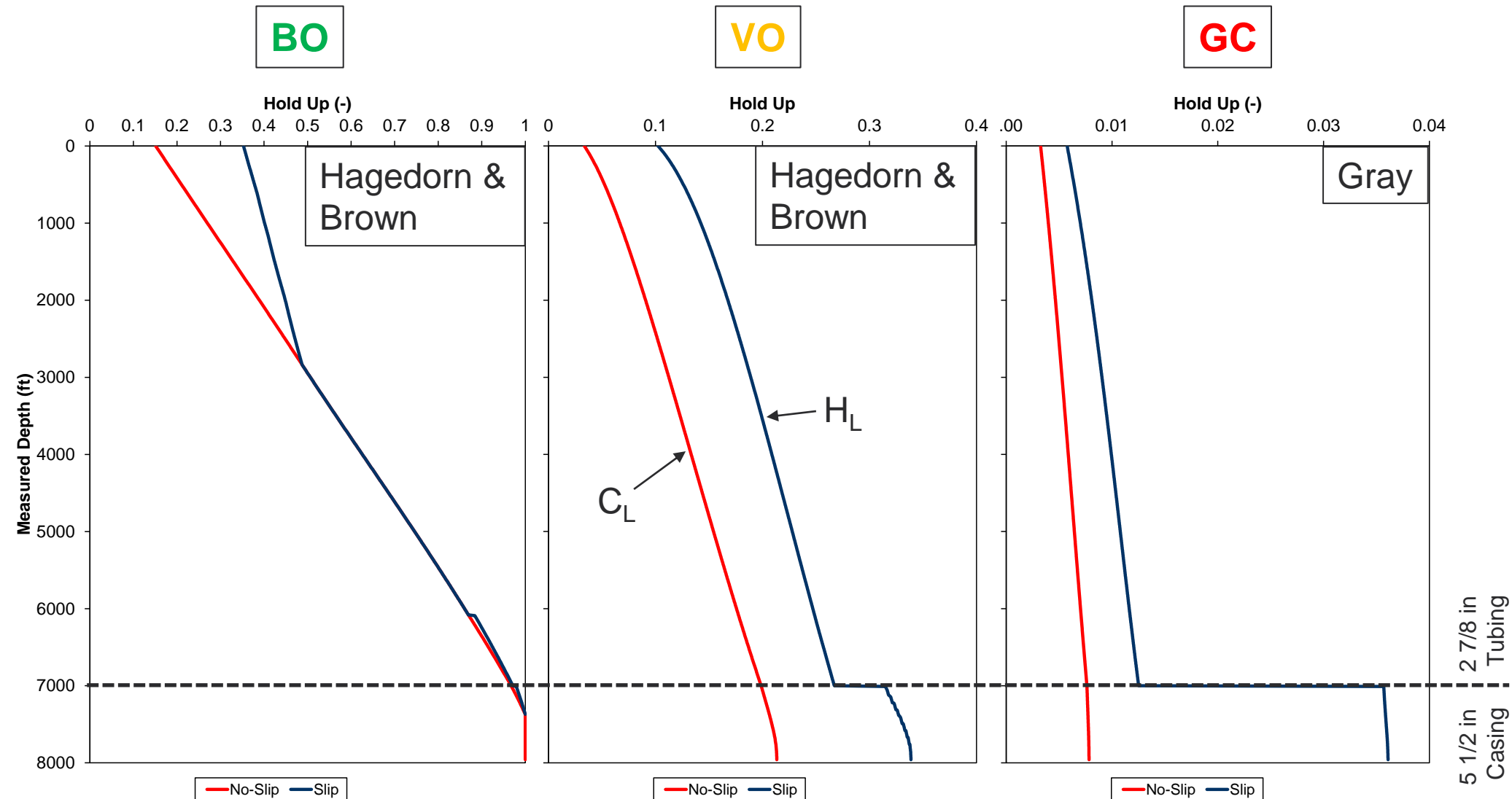
Calculate from gauge to sandface using measured pressures

SAVE

Multiphase Flow—Pressure Profile



Multiphase Flow—Liquid Fractions



Multiphase Flow—Pressure Gradient

BO

VO

GC

Pressure Loss as Fraction of Total Loss

Pressure Loss as Fraction of Total Loss

Pressure Loss as Fraction of Total

0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%

0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%

0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%

Hagedorn & Brown

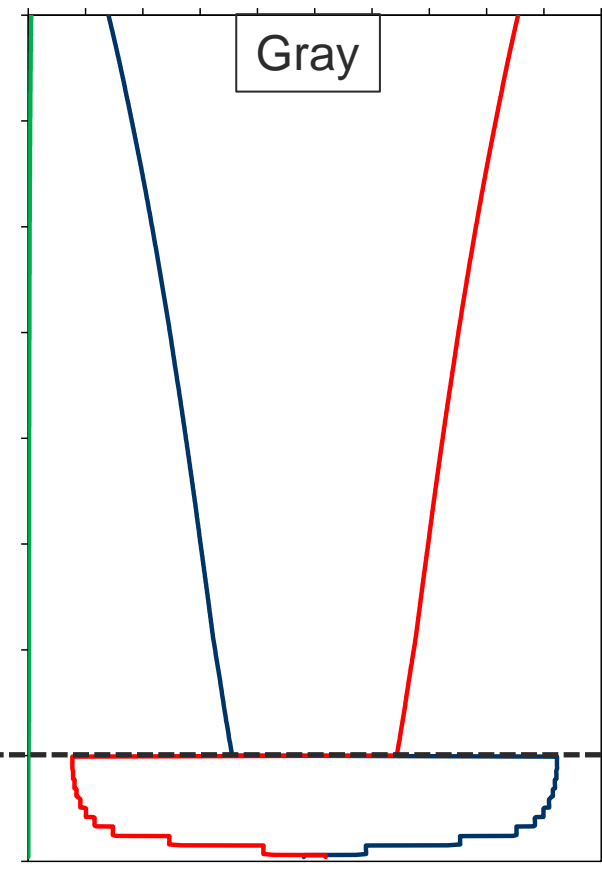
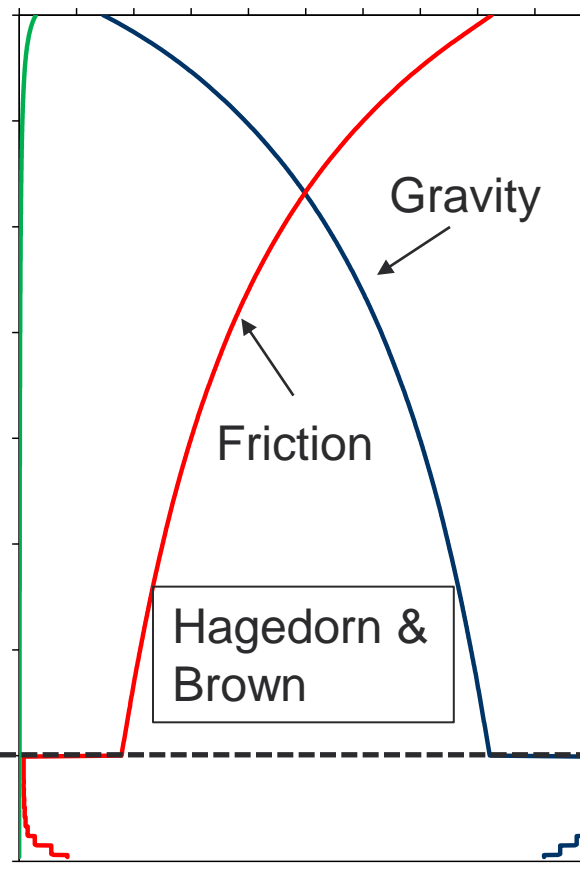
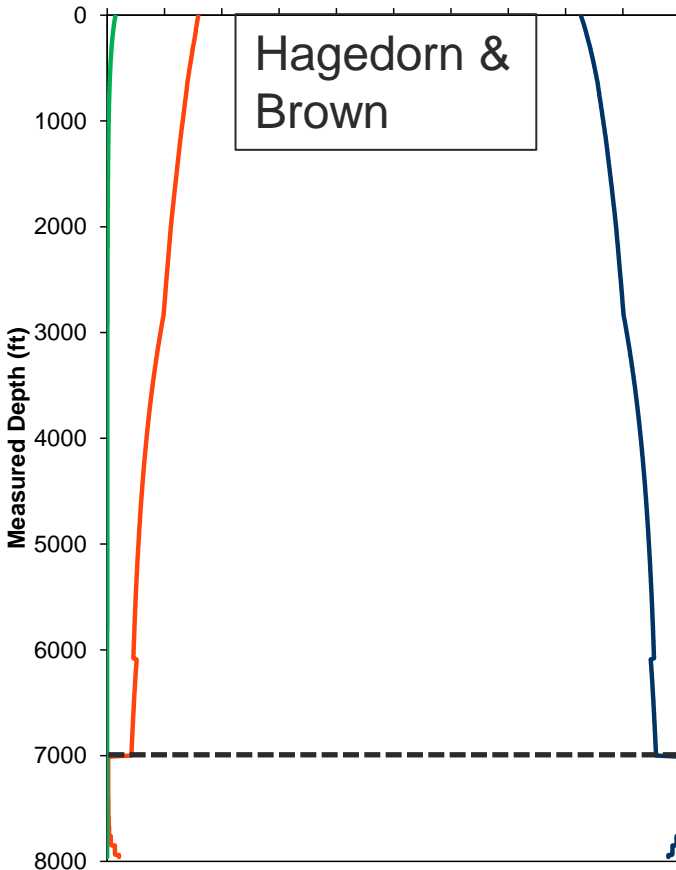
Hagedorn & Brown

Gray

Gravity

Friction

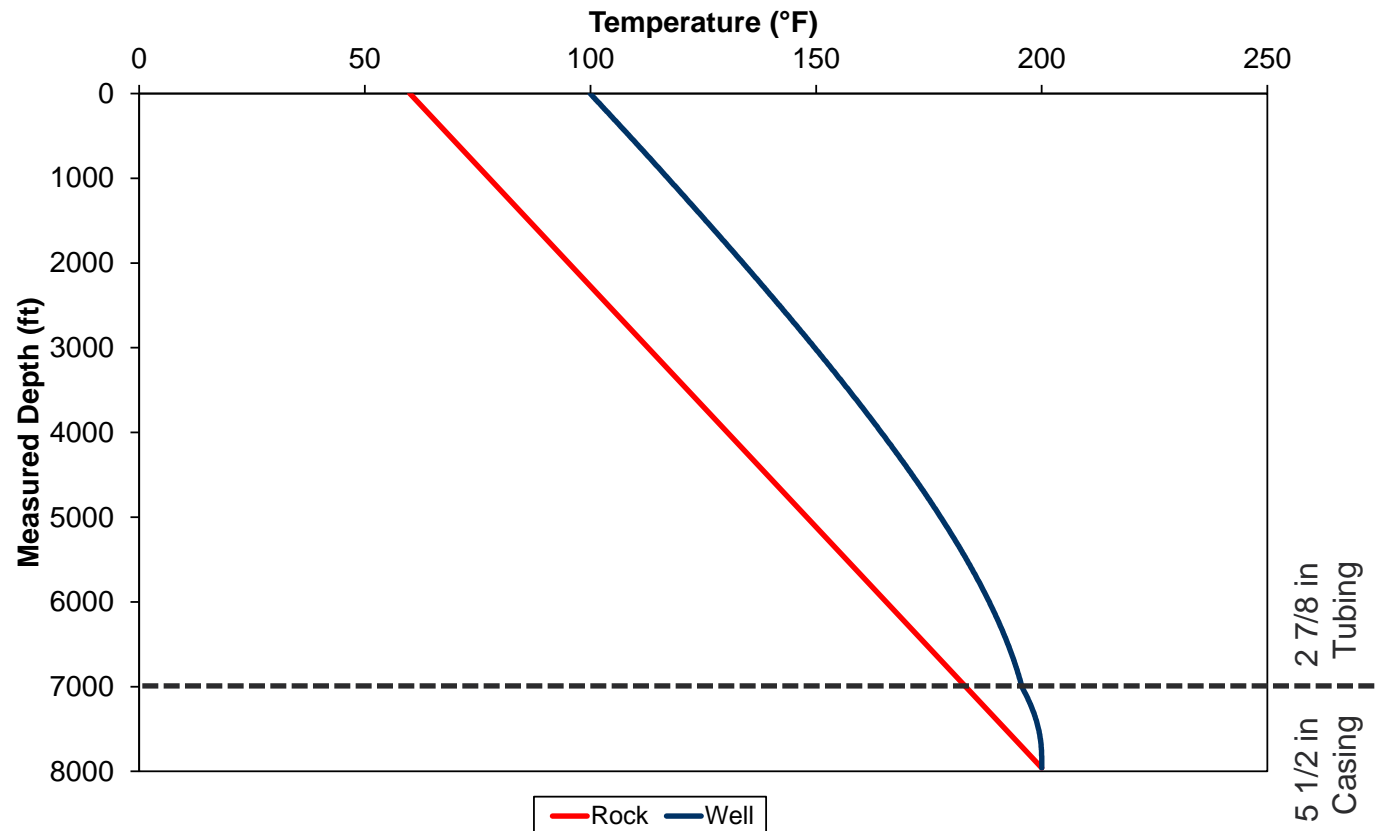
5 1/2 in
2 7/8 in
Tubing
Casing



BHP Calculations—Temperature Gradient

- Simple thermodynamic relationships give a temperature gradient on the form

$$-\frac{dT}{ds} = \frac{U\pi d_h}{c_p \dot{m}} (T - T_{rock})$$



Correlations

Correlations—Hagedorn and Brown

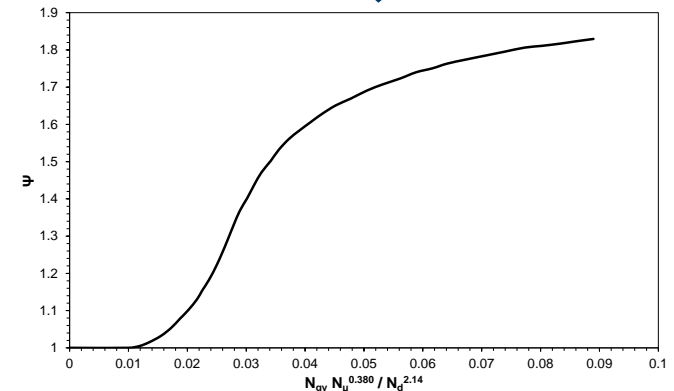
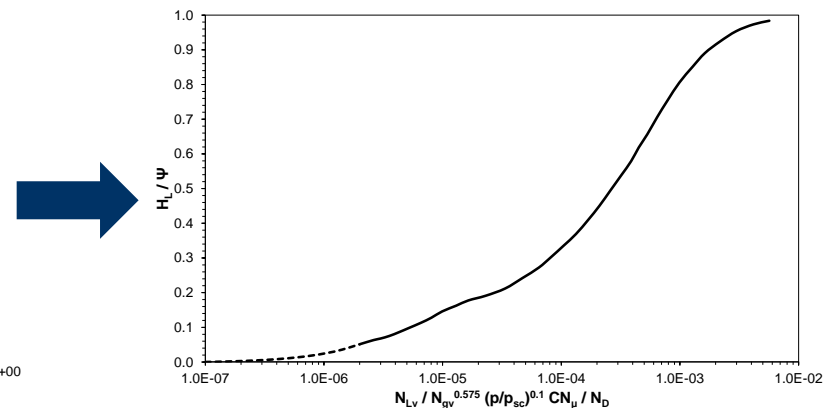
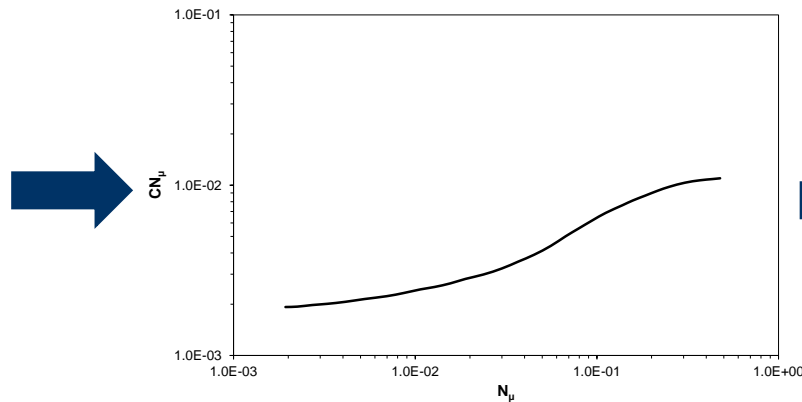
- Hagedorn and Brown (1965)
- Liquid hold-up is calculated by four dimensionless numbers and graphical lookup.

$$N_{Lv} = v_{sL} \left(\frac{\rho_L}{g\sigma} \right)^{1/4}$$

$$N_{gv} = v_{sg} \left(\frac{\rho_L}{g\sigma} \right)^{1/4}$$

$$N_d = d_h \left(\frac{\rho_L g}{\sigma} \right)^{1/2}$$

$$N_\mu = \mu_L \left(\frac{g}{\rho_L \sigma^3} \right)^{1/4}$$



Calculate pressure gradient by setting

$$\rho_g = \rho_a = \rho_s$$

$$\rho_f = \rho_m^2 / \rho_s$$

$$f_{Ds} = f_D(N_{Re}) \text{ where } N_{Re} = \rho_s v_m d_h / (\mu_L^{H_L} \mu_g^{1-H_L})$$

Correlations—Hagedorn and Brown

- It's common to apply a modification to the original Hagedorn and Brown when bubble flow occurs. The modification follows the suggested calculation by Griffith.

Bubble flow occurs when

$$1 - C_L < \max \left\{ 1.071 - 0.2218 \frac{v_m^2}{d_h}, 0.13 \right\}$$

Calculate liquid hold-up by

$$H_L = -\frac{v_m - v_s + \sqrt{(v_m - v_s)^2 + 4v_s v_L}}{2v_s}$$

$$v_s = 0.8 \text{ ft/s}$$

Calculate the pressure gradient by setting

$$\rho_g = \rho_a = \rho_s$$

$$\rho_f = \rho_L$$

$$v_m = v_L$$

$$f_{Ds} = f_D(N_{Re}) \text{ where } N_{Re} = \rho_L v_L d_h / \mu_L$$

Correlations—Beggs and Brill

- Beggs and Brill (1973)
- Relies on calculating the liquid hold-up for horizontal flow, and then correcting it by inclination.

$$\frac{H_L(\phi)}{H_L(0)} = \psi$$

- Both the horizontal liquid hold-up and the inclination correction factor are functions of flow regime.

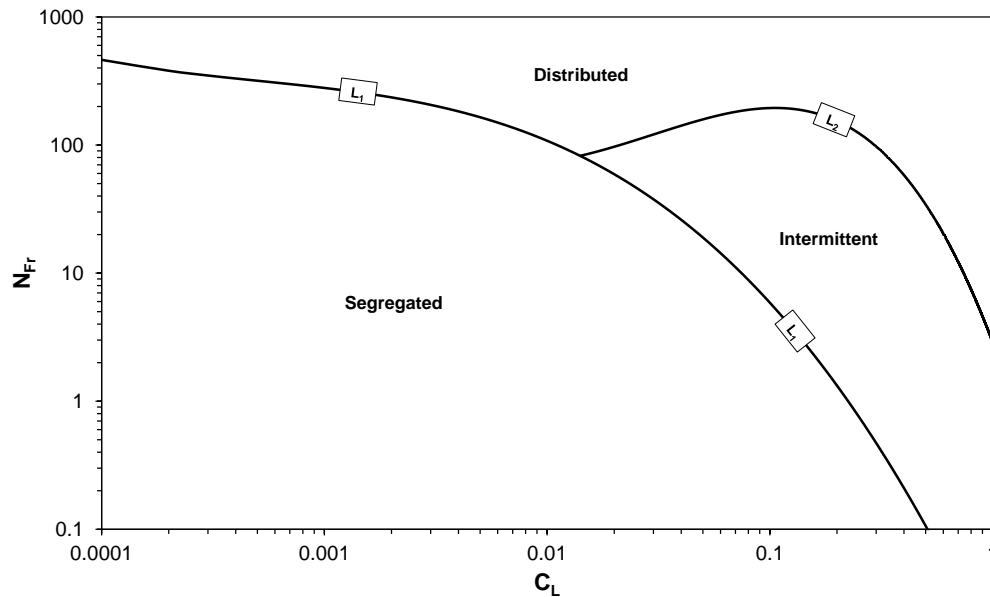
$$H_L(0) = AC_L^\alpha N_{Fr}^\beta \quad \psi = 1 + \left[(1 - C_L) \ln(DC_L^\delta N_{Fr}^\epsilon N_{Lv}^\zeta) \right] \left(\sin(\phi) - \frac{1}{3} \sin(\phi)^3 \right)$$

	A	α	β	D	δ	ϵ	ζ
Segregated	0.98	0.4846	-0.0868	0.011	-3.768	-1.614	3.539
Intermittent	0.845	0.5351	-0.0173	2.96	0.305	0.0978	-0.4479
Distributed	1.065	0.5824	-0.0609	1	0	0	0

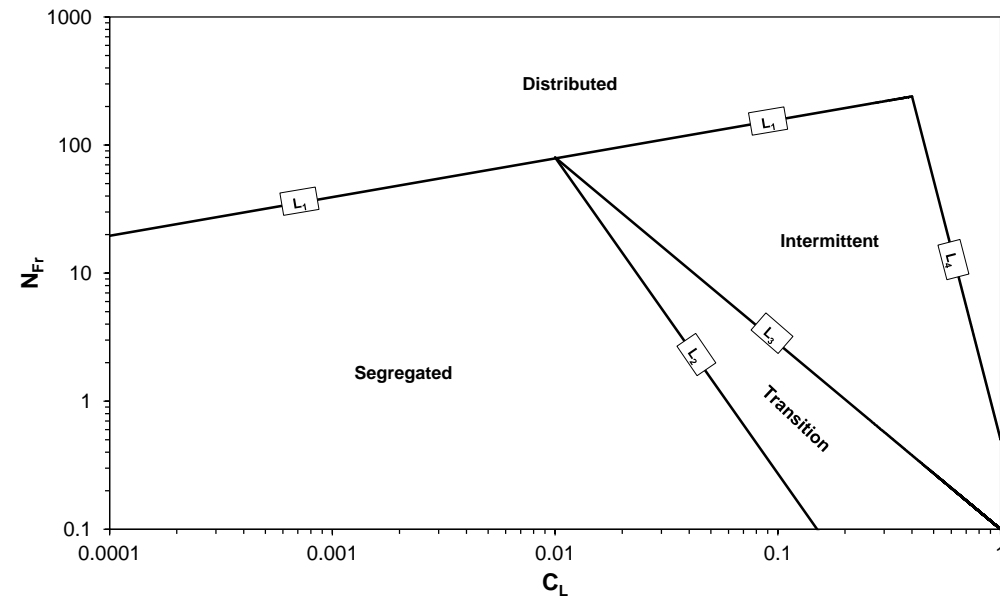
Correlations—Beggs and Brill

- Flow-regime map in the original paper is replaced by a later suggested map that includes “transition” flow.

Original Flow Map



Revised Flow Map



$$N_{Fr} = \frac{v_m^2}{gd_h} \text{ Froude Number}$$

Correlations—Beggs and Brill

- Friction factor is corrected to account for multiphase flow

$$\frac{f_{Ds}}{f_D} = e^S$$

where S is a function of $H_L(\phi)$.

Calculate the pressure gradient by setting:

$$\rho_g = \rho_a = \rho_s$$

$$\rho_f = \rho_m$$

$$f_D(N_{Re}) \text{ where } N_{Re} = \rho_m v_m d_h / \mu_m$$

Correlations—Gray

- Gray (1971)
 - Published in *User's Manual for API 14B SCSSV Sizing Computer Program*
- Assumes mist flow in well → Only applicable in gas wells
- Corrects the friction term by using an effective roughness that reflects liquid adhering to the pipe wall.

Calculate the pressure gradient by setting:

$$\rho_g = \rho_a = \rho_s$$

$$\rho_f = \rho_m$$

$$f_{Ds} = f_D(N_{Re}) \text{ where } N_{Re} = \rho_m v_m d_h / \mu_m \text{ and } k_{eff} / d_h \text{ instead of } k / d_h$$

Correlations—Woldesemayat and Ghajar

- Woldesemayat and Ghajar (2007)
- Correlation based on an extensive review of correlations and data for inclined pipe flow.

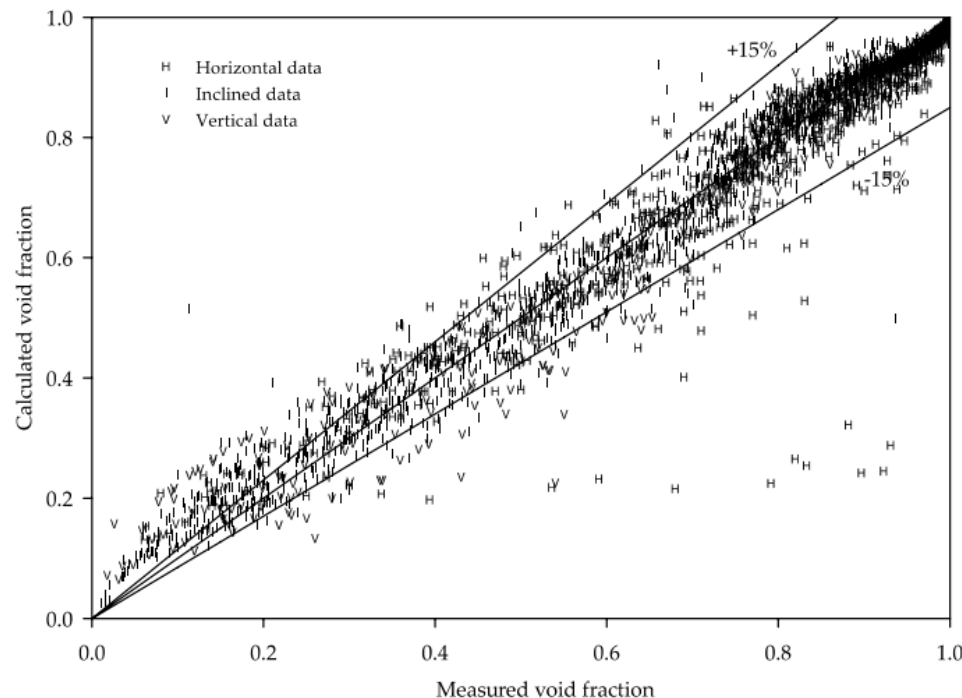


Fig. 7. Comparison of present study correlation with measured combined total experimental data.

Calculate the pressure gradient by setting:

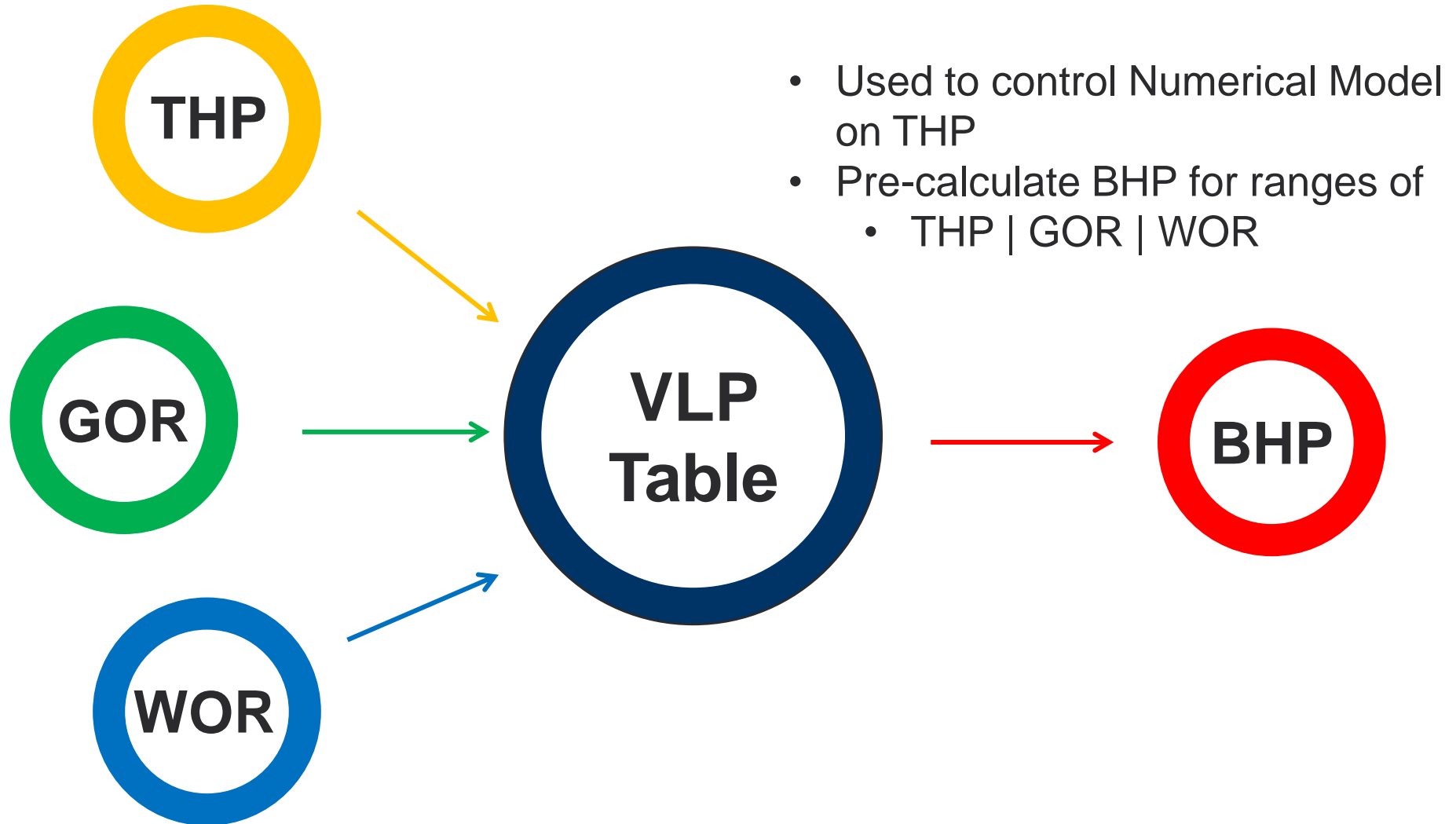
$$\rho_g = \rho_a = \rho_f = \rho_s$$

$$f_D(N_{Re}) \text{ where } N_{Re} = \rho_s v_m d_h / \mu_s$$

Tubing Tables / VLP in Numerical Model

Vertical Lift Performance Tables

“Tubing Tables”



We support energy companies, oil services companies, investors and government organizations with expertise and expansive analysis within PVT, gas condensate reservoirs and gas-based EOR. Our coverage ranges from R&D based industry studies to detailed due diligence, transaction or court case projects.

We help our clients find best possible answers to complex questions and assist them in the successful decision-making on technical challenges. We do this through a continuous, transparent dialog with our clients - before, during and after our engagement.

The company was founded by Dr. Curtis Hays Whitson in 1988 and is a Norwegian corporation located in Trondheim, Norway, with local presence in USA, Middle East, India and Indonesia.

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